



UNIVERSITÉ
DE GENÈVE



SWISS NATIONAL SCIENCE FOUNDATION

LOUIS LEGRAND

Julien Carron

Legrand and Carron 2021

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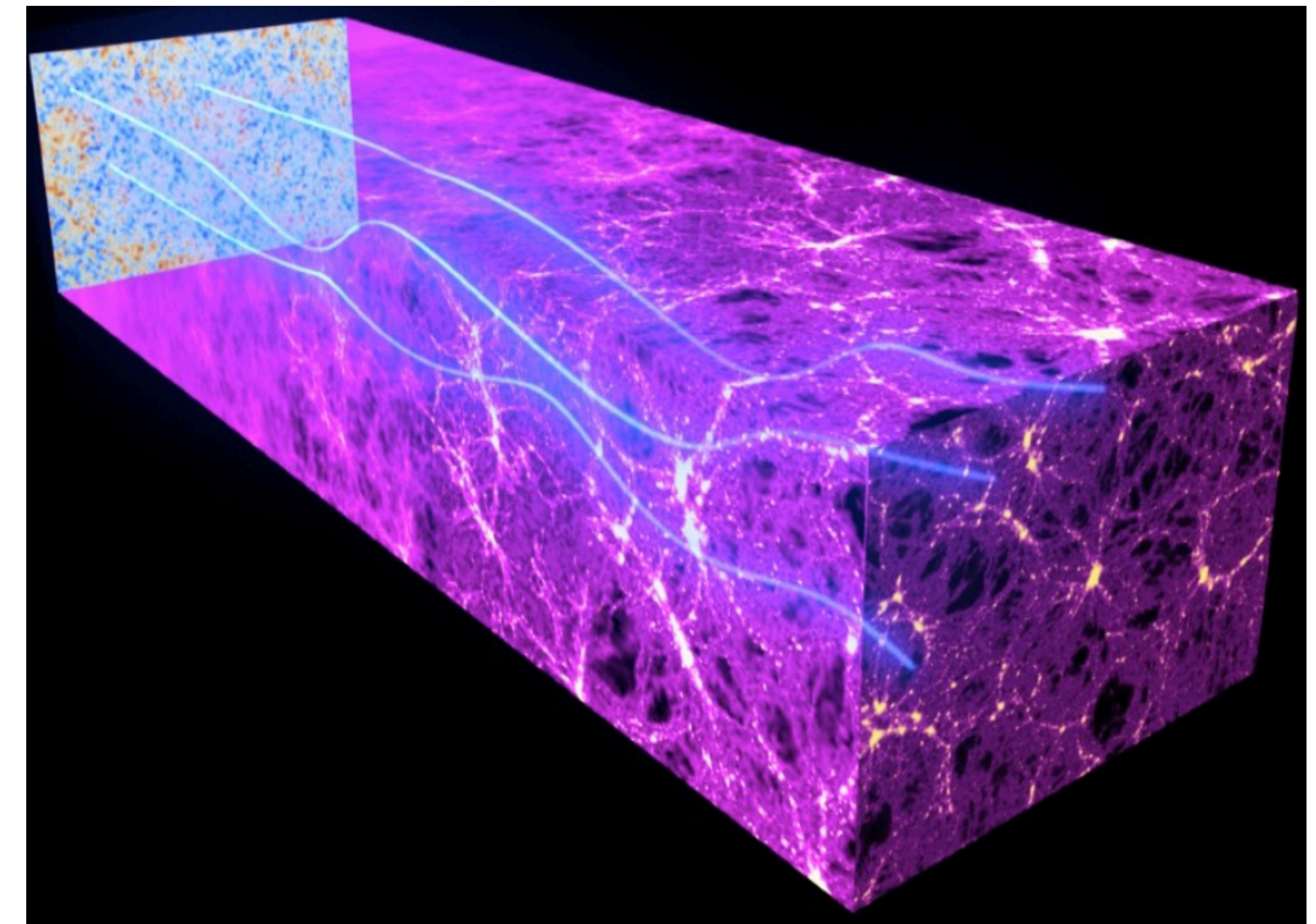
CMB LENSING WITH NEXT GENERATION SURVEYS

CMB GRAVITATIONAL LENSING

- ▶ CMB is an extended light source at $z=1100$
- ▶ CMB photons are lensed by the large scale structures created by gravitational evolution of matter

$$\alpha = \vec{\nabla} \phi$$

$$\phi(\mathbf{n}) = -2 \int_0^{\chi_*} d\chi \frac{\chi_* - \chi}{\chi_* \chi} \Psi(\chi \mathbf{n}; \eta_0 - \chi)$$

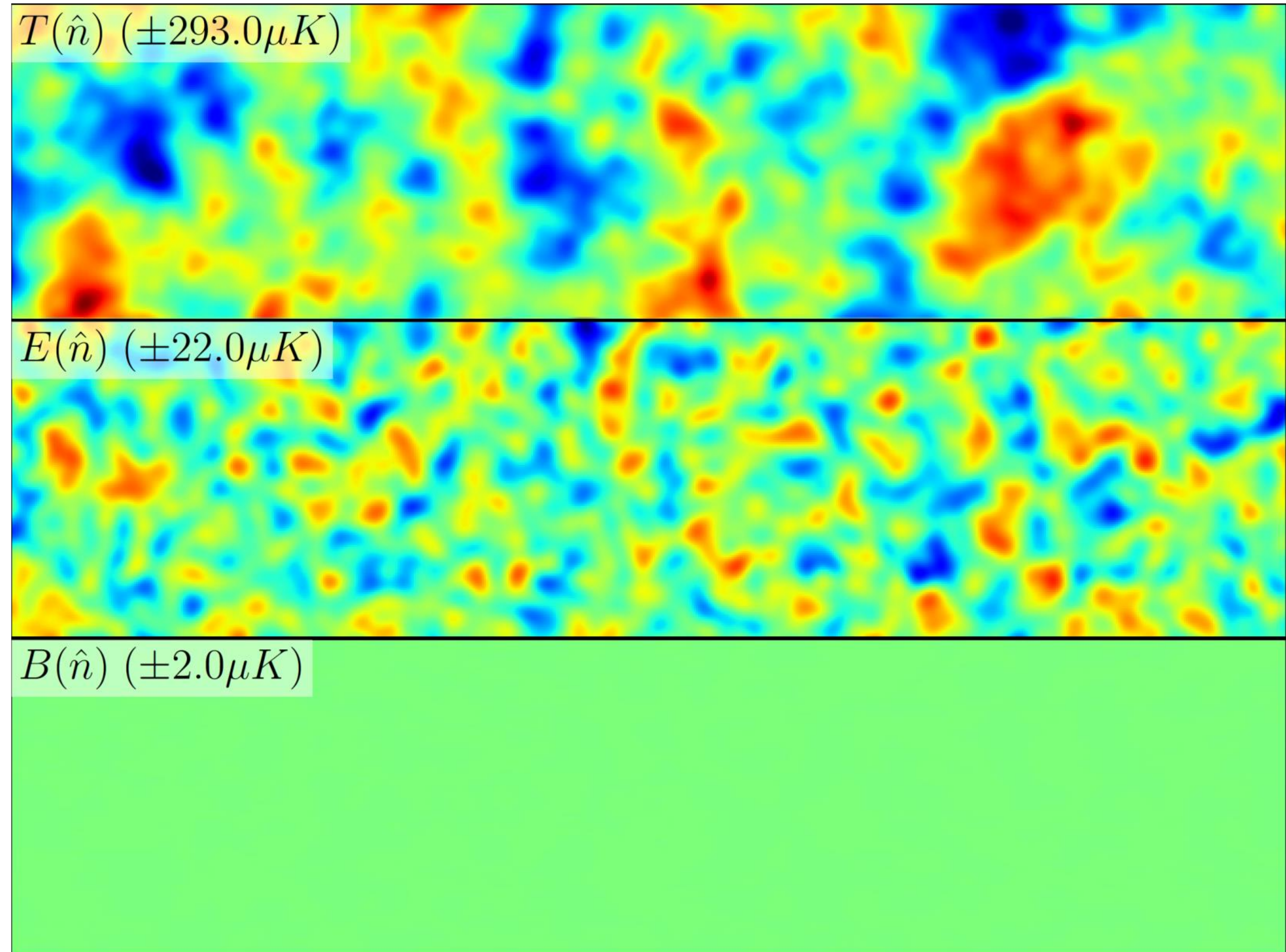


CMB LENSING

- ▶ Lensing acts as a remapping of the primordial CMB fields

$$X^{\text{len}}(\mathbf{n}) = X^{\text{unl}}(\mathbf{n} + \boldsymbol{\alpha}(\mathbf{n}))$$

