



COSMOLOGY FROM HOME 2022

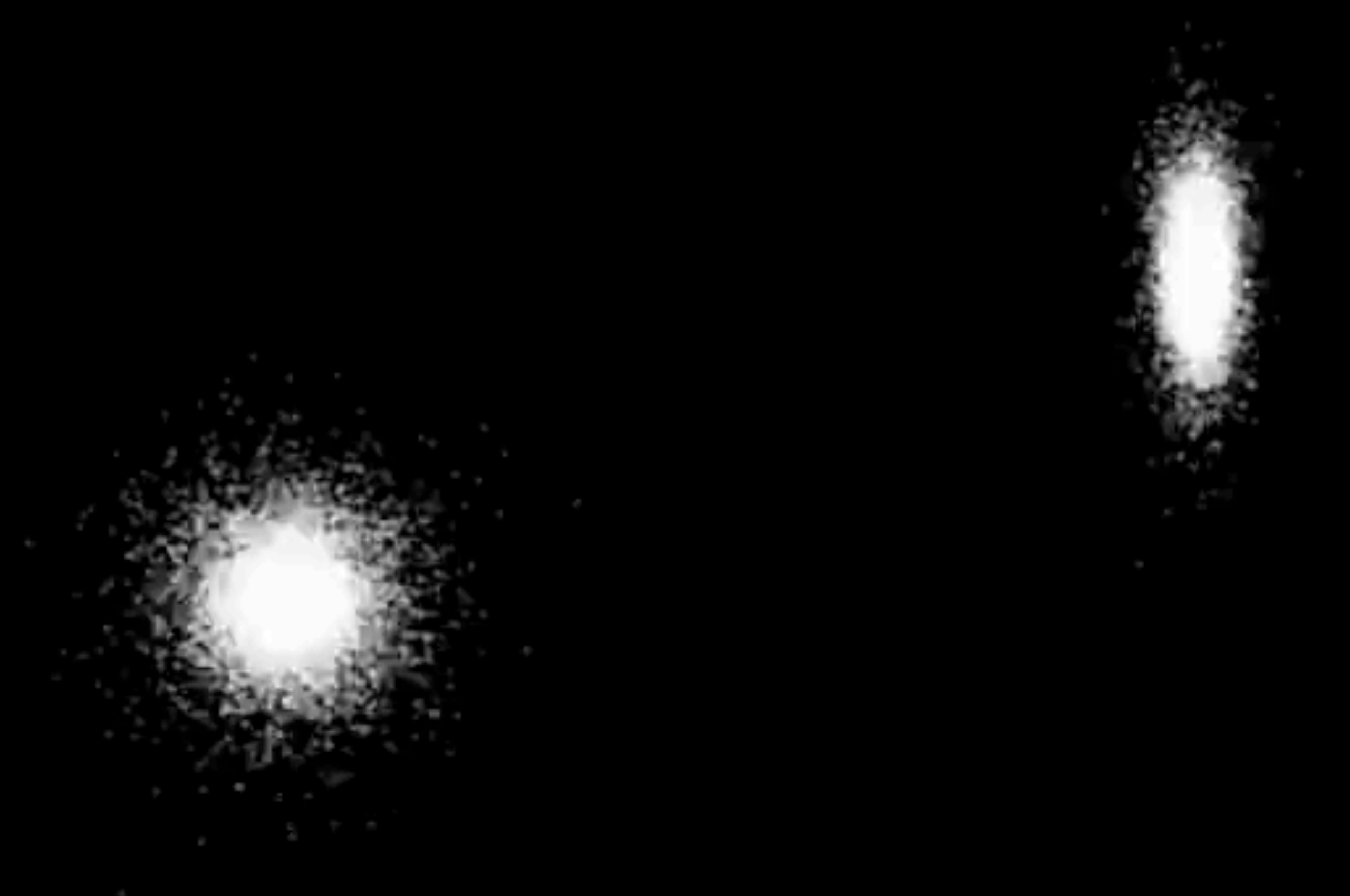
# EVOLUTION OF MASSIVE BLACK HOLE BINARIES IN MERGING NUCLEAR STAR CLUSTERS

ARXIV: 2205.12289

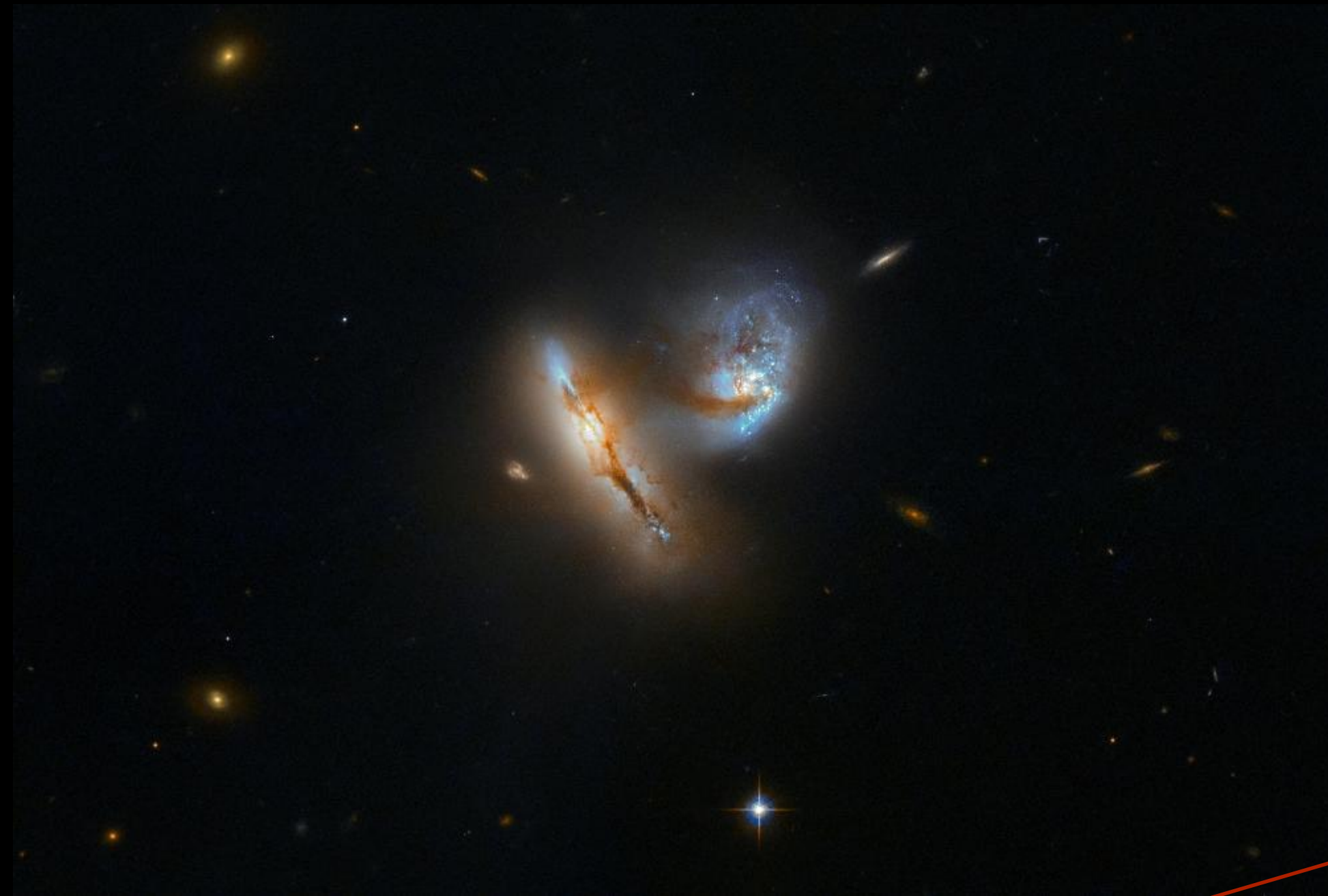
DIPTAJYOTI MUKHERJEE ([DIPTAJYM@ANDREW.CMU.EDU](mailto:DIPTAJYM@ANDREW.CMU.EDU))  
PHD CANDIDATE | CARNEGIE MELLON UNIVERSITY

Image credit: NASA, ESA, and J. Olmstead (STScI)