- ▶ It creates statistical anisotropies and correlation between different scales

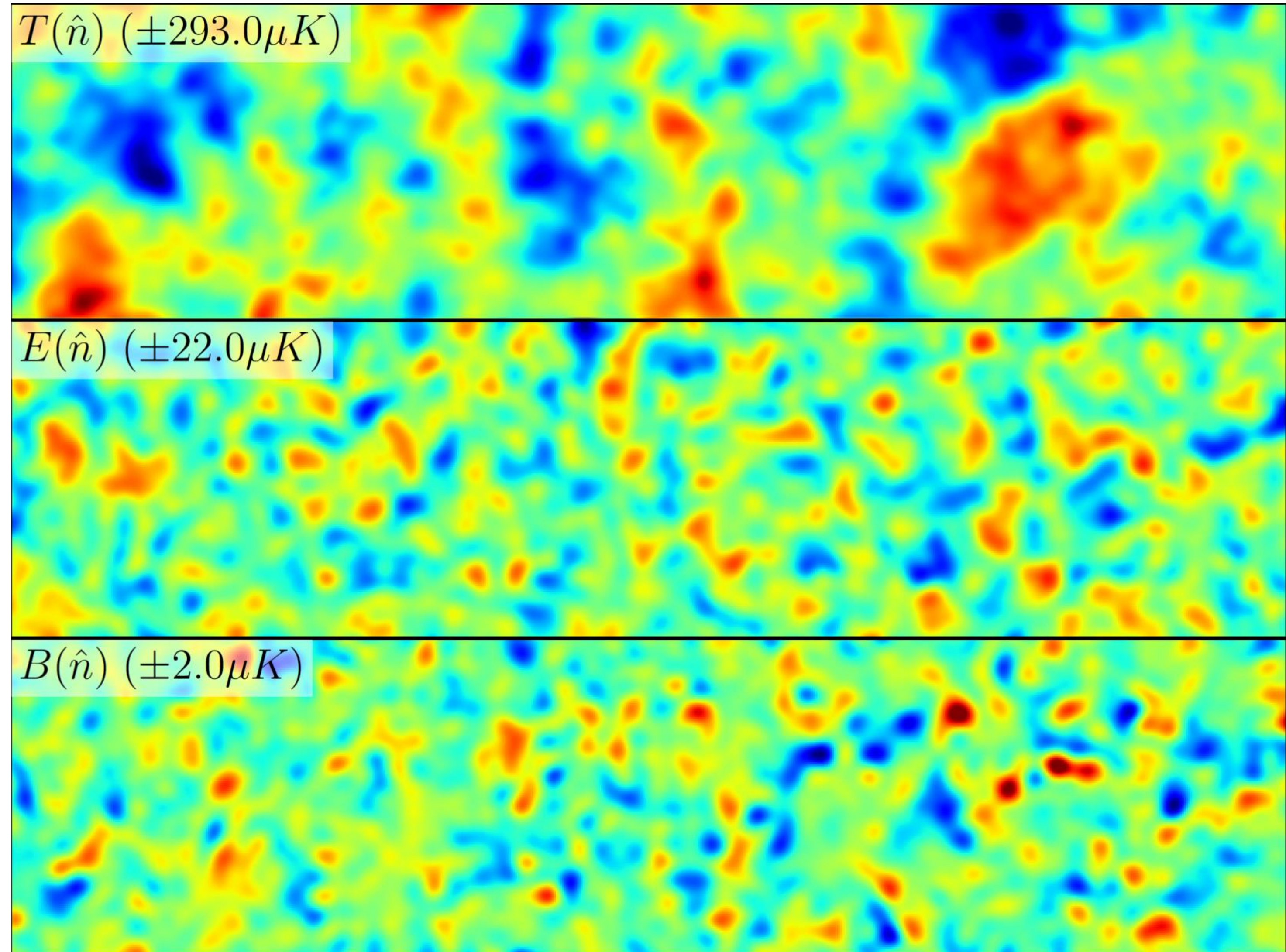


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HOW CAN WE MEASURE THE CMB LENSING POTENTIAL?

QUADRATIC ESTIMATOR (QE)

- ▶ Lensing creates correlations between different multipole moments

$$\langle X^{\text{len}}(\mathbf{l}) Y^{\text{len}*}(\mathbf{l}') \rangle_{\substack{\text{fixed lensed} \\ \mathbf{l} \neq \mathbf{l}', L = \mathbf{l} + \mathbf{l}'}} = f_{XY}(\mathbf{l}, \mathbf{l}') \phi(\mathbf{L})$$

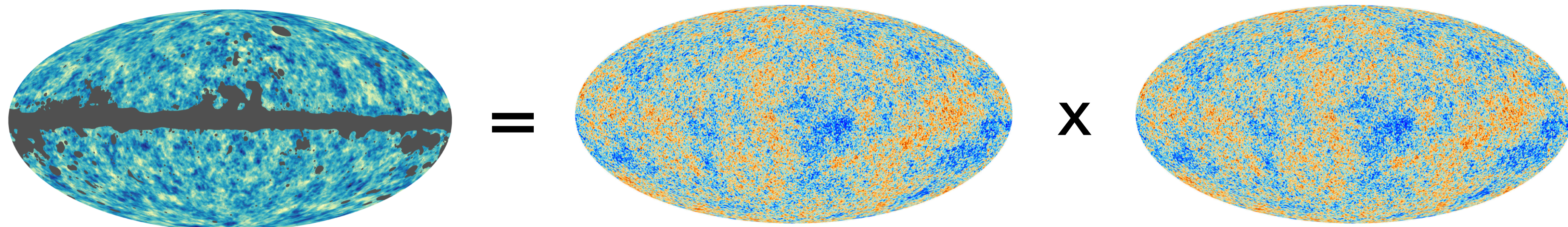
Lensing induced correlations

- ▶ The QE combines scales of two CMB fields (Hu & Okamoto 2002)

$$\hat{\phi}(\mathbf{L}) = \frac{1}{R_L^{XY}} \int \frac{d^2\mathbf{l}}{2\pi} f^{XY}(\mathbf{l}, \mathbf{L}) \bar{X}(\mathbf{l}) \bar{Y}^*(\mathbf{l} - \mathbf{L})$$

Normalisation (response of the estimator)

Inverse variance filtered CMB fields



NOISY RECONSTRUCTION

- ▶ The power spectrum of the estimated lensing potential is a 4 point functions of the maps

$$C_L^{\hat{\phi}\hat{\phi}} = \text{[Map 1]} \times \text{[Map 2]} = \text{[Map 3]} \times \text{[Map 4]} \times \text{[Map 5]} \times \text{[Map 6]}$$

- ▶ Chance correlations between different scales can mimic the lensing effect

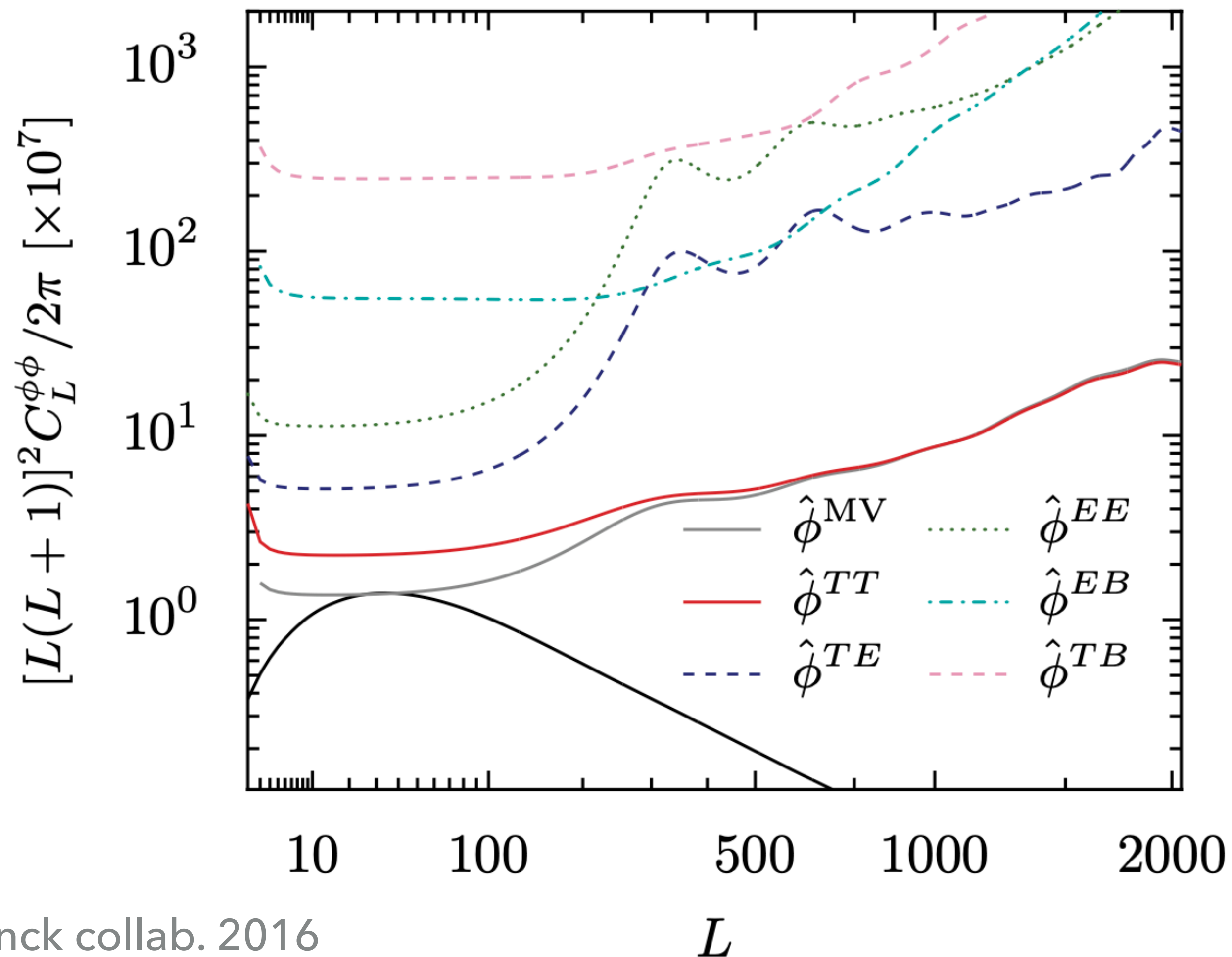
$$C_L^{\hat{\phi}\hat{\phi}} = C_L^{\phi\phi} + N_L^0 + N_L^1 + \dots$$

The signal we want

Disconnected (gaussian) contractions of the lensed CMB fields

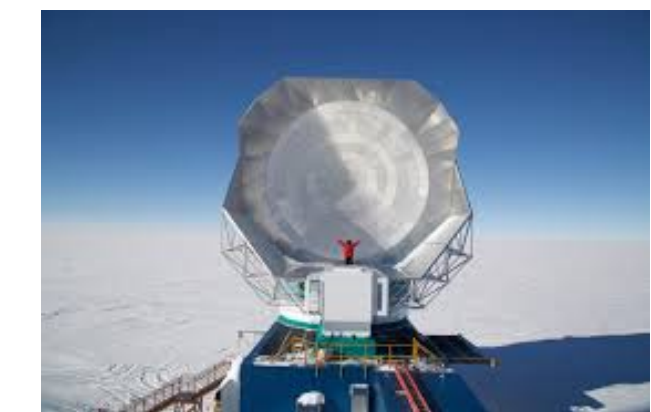
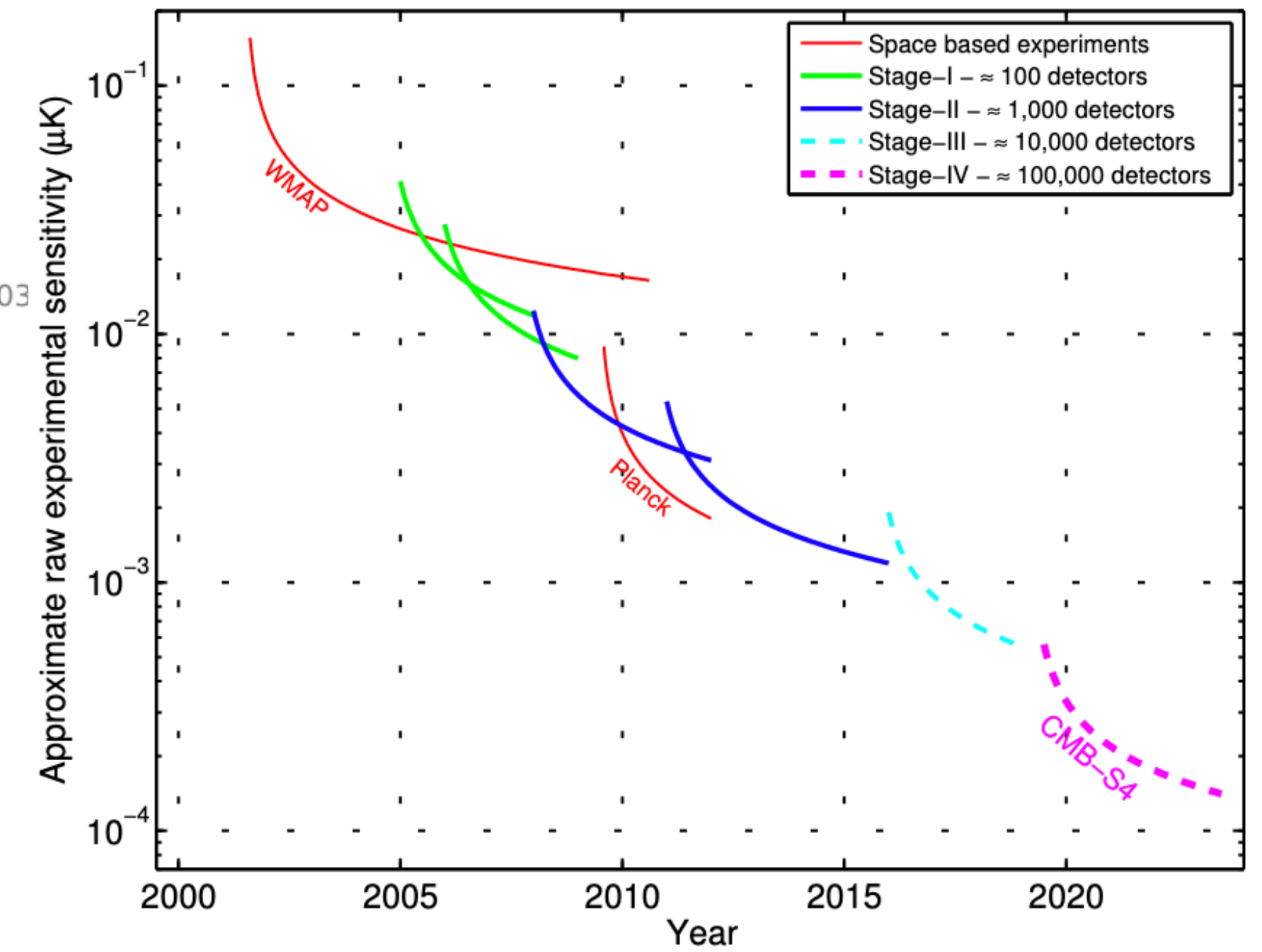
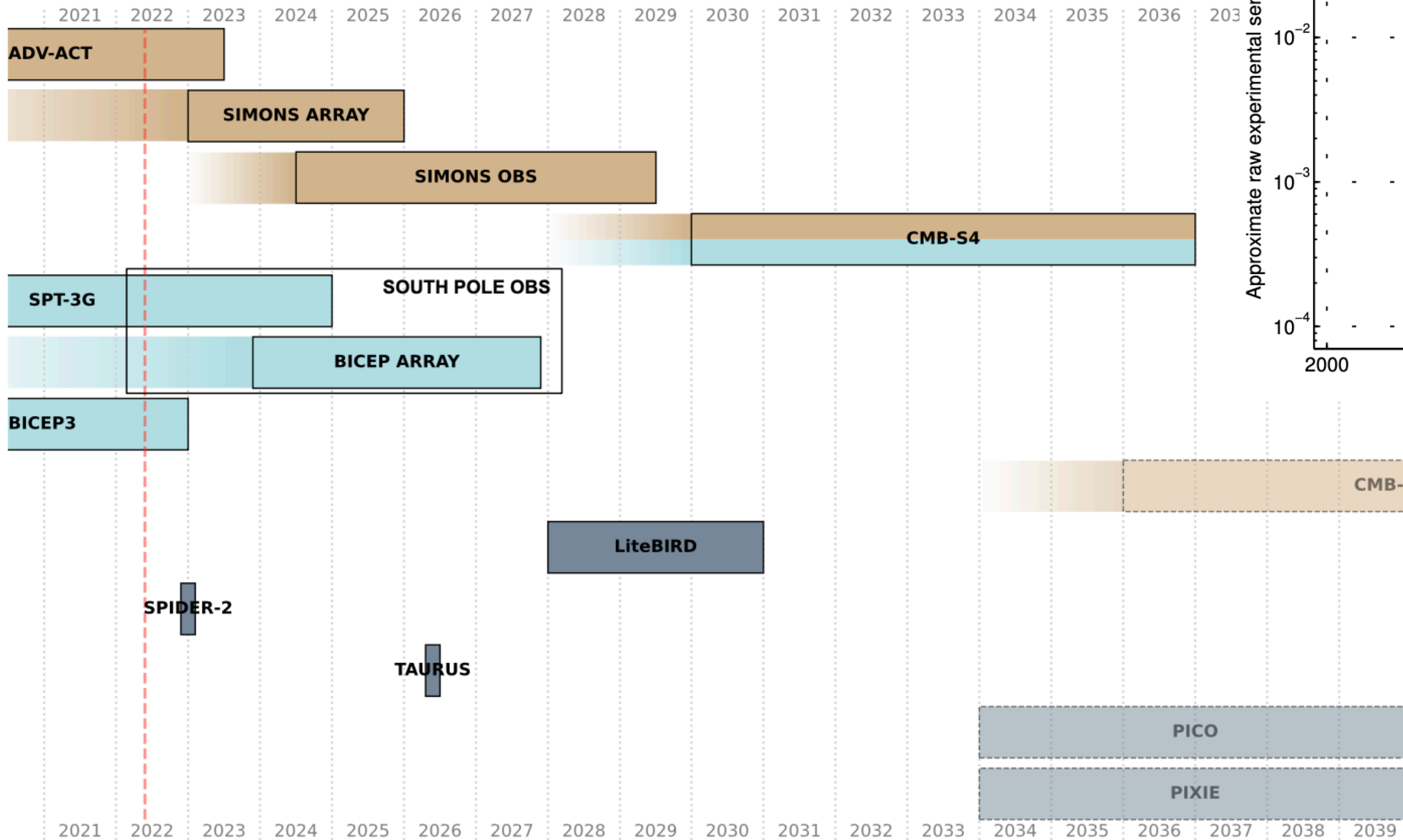
Non gaussian secondary contractions created by lensing (proportional to $C^{\phi\phi}$)

NOISY RECONSTRUCTION



- ▶ Planck lensing power spectrum is dominated by the N0 bias at all scales
- ▶ Combining all pairs of maps into a minimum variance estimator
- ▶ TT estimator is dominating in Planck