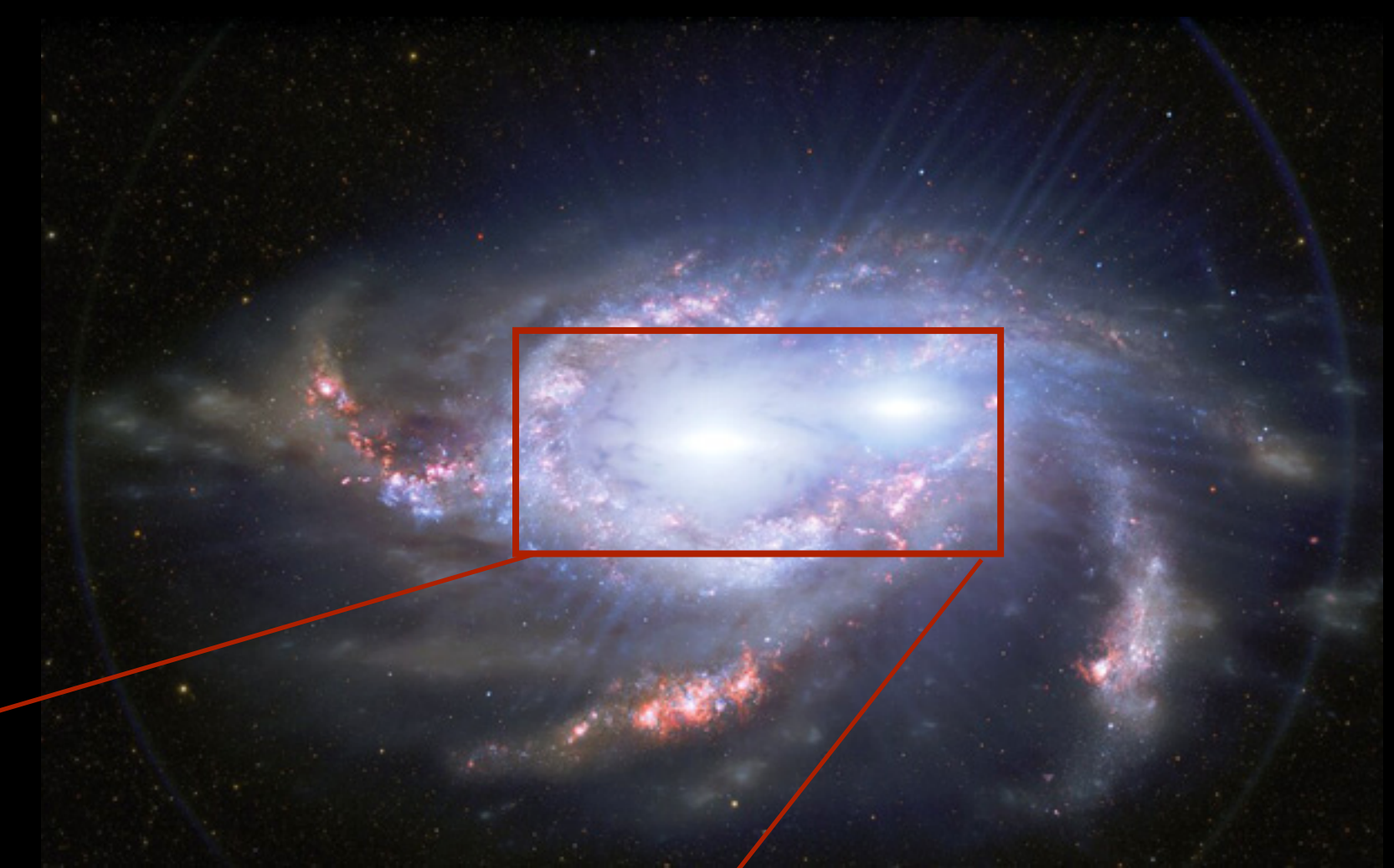
# HIERARCHICAL GROWTH



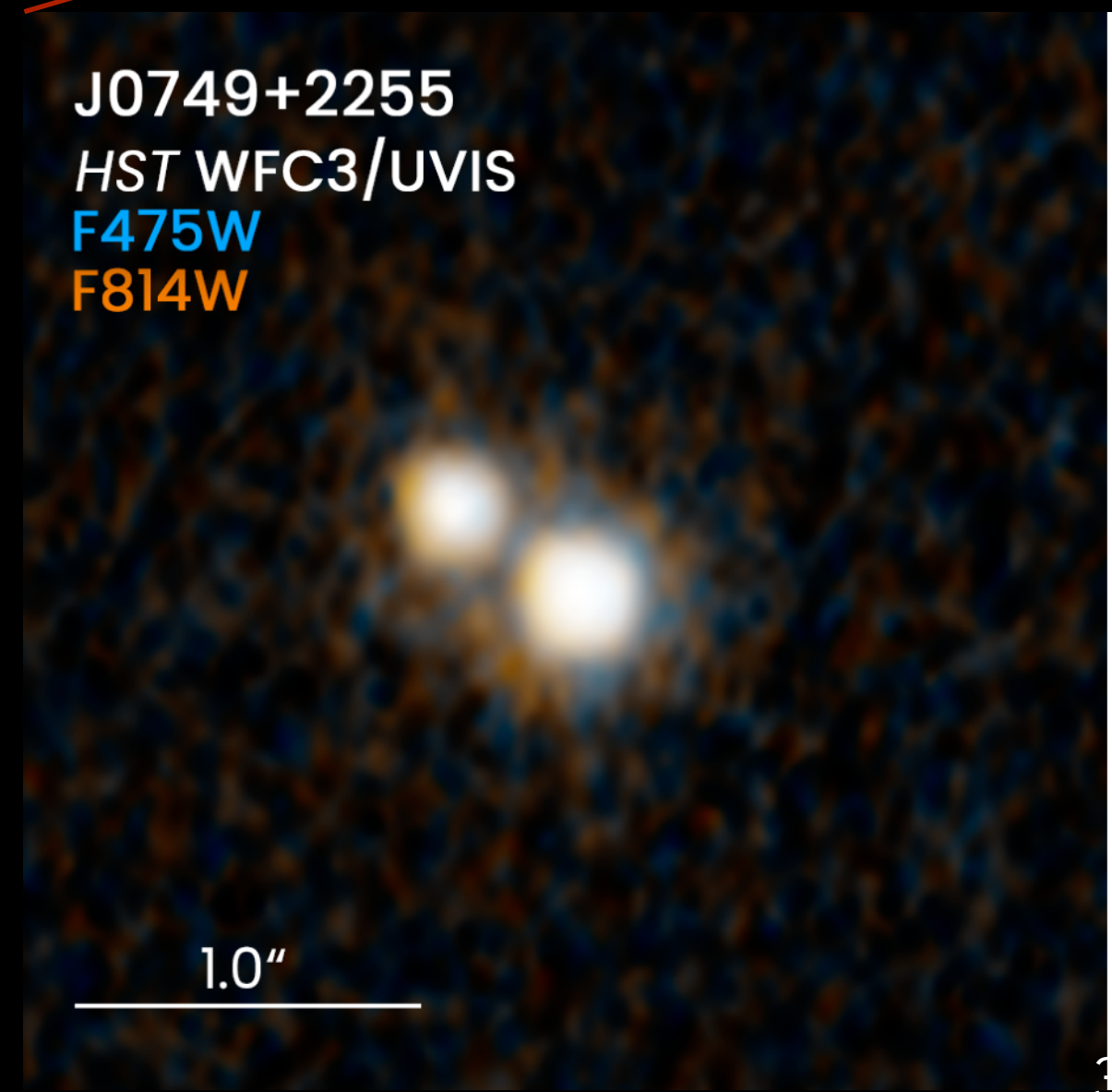
Simulation performed using GADGET-2 (Springel 2005)