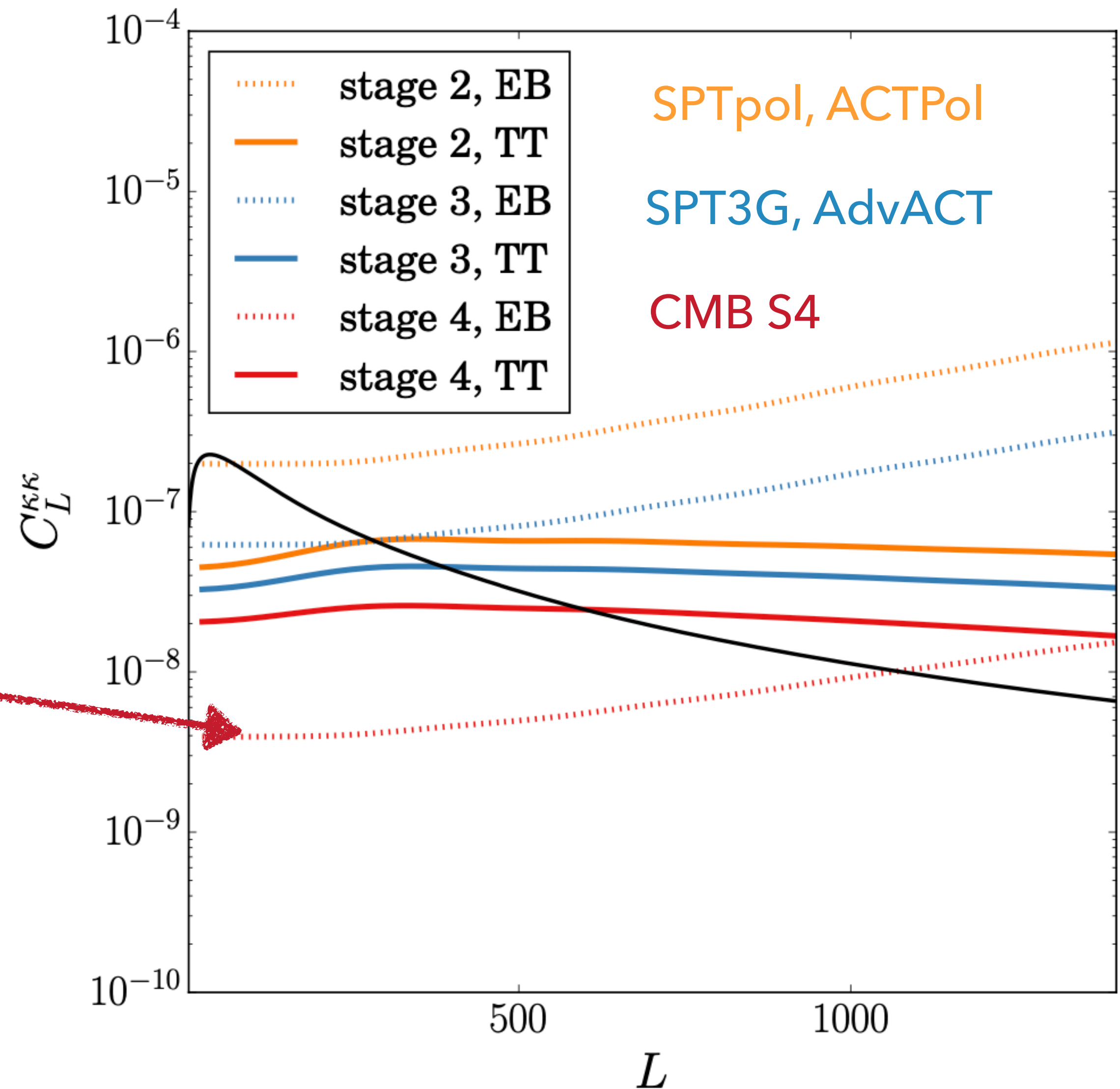
NEXT GENERATION SURVEYS



Chang et al 2022

NEXT GENERATION CMB SURVEYS

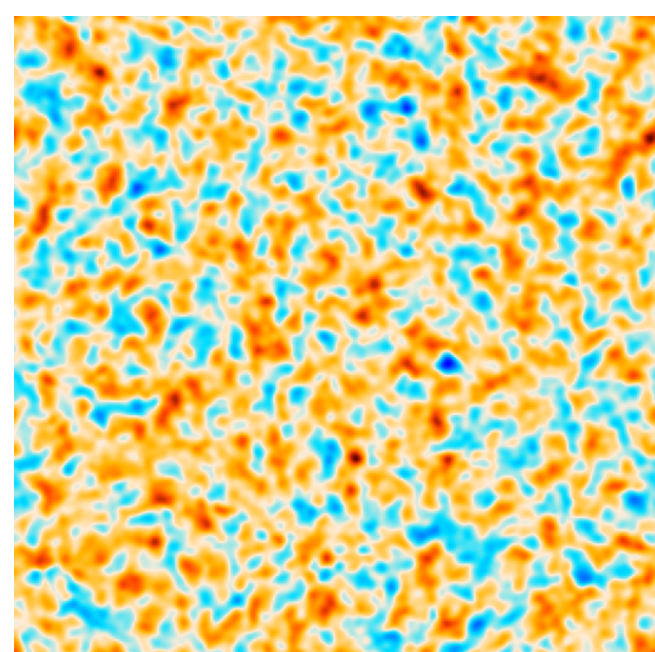
EB (polarisation) estimator
will be dominant for CMB S4



MORE OPTIMAL ESTIMATORS

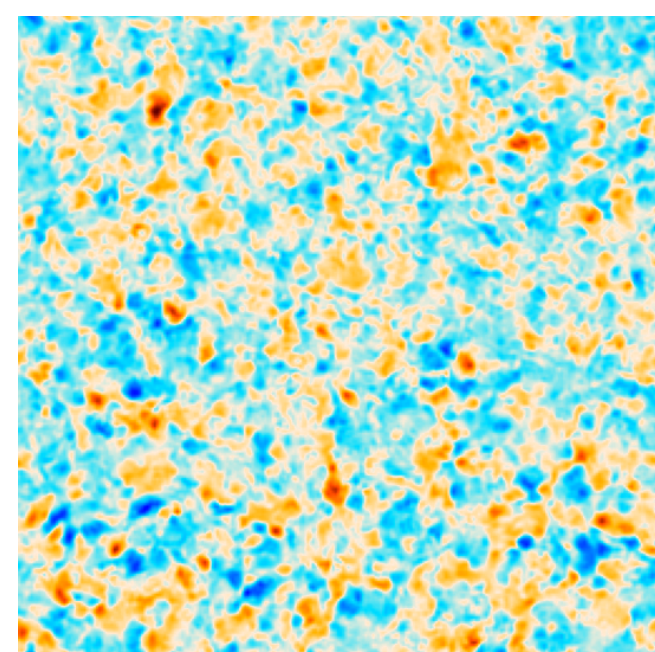
- ▶ Neglecting primordial B modes, one could reconstruct perfectly the lensing field

Lensed E



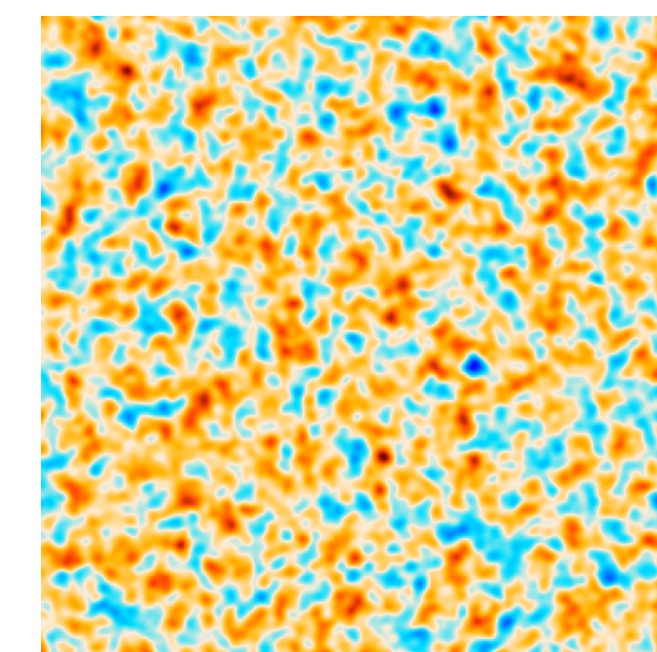
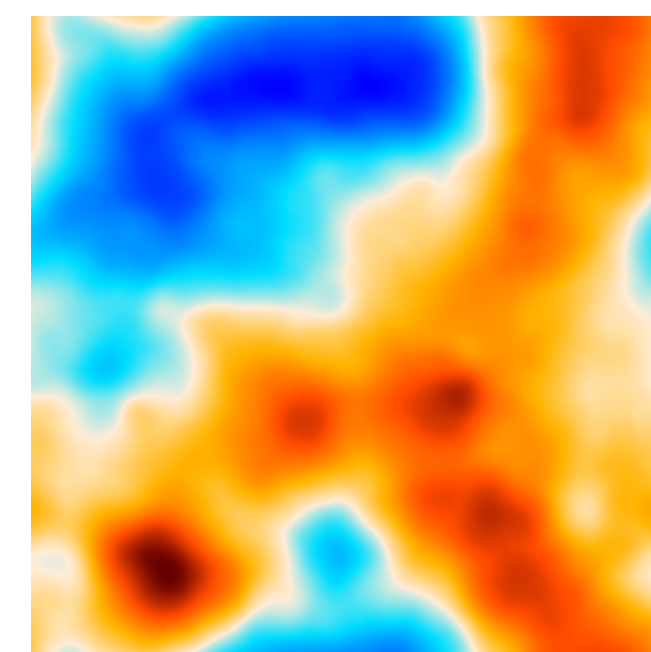
+

Lensed B



No primordial B
 \Leftrightarrow

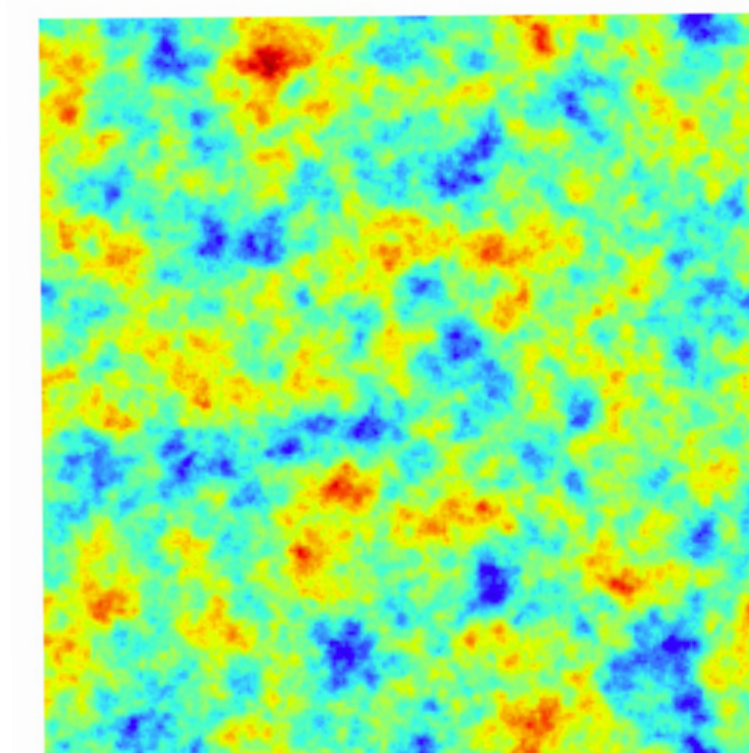
Lensing potential + Unlensed E



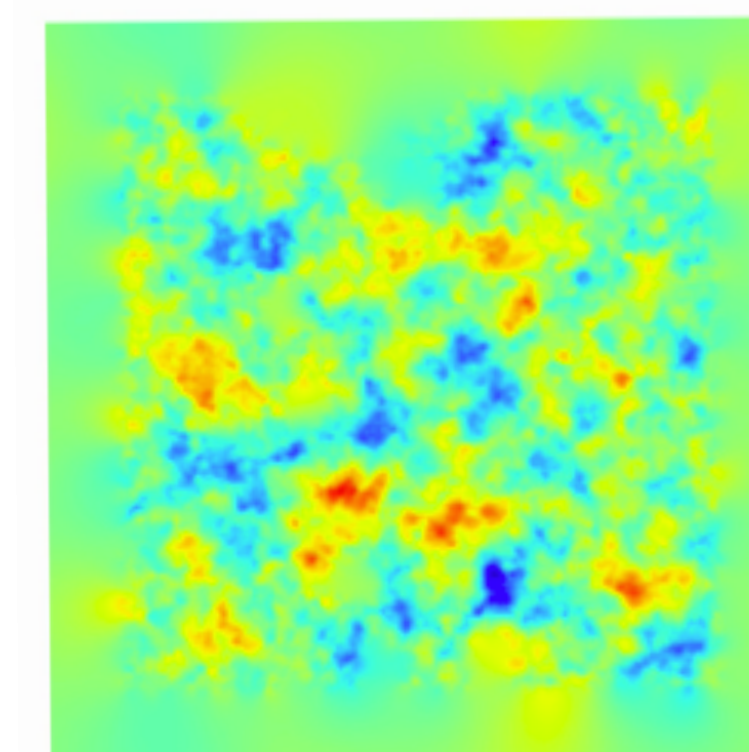
- ▶ Likelihood based approach, first introduced in Hirata & Seljak 2003 $P(\phi | \text{data})$
- ▶ How can we find the maximum of this likelihood ?
 - ▶ Sampling-based approach -> Millea et al 2020
 - ▶ Iterative approach -> Carron & Lewis 2017

ITERATIVE APPROACH

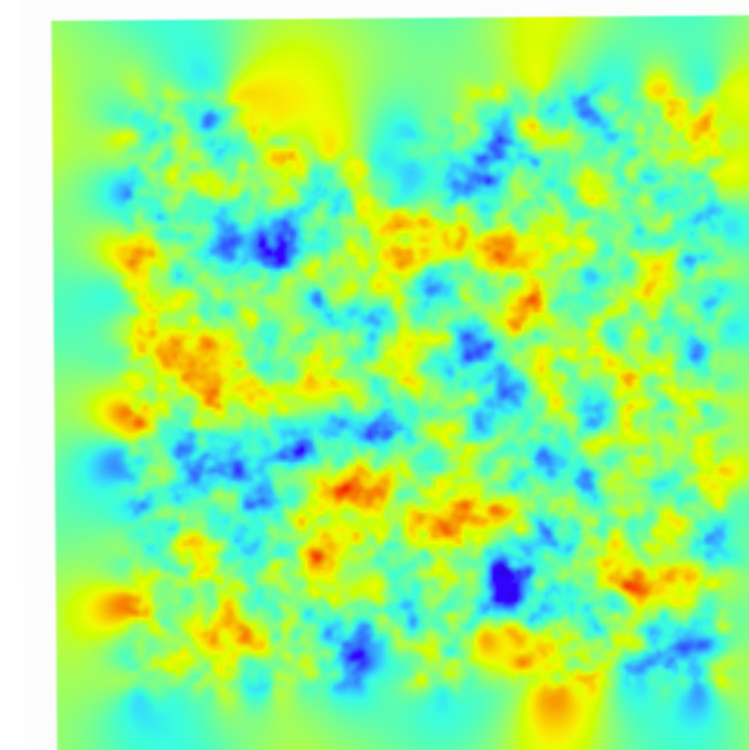
- ▶ Newton-Raphson iterations on the likelihood
- ▶ At each step we get an estimate of the maximum a posteriori lensing field, obtained with a QE
- ▶ In practice at each step:
 - ▶ delens the data using the deflection estimate
 - ▶ apply a quadratic estimator on the resulting maps
 - ▶ start again until convergence
- ▶ Advantage: fast and based on a well known tool, the quadratic estimator



Input ϕ



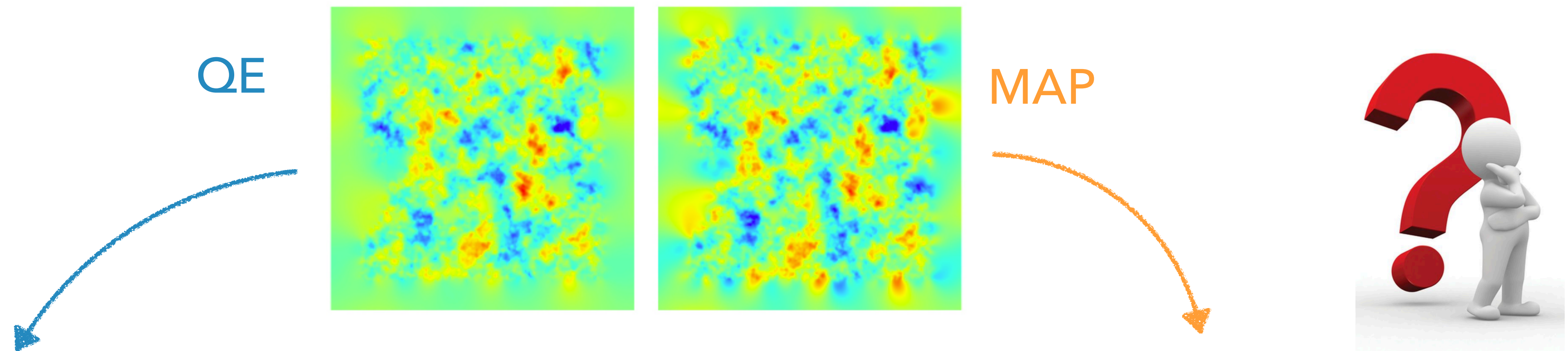
QE



MAP

OPTIMAL LENSING POWER SPECTRUM ESTIMATION

- ▶ Problem: cannot track analytically the 4 point function of the lensing power spectrum
- ▶ How do we debias the spectrum obtained from the iterative lensing reconstruction ?



$$C_L^{\hat{\phi}\hat{\phi}} = C_L^{\phi\phi} + N_L^0 + N_L^1 + \dots$$

$$C_L^{\hat{\phi}\hat{\phi}} = C_L^{\phi\phi} + N_L^{0,\text{MAP}} + N_L^{1,\text{MAP}} + \dots$$