~kpc

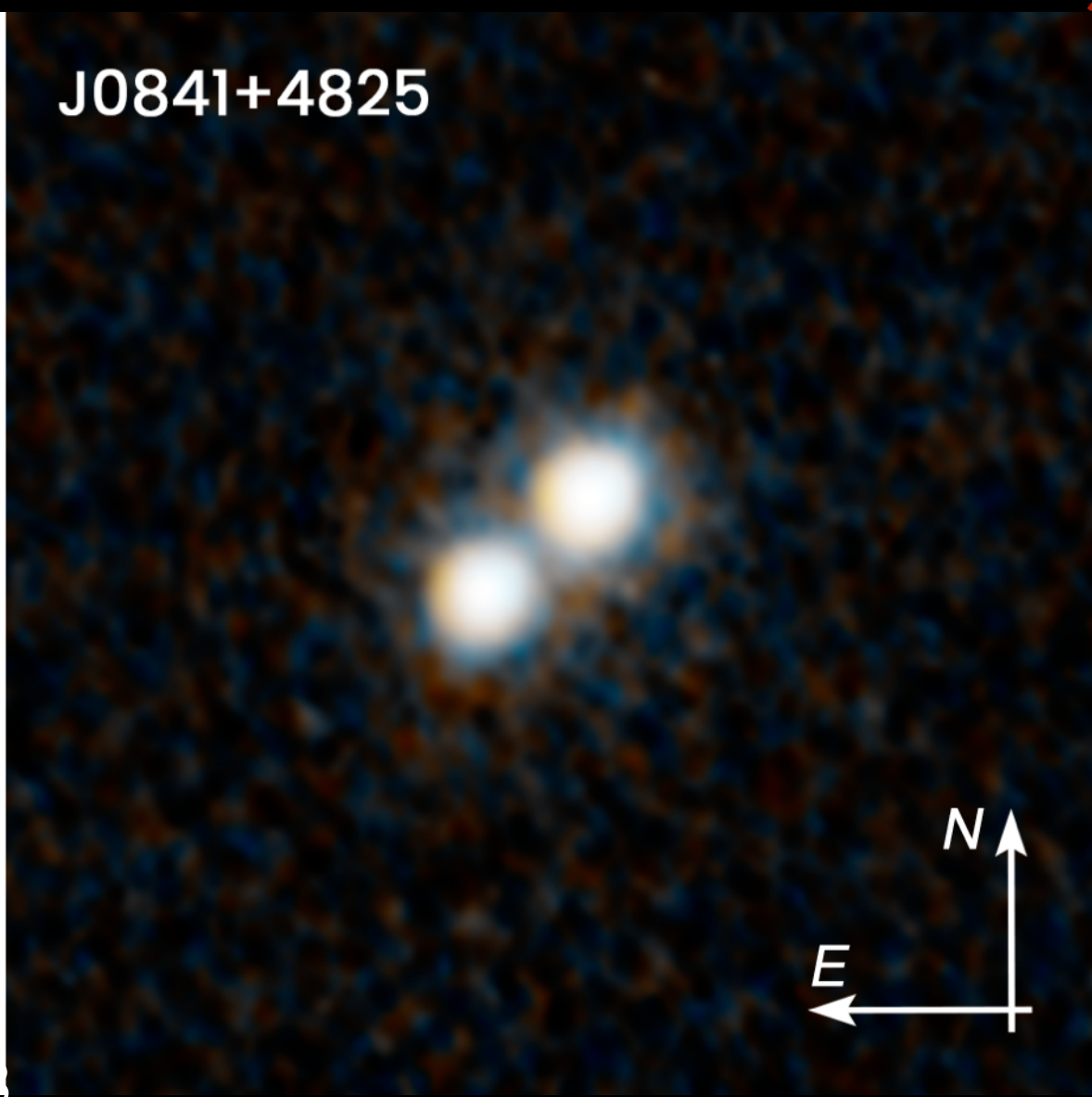


< pc



J0749+2255  
HST WFC3/UVIS  
F475W  
F814W

1.0"



J0841+4825

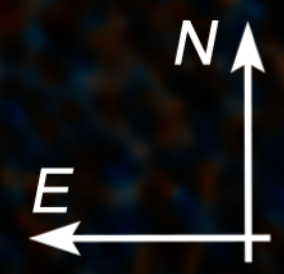
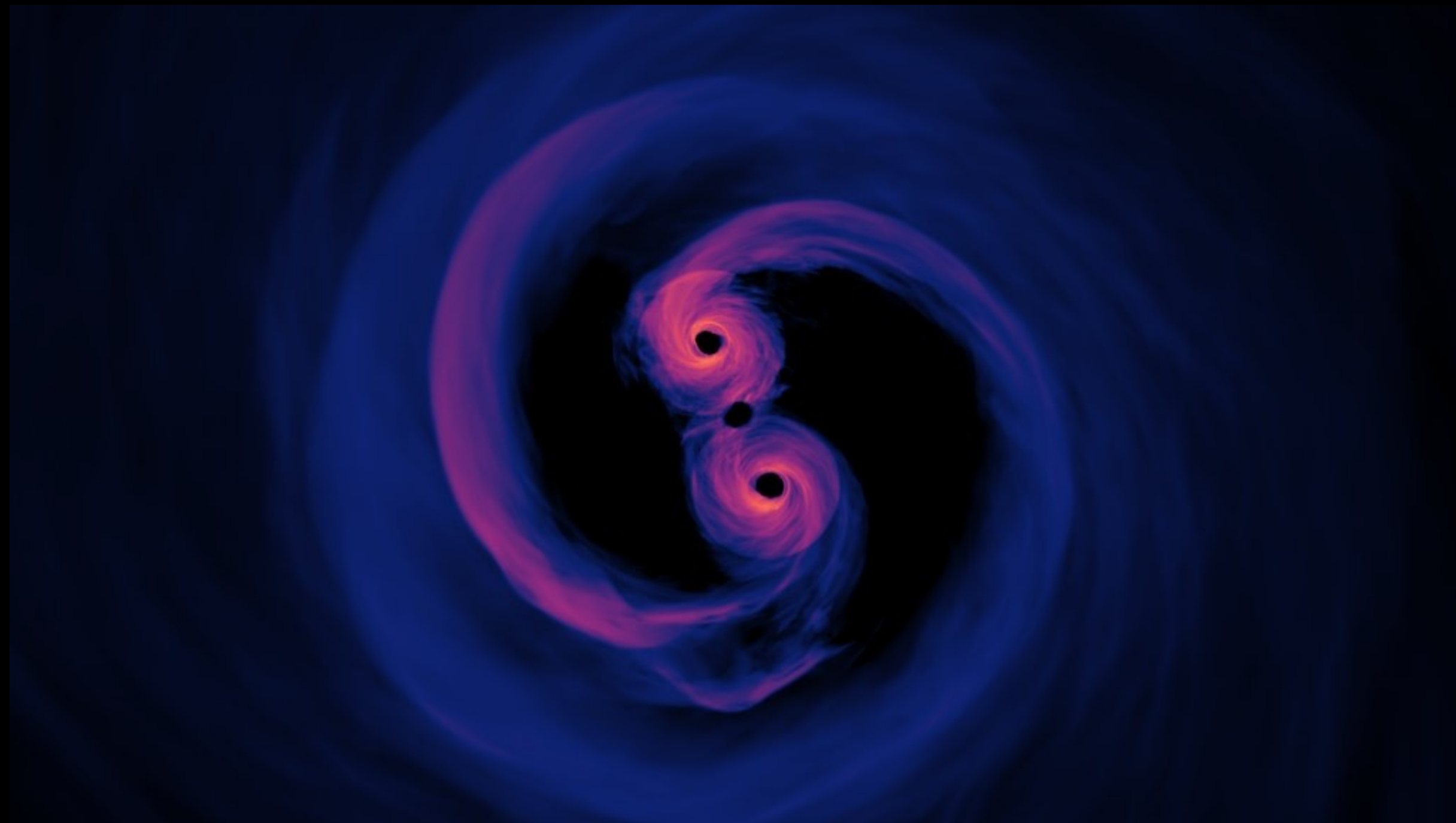


Image credits: NASA, ESA, Hsiang-Chih Hwang (JHU), Nadia Zakamska (JHU), Yue Shen (UIUC)

# MASSIVE BLACK HOLE BINARIES



One of the most important LISA sources

Theories of formation and assembly uncertain

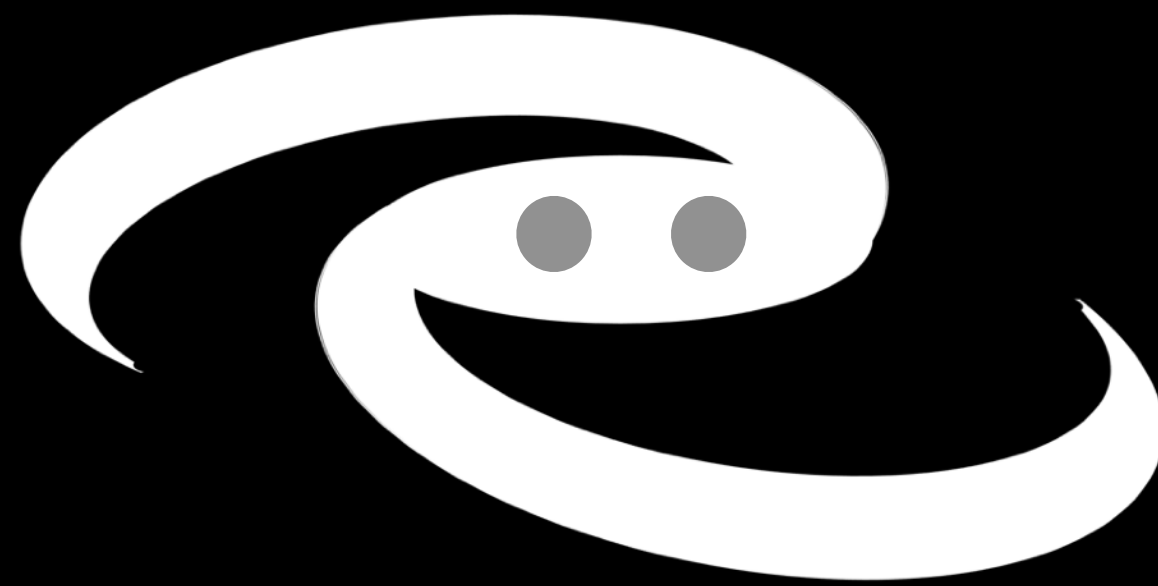
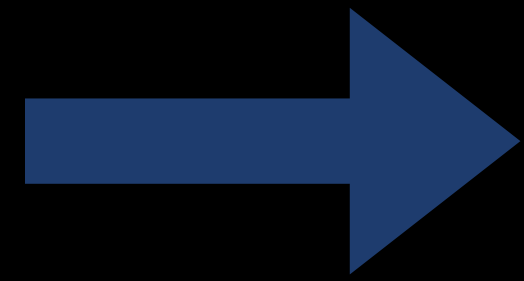
Dynamics sensitive to the surrounding environment

To maximize LISA science output, theoretical advances needed in dynamics and evolution!