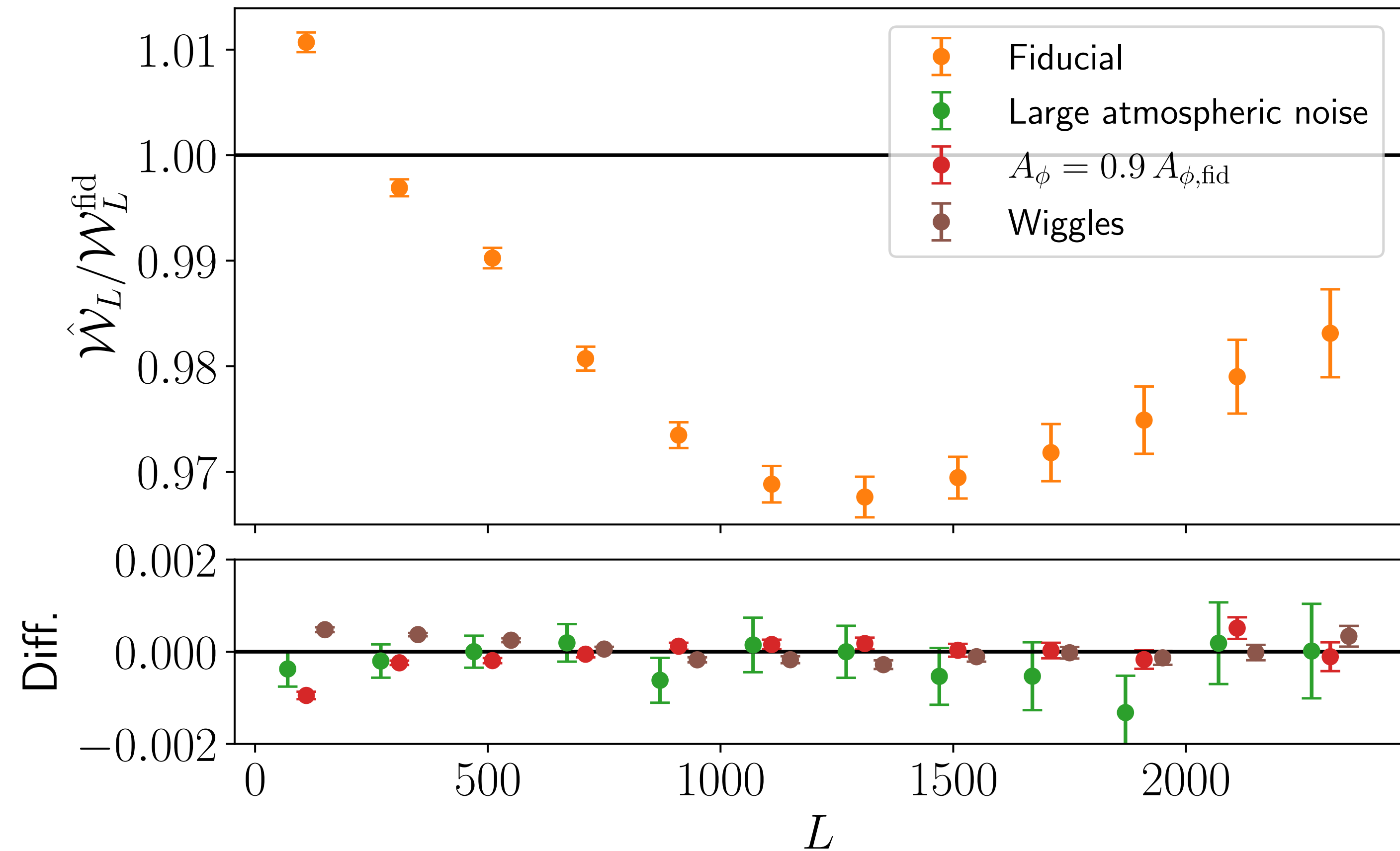
NORMALISATION

$$\hat{\phi}(\mathbf{L}) = \frac{1}{R_L^{XY}} \int \frac{d^2\mathbf{l}}{2\pi} f^{XY}(\mathbf{l}, \mathbf{L}) \bar{X}(\mathbf{l}) \bar{Y}^*(\mathbf{l} - \mathbf{L})$$

- ▶ For the MAP we assumed it is a Wiener filter

$$W_L = \frac{C_L^{\phi\phi}}{C_L^{\phi\phi} + N_L^0}$$

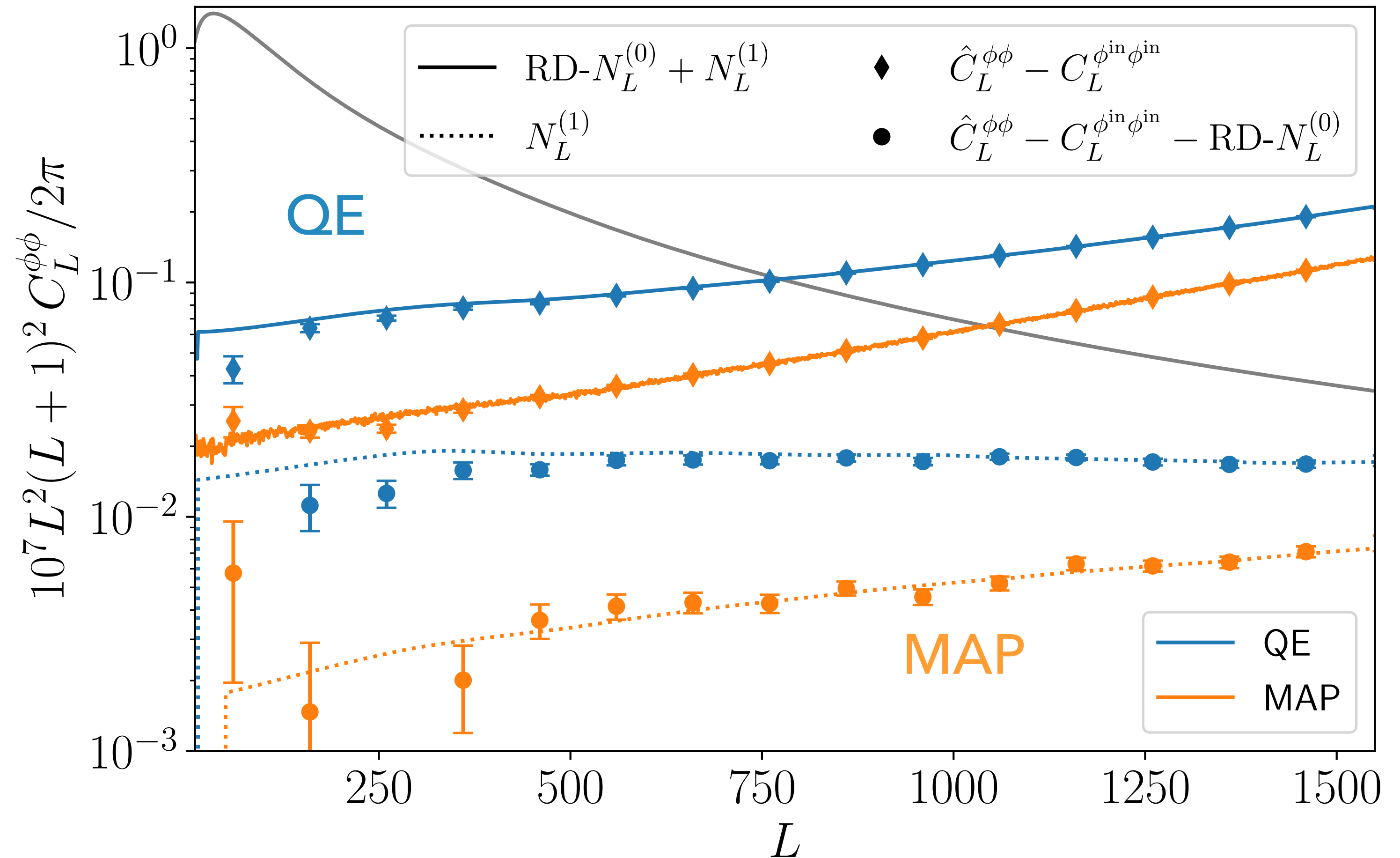
- ▶ Correct small bias with simulations



ITERATIVE BIASES

$$C_L^{\hat{\phi}\hat{\phi}} = C_L^{\phi\phi} + N_L^0 + N_L^1$$

- ▶ Assume N0 and N1 biases are same expression of the QE but with partially delensed CMB spectra
- ▶ We obtain them by iteratively estimating the fiducial delensed CMB spectra and residual lensing power spectrum



REALISATION DEPENDENT DEBIASING

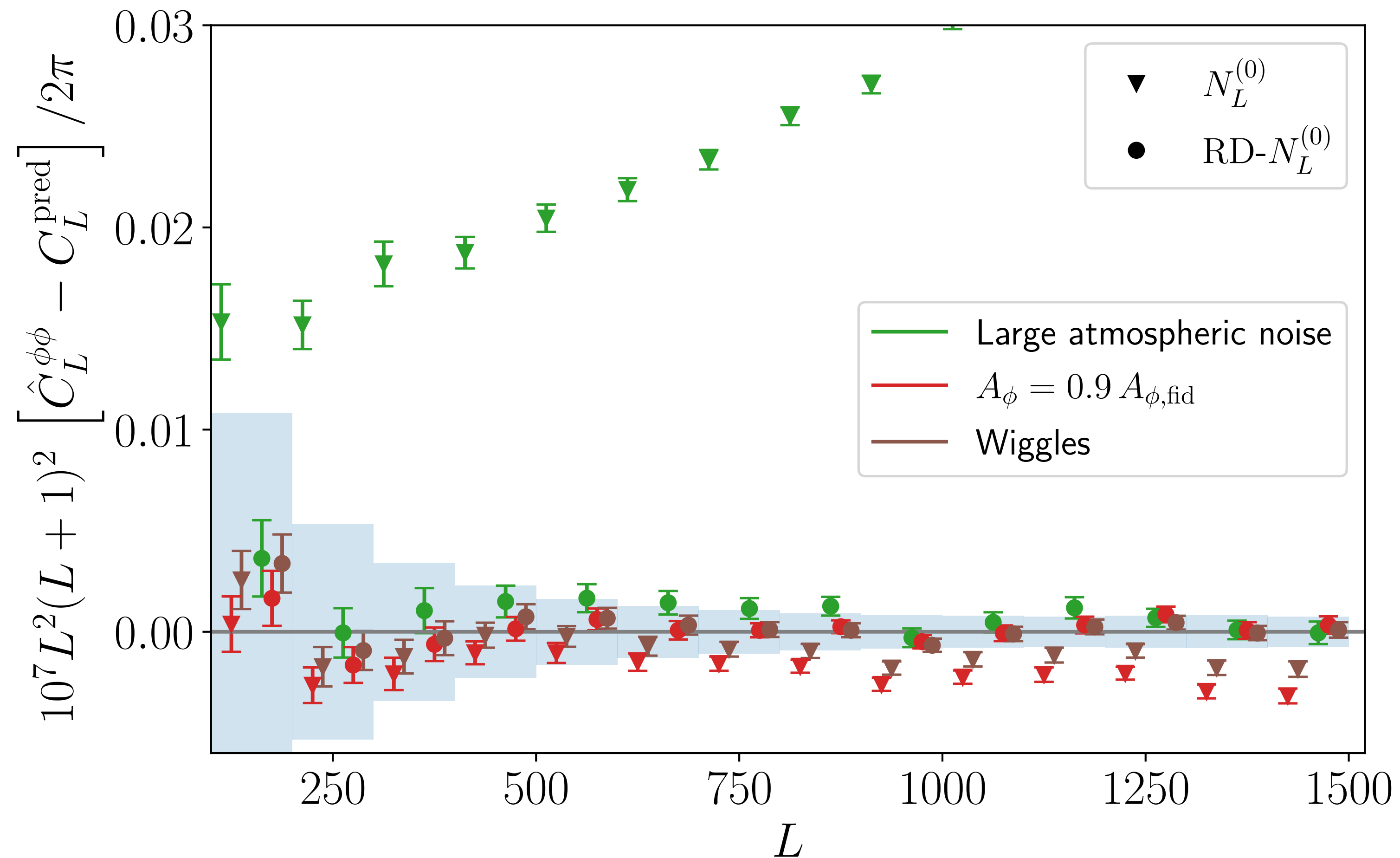
- ▶ Because N0 bias dominates the signal, it needs to be evaluated very accurately
- ▶ Very sensitive to the assumptions made on the spectra and noise of the CMB for the reconstruction
- ▶ Obtain a realisation dependant debaser with a smart combinations of the data maps with simulations in the fiducial settings:

$$\text{RD-}N_L^{(0)} \equiv \left\langle 4\hat{C}_L^{di} - 2\hat{C}_L^{ij} \right\rangle_{N_{\text{bias}}},$$

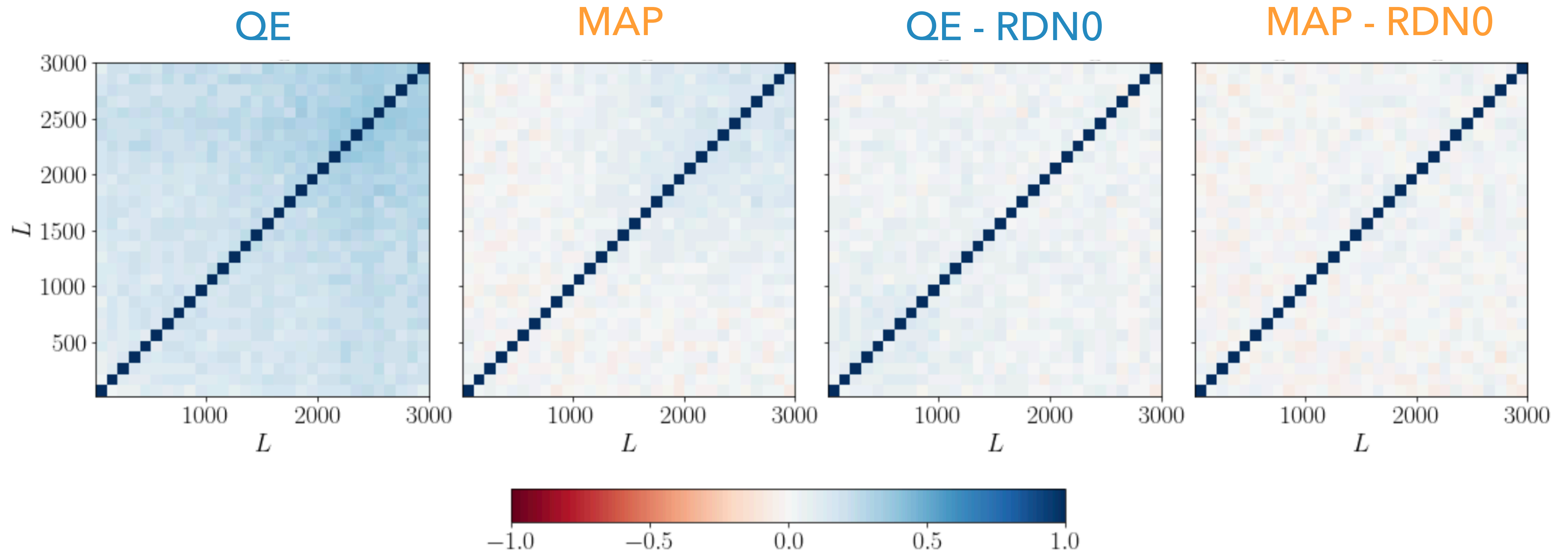
- ▶ This RDN0 is **insensitive at first order to mismatch** in the fiducial spectra

RDNO FOR THE MAP

- ▶ Same as the QE, but simulations have the MAP lensing potential instead of being random



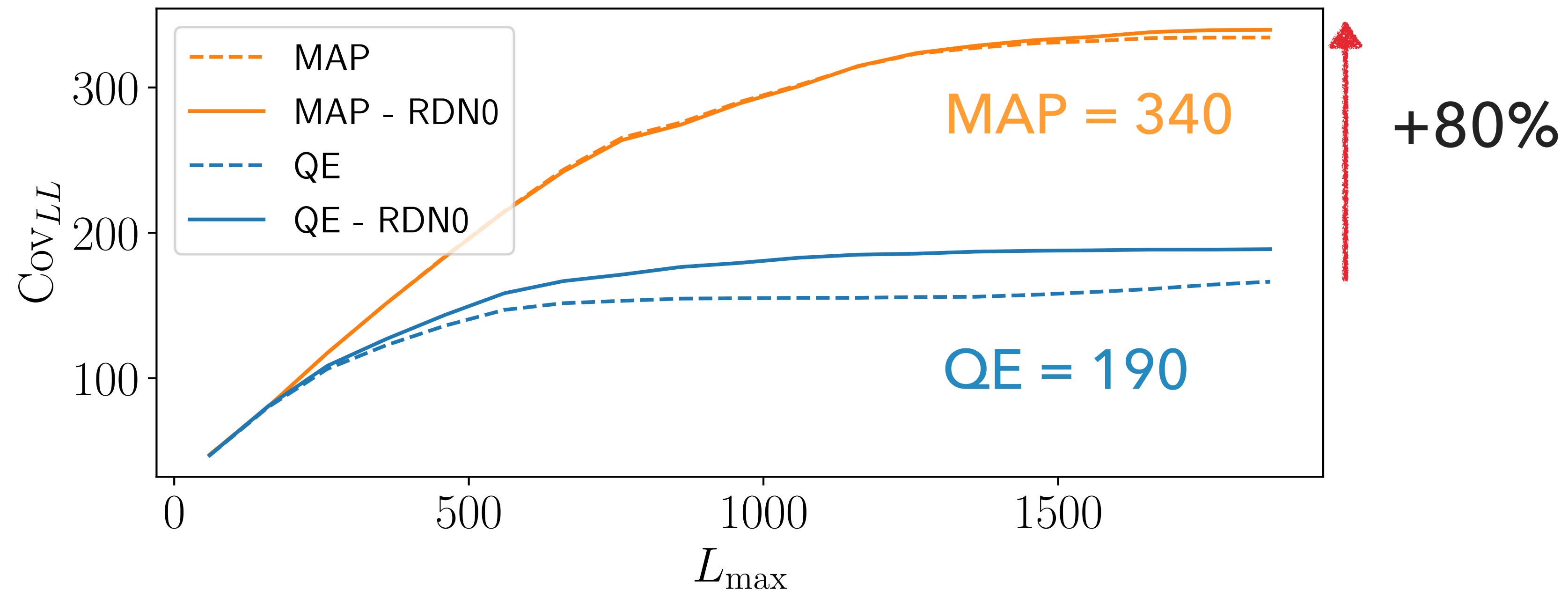
CORRELATION MATRICES



- ▶ 1024 flat sky CMB-S4 like simulations
- ▶ Covariance matrices normalised by the diagonal