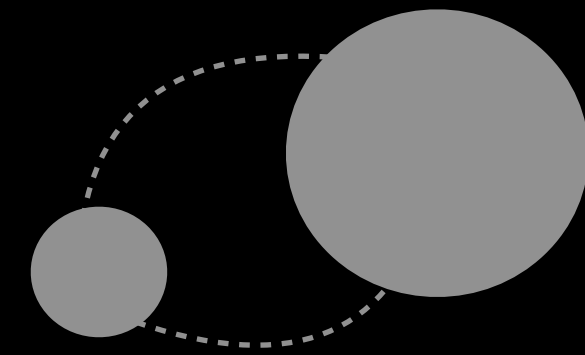
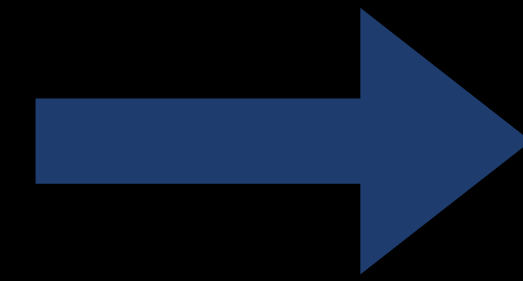
~kpc

dynamical friction from  
surrounding media



~pc

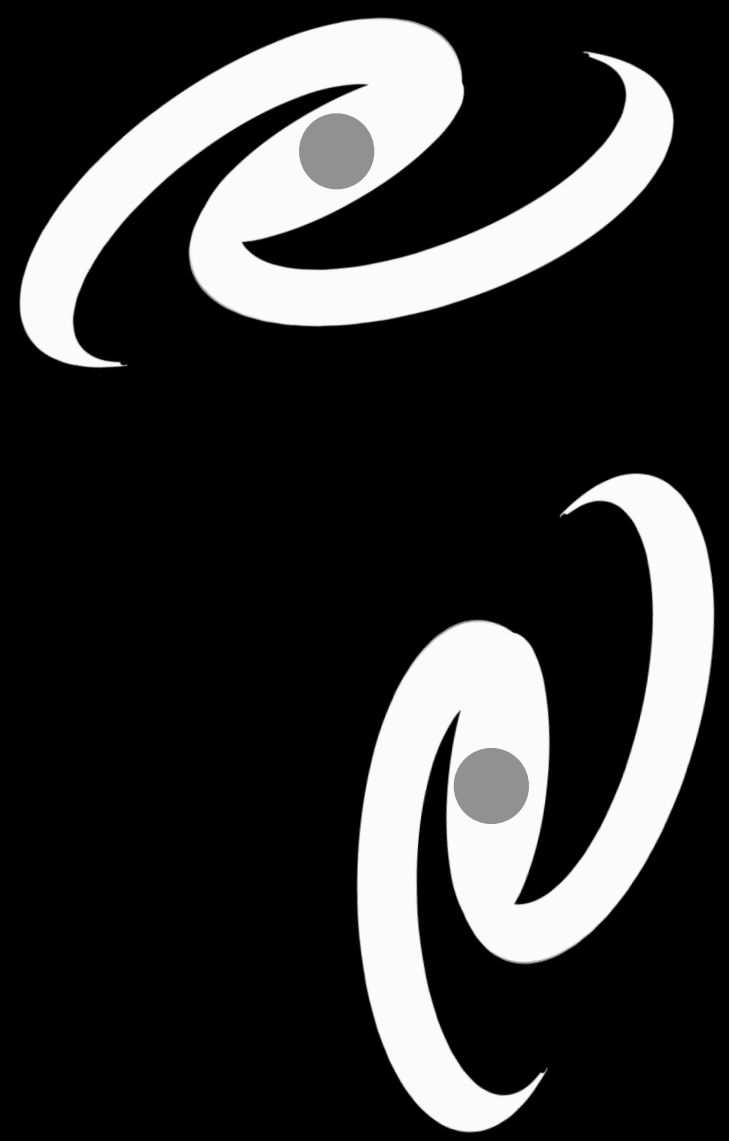
dynamical friction,  
stellar hardening  
dependent on host



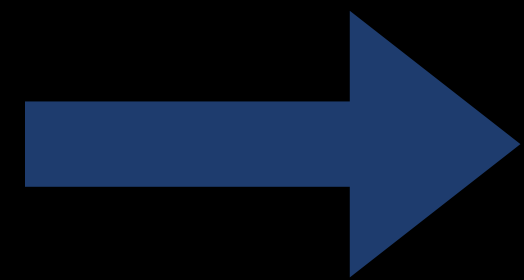
~milli-pc

stellar hardening  
dependent on host, GW  
emission

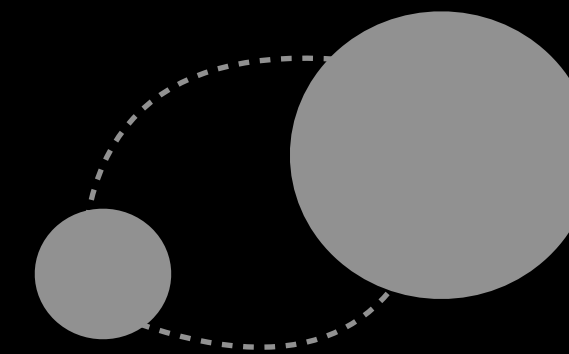
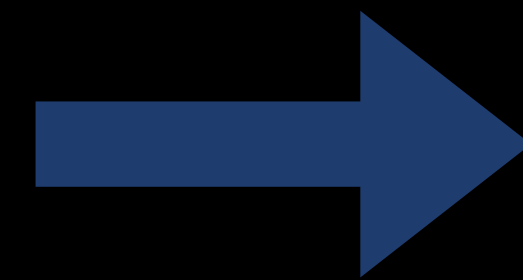
**Uncertain timescales due to issues like final pc problem**



~kpc



~pc



~milli-pc

NEED HIGH RESOLUTION N-BODY SIMULATIONS

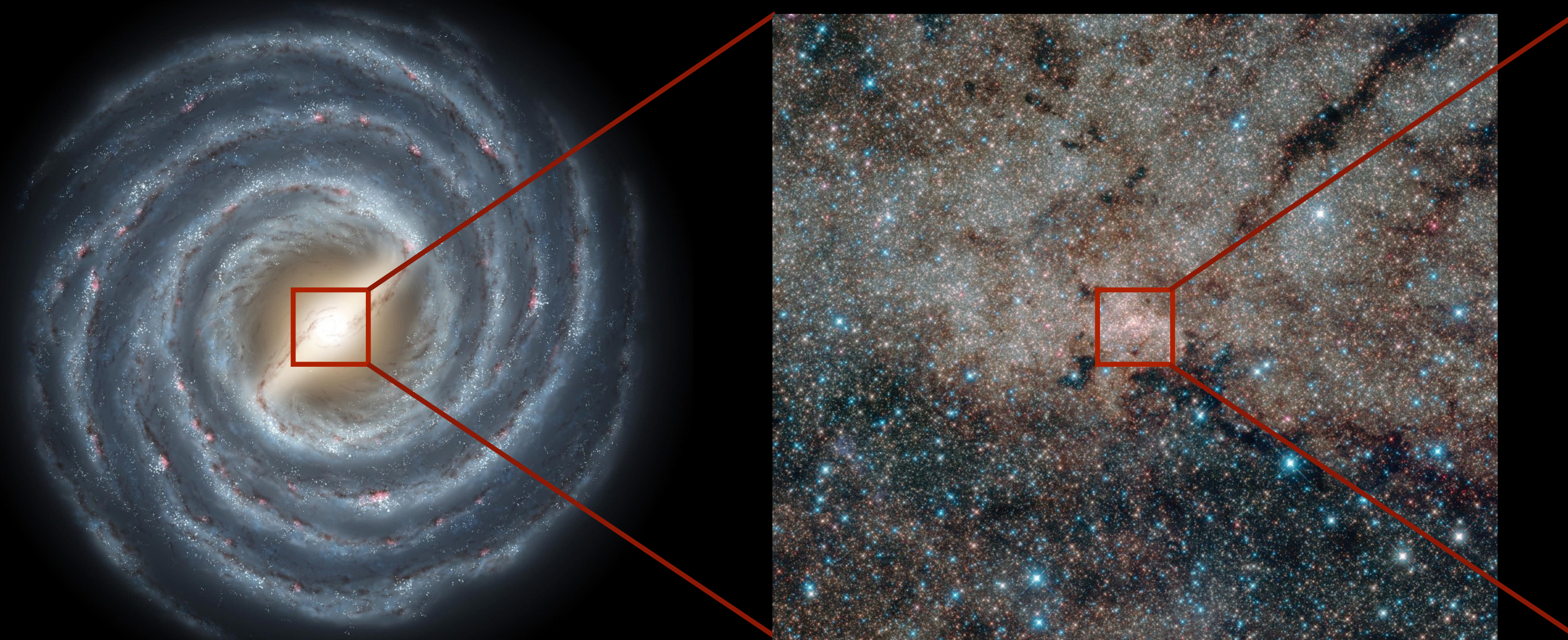
RESOLVED IN  
COSMOLOGICAL  
SIMULATIONS

UNRESOLVED IN  
COSMOLOGICAL  
SIMULATIONS

# NUCLEAR STAR CLUSTERS

90% at  $M_{\text{stellar}} = 10^9 M_{\odot}$

50% of Milky Way sized galaxies



~kilo-pc

~pc


~milli-pc

# MBH BINARIES IN NUCLEAR STAR CLUSTERS

- Ogiya+ (2020) showed that NSCs greatly accelerate transition to GW dominated phase
- Robust and works better for lower mass ratio binaries
- Motivated to study how realistic models of NSCs with mass spectrum affect dynamics



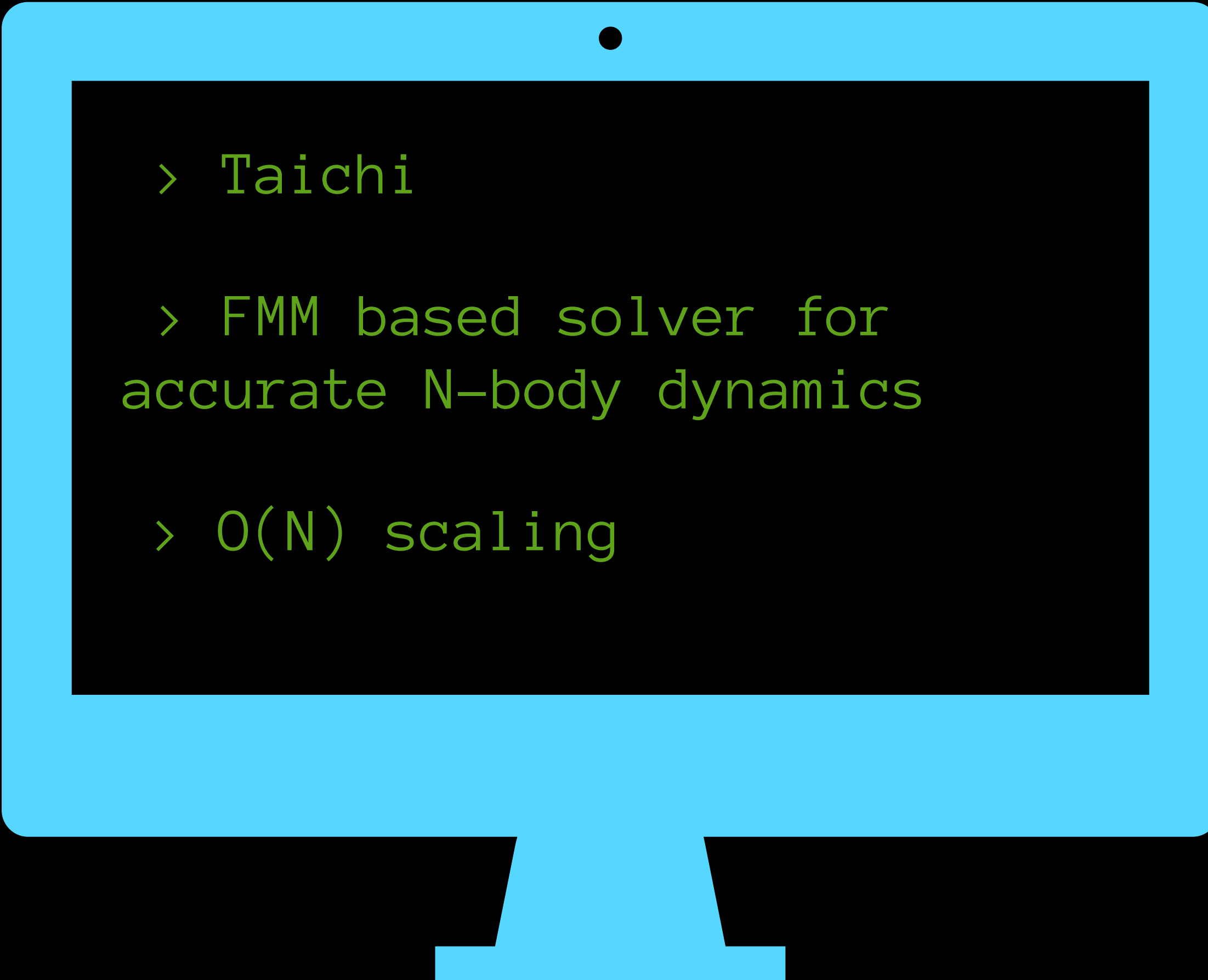
# SIMULATING PC SCALE DYNAMICS

High-resolution 

Can resolve three body scattering 

Accurate 

Fast 

- 
- > Taichi
  - > FMM based solver for accurate N-body dynamics
  - >  $O(N)$  scaling

Mukherjee+ (2021)

# MODELS

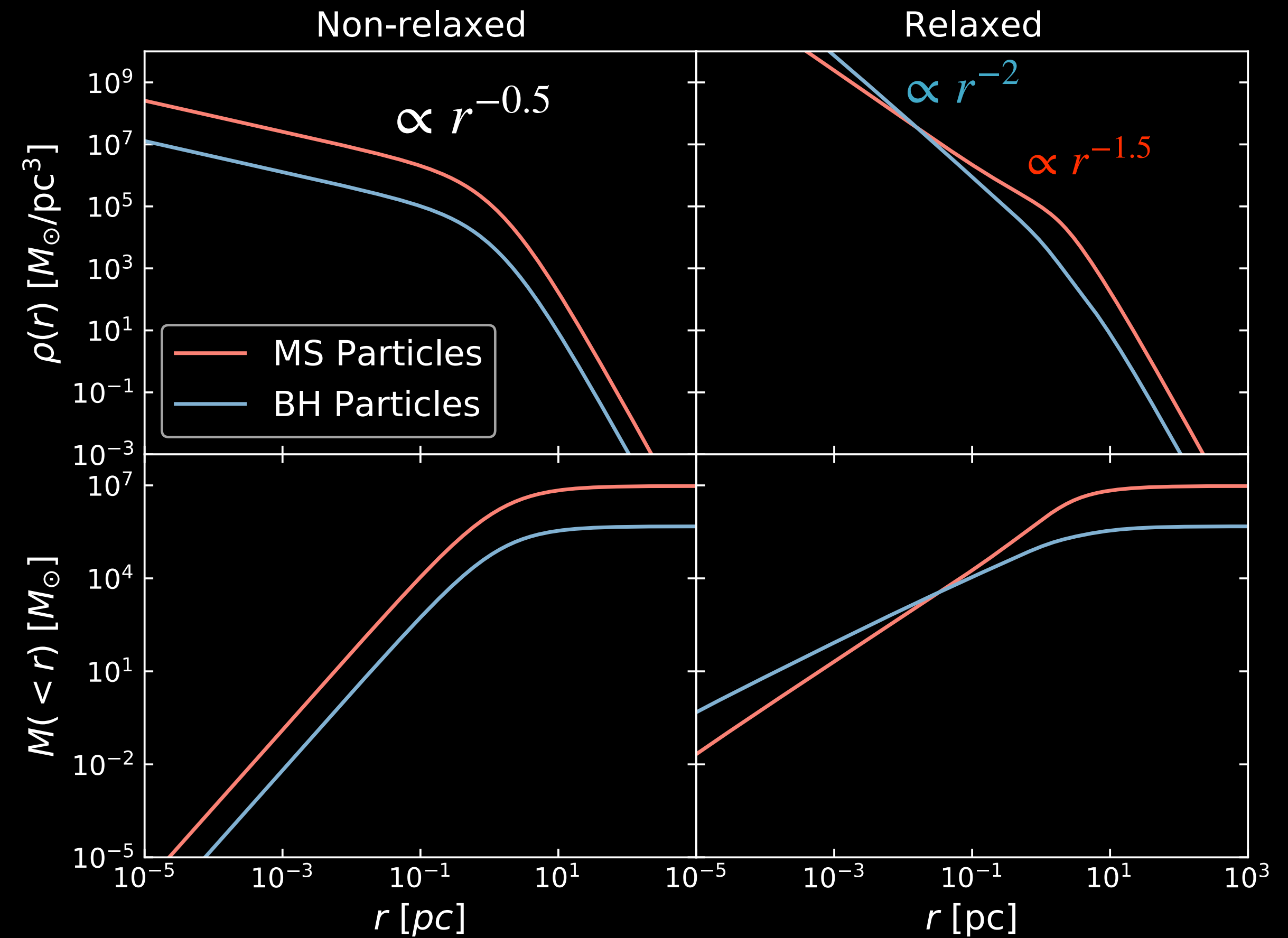
- Masses of MBHs in LISA band

$$M_{\text{primary}} = 10^6 M_{\odot} \quad q = 1.0, 0.1, 0.01$$

- Realistic NSCs with a two-component mass spectrum

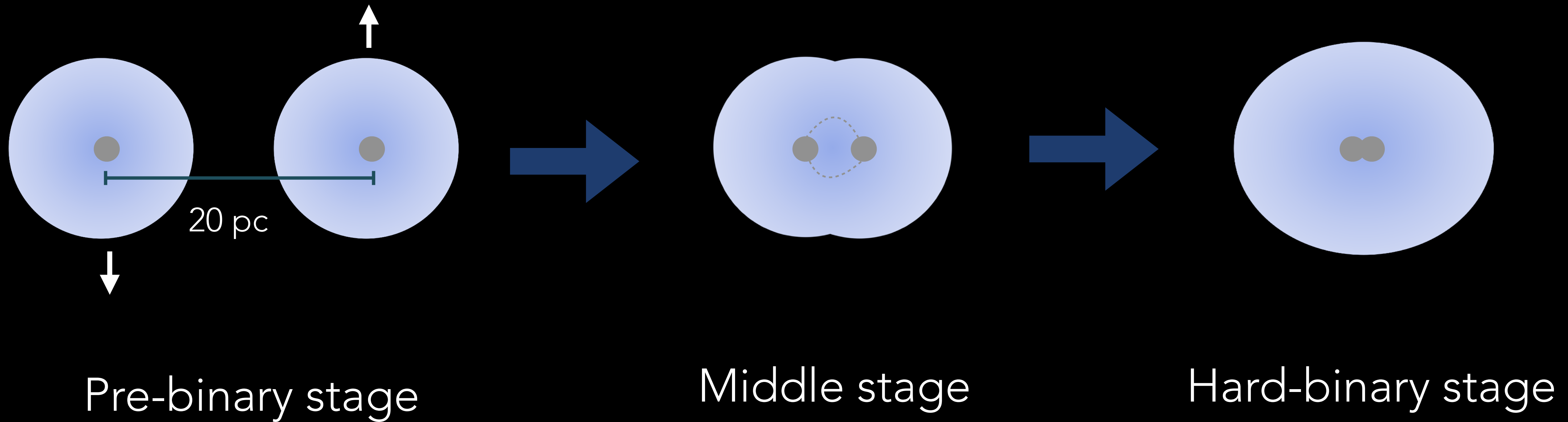
$$M_{\text{NSC}} = 10^7 M_{\odot} \quad N_{\text{MS}} : N_{\text{BH}} = 1 : 0.005$$

- Collisional relaxation: segregated vs. non-segregated



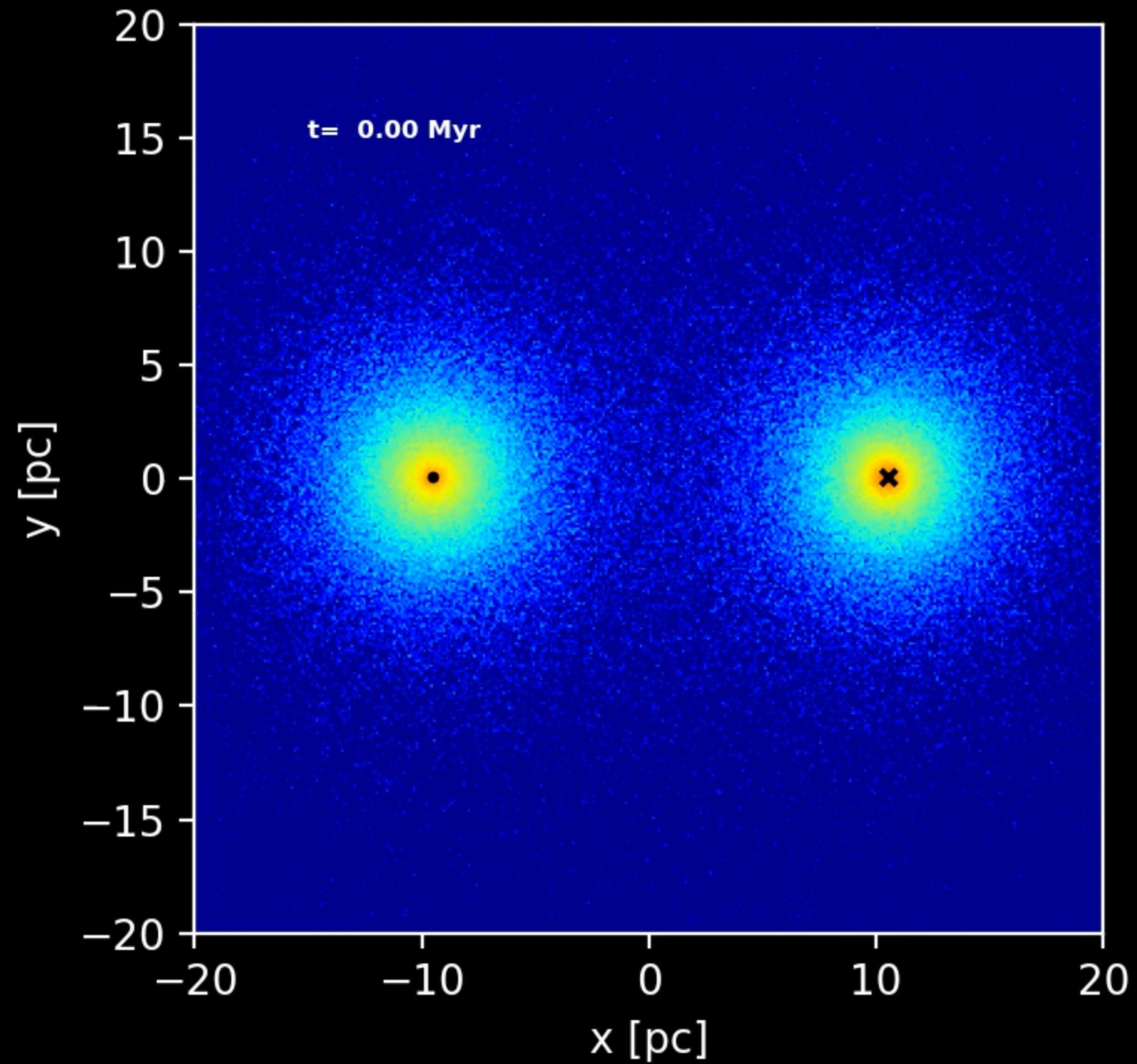
Mukherjee+ (2022)

# MODELS

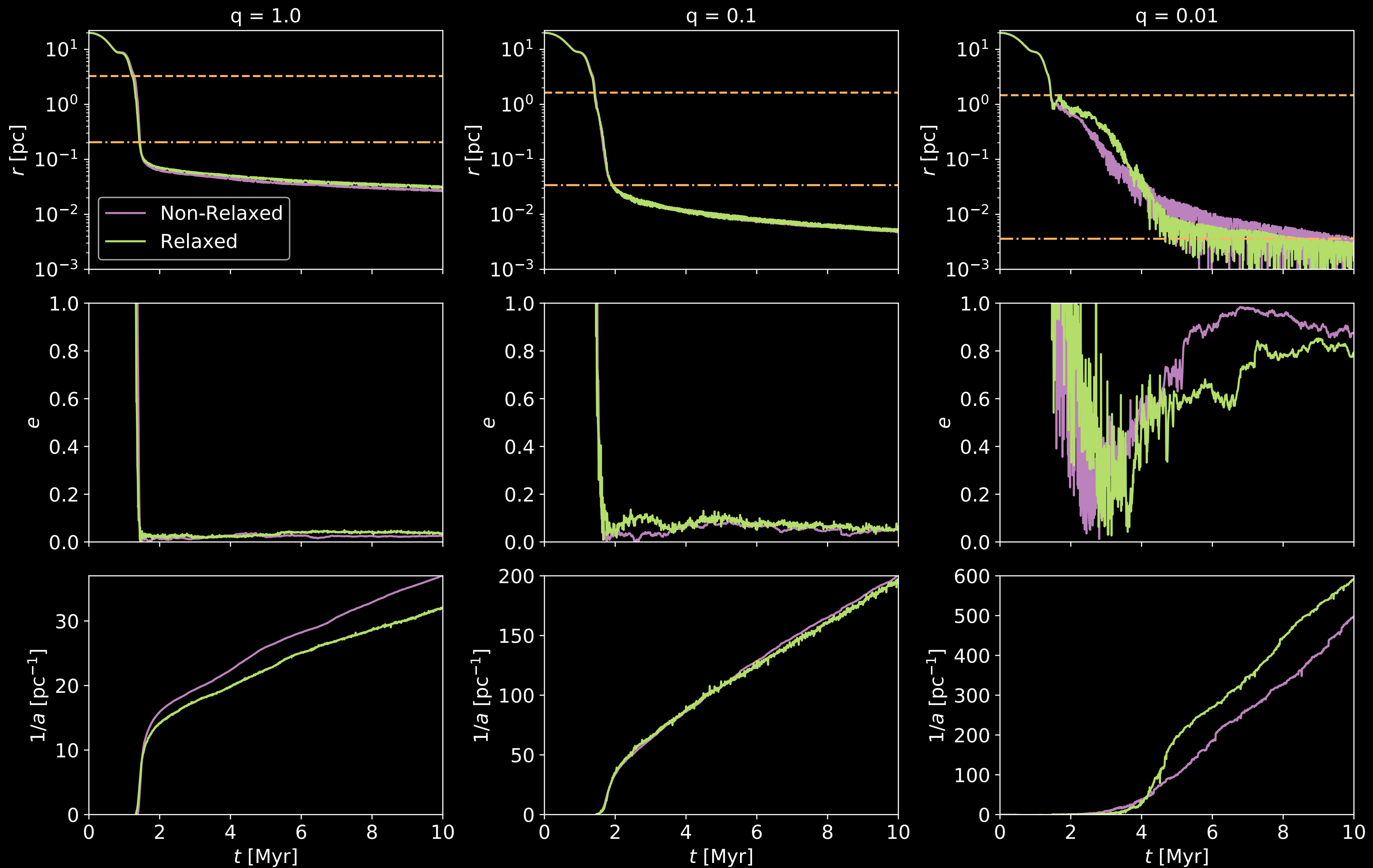


Begelman+ (1980), Merritt (2013), Ogiya+ (2020)

# VISUALIZING THE MERGER PROCESS



# EVOLUTION OF ORBITAL PARAMETERS

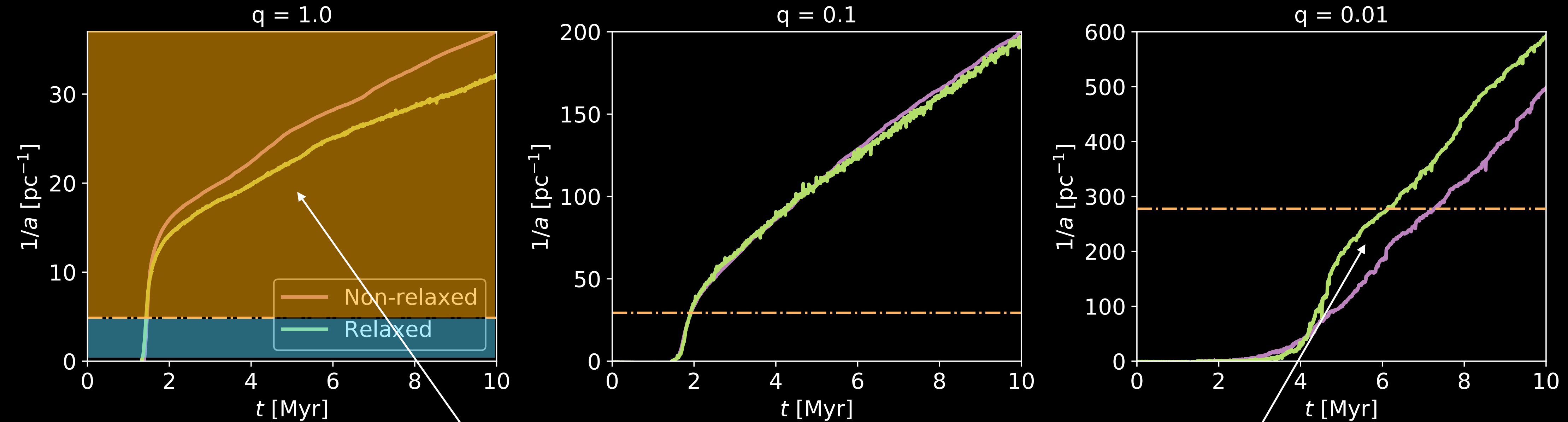


# EVOLUTION OF MBH BINARY

$$E_{\text{binary}} = -\frac{GM_1M_2}{2a}$$

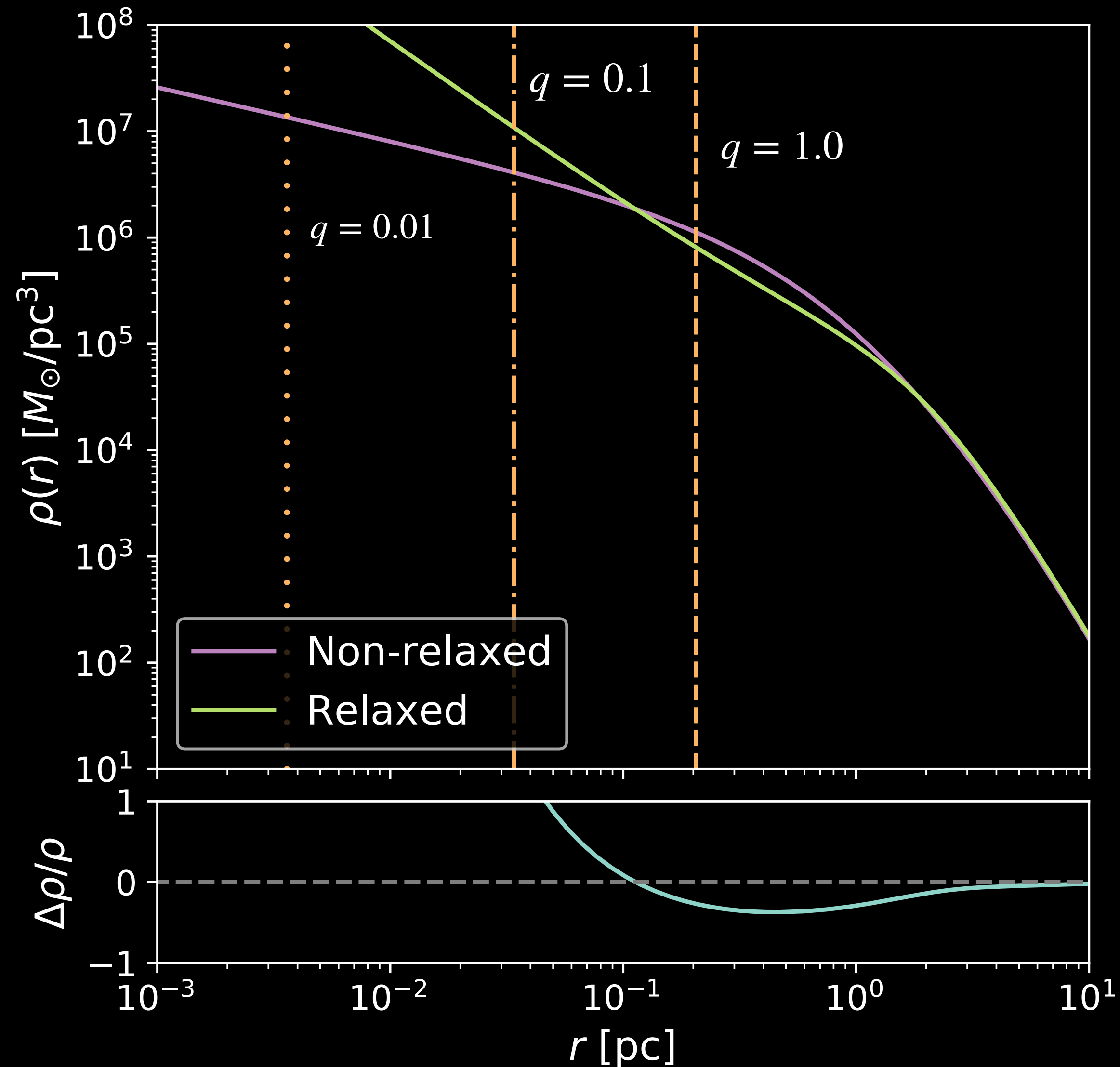
HARD BINARY PHASE

PRE-HARD BINARY PHASE



Why does the trend change over the mass ratio?

# EVOLUTION OF THE MBH BINARY

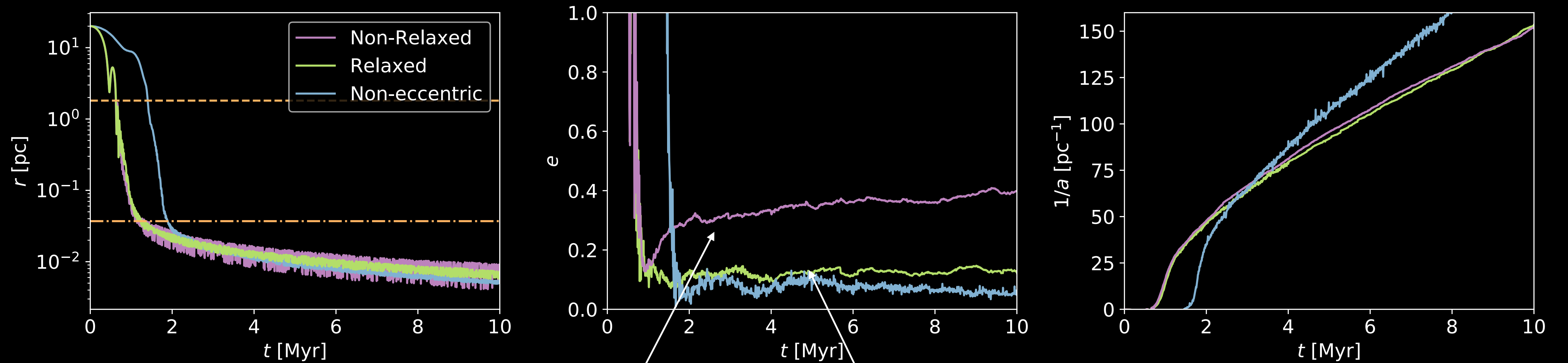


$$\left. \frac{dE}{dt} \right|_{\text{df}} \approx -4.4 \frac{G^2 M_2^2 \rho(r) \ln(\Lambda)}{\sigma}$$

$$\left. \frac{dE}{dt} \right|_{\text{s}} = - \frac{H(a)}{2q} \frac{G^2 M_2^2 \rho(r)}{\sigma}$$

Relaxed models have a lower density than non-relaxed models until a certain radius!

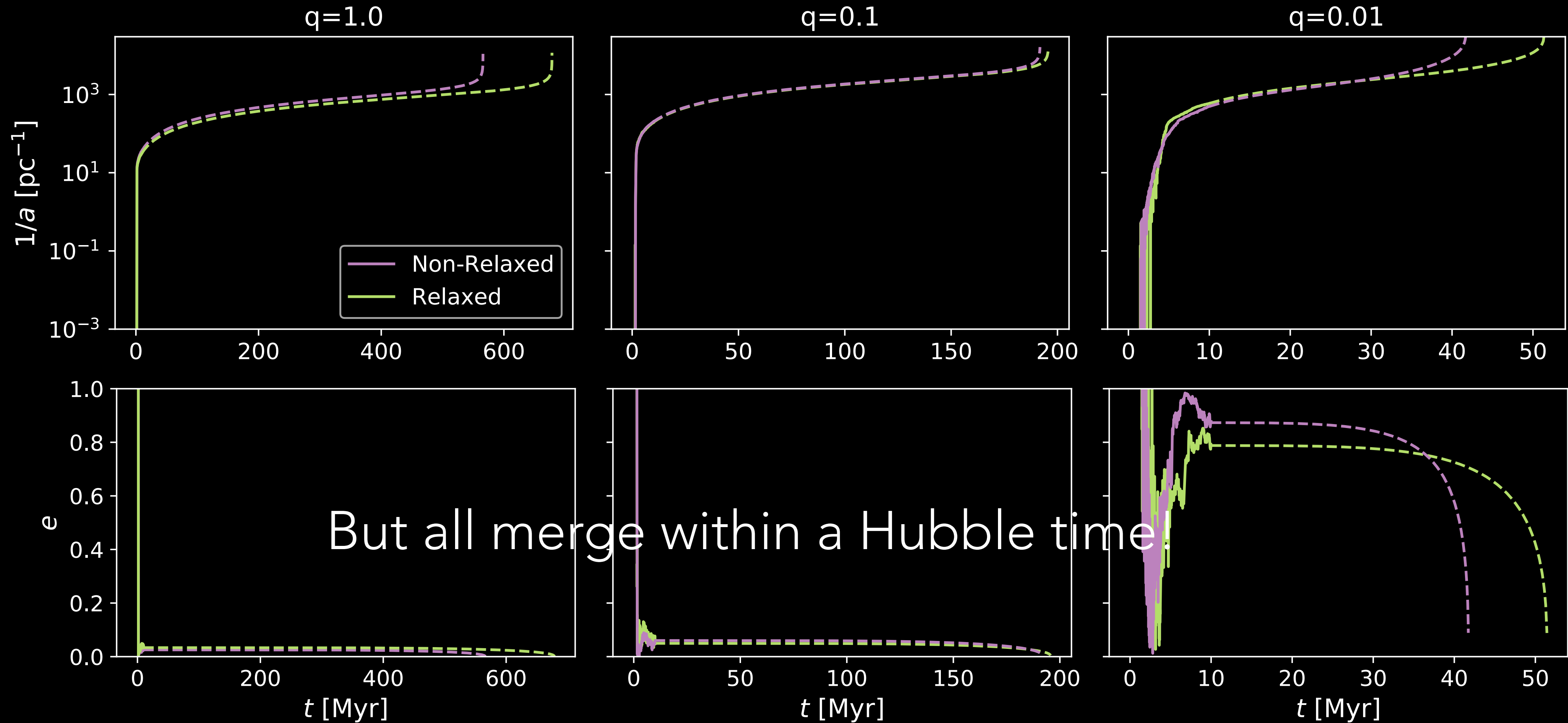
# ECCENTRIC ORBITAL PARAMETERS



Non-relaxed models demonstrate higher eccentricities

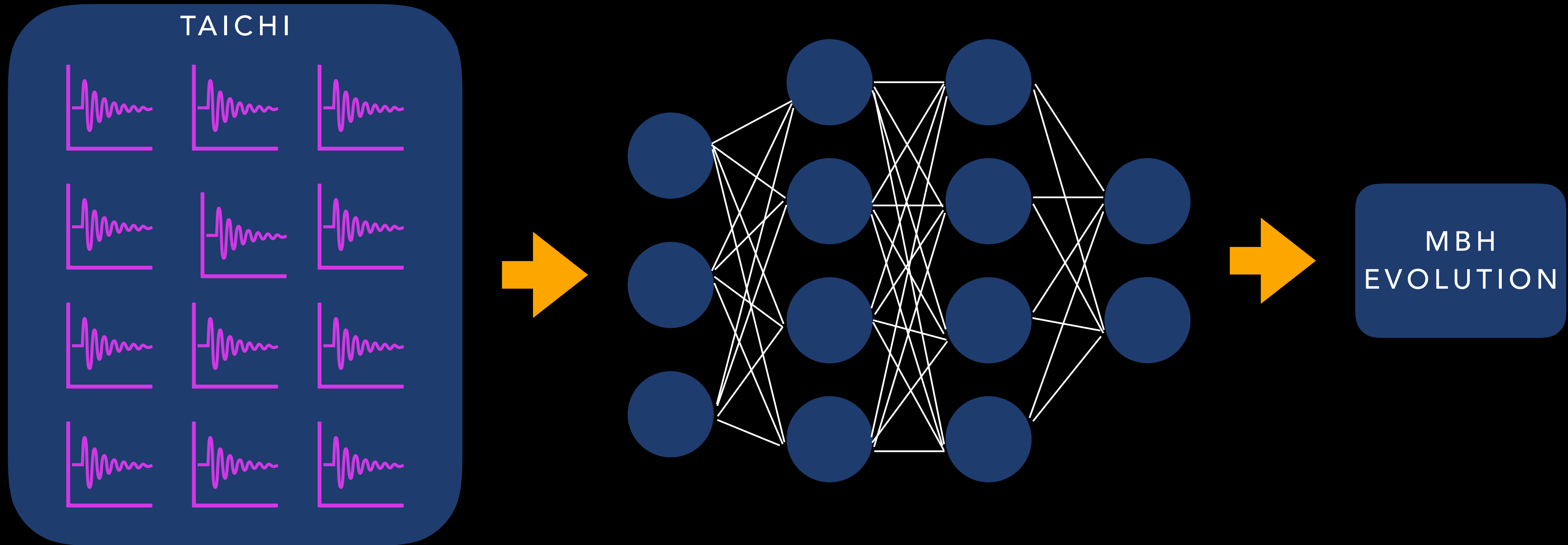


# GRAVITATIONAL WAVE TIMESCALES



Non-relaxed models merge faster in all cases

# IMPROVING COSMOLOGICAL SIMULATIONS



# CONCLUSIONS

- Able to ascertain the differences in evolution of MBHs in relaxed and non-relaxed NSCs
- Showed that NSCs are extremely robust and efficient at merging MBHs, especially lower mass MBHs
- Presented Taichi as an effective N-body code to solve problems of this scale
- Discussed potential improvements to future cosmological simulations