SIGNAL TO NOISE RATIO

$$\text{SNR}(L_{\max}) = \sqrt{\sum_{L_{\min}}^{L_{\max}} C_L^{\phi\phi, \text{fid}} \text{Cov}_{LL'}^{-1} C_L^{\phi\phi, \text{fid}}}$$



- ▶ Signal to noise ratio of the lensing power spectrum as a function of the maximum scale used in the analysis
- ▶ Information gain saturates above 1000 for QE and 1500 for MAP

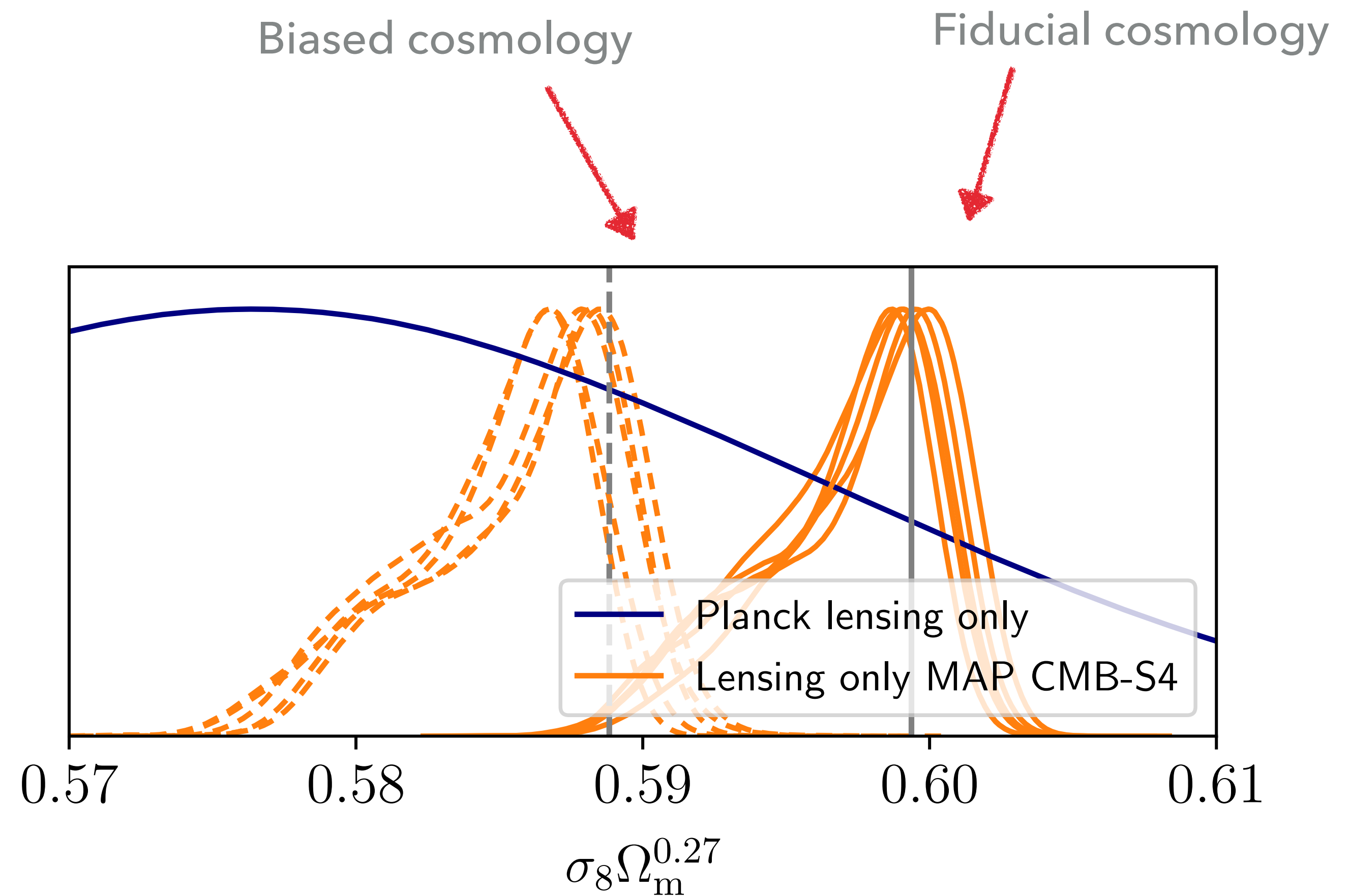
LIKELIHOOD ANALYSIS

$$\ln L(\theta | \hat{\phi}) = -\frac{1}{2} \left(C_L^{\hat{\phi}\hat{\phi}} - RD-N_L^0 - C^{\phi\phi}(\theta) - N_L^1(\theta) \right)^T \mathbf{Cov}^{-1} \left(C_L^{\hat{\phi}\hat{\phi}} - RD-N_L^0 - C^{\phi\phi}(\theta) - N_L^1(\theta) \right)$$

- ▶ Estimate most likely cosmology by sampling the parameter space with a MCMC
- ▶ Do not re-estimate the lensing potential for each step of the sampling
- ▶ Introduce a possible bias (mismatch between the fiducial and the true cosmology)
- ▶ We correct this bias at first order
 - ▶ on the normalisation of the lensing potential
 - ▶ on the N1 bias

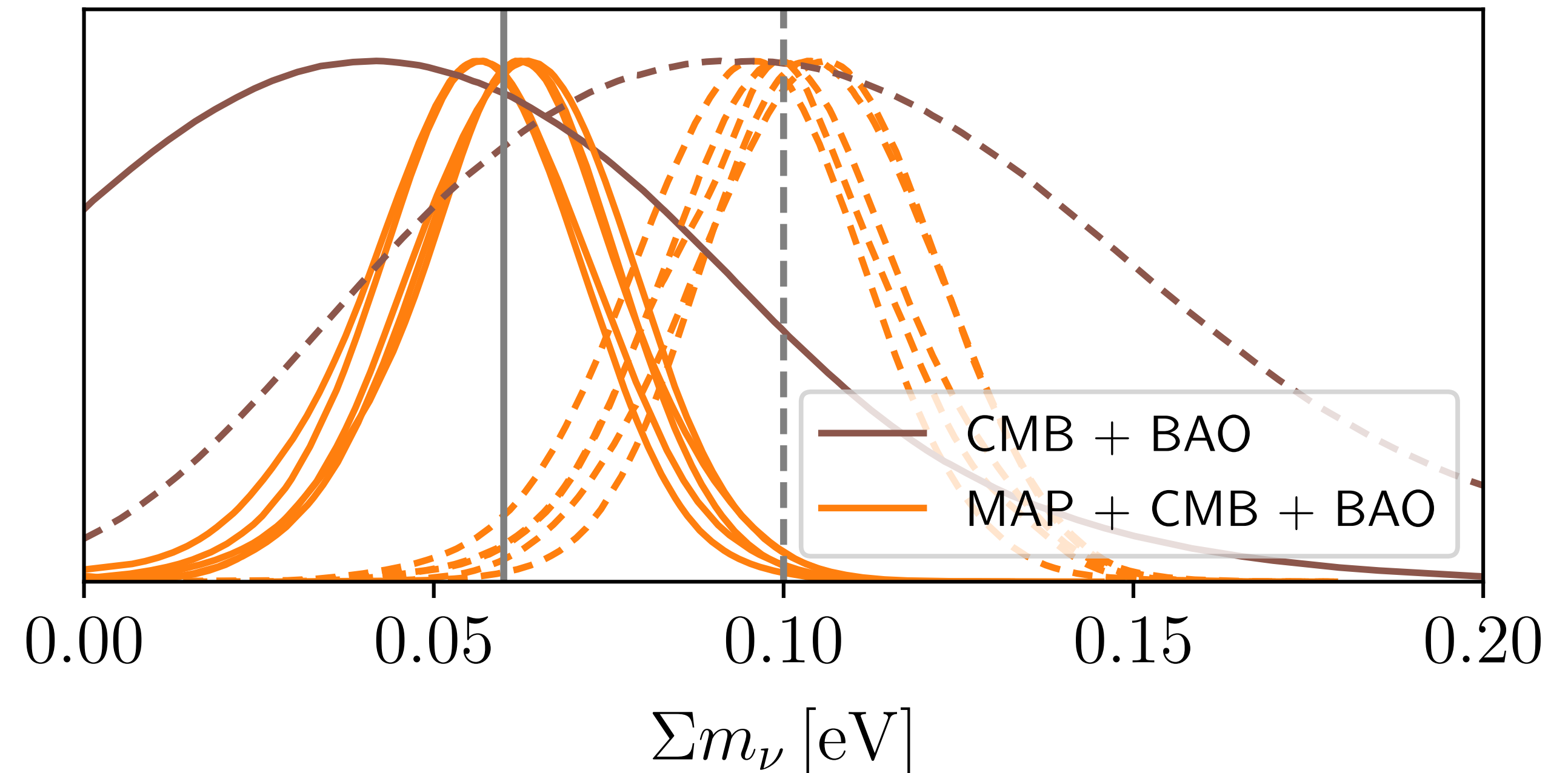
LENSING LIKELIHOOD

- ▶ Two datasets:
 - ▶ One in the fiducial cosmology used for the reconstruction
 - ▶ and a cosmology with less matter and more massive neutrinos
- ▶ Sampling 6 LCDM parameters
- ▶ We found unbiased estimates of the $\sigma_8 - \Omega_m$ combined parameter.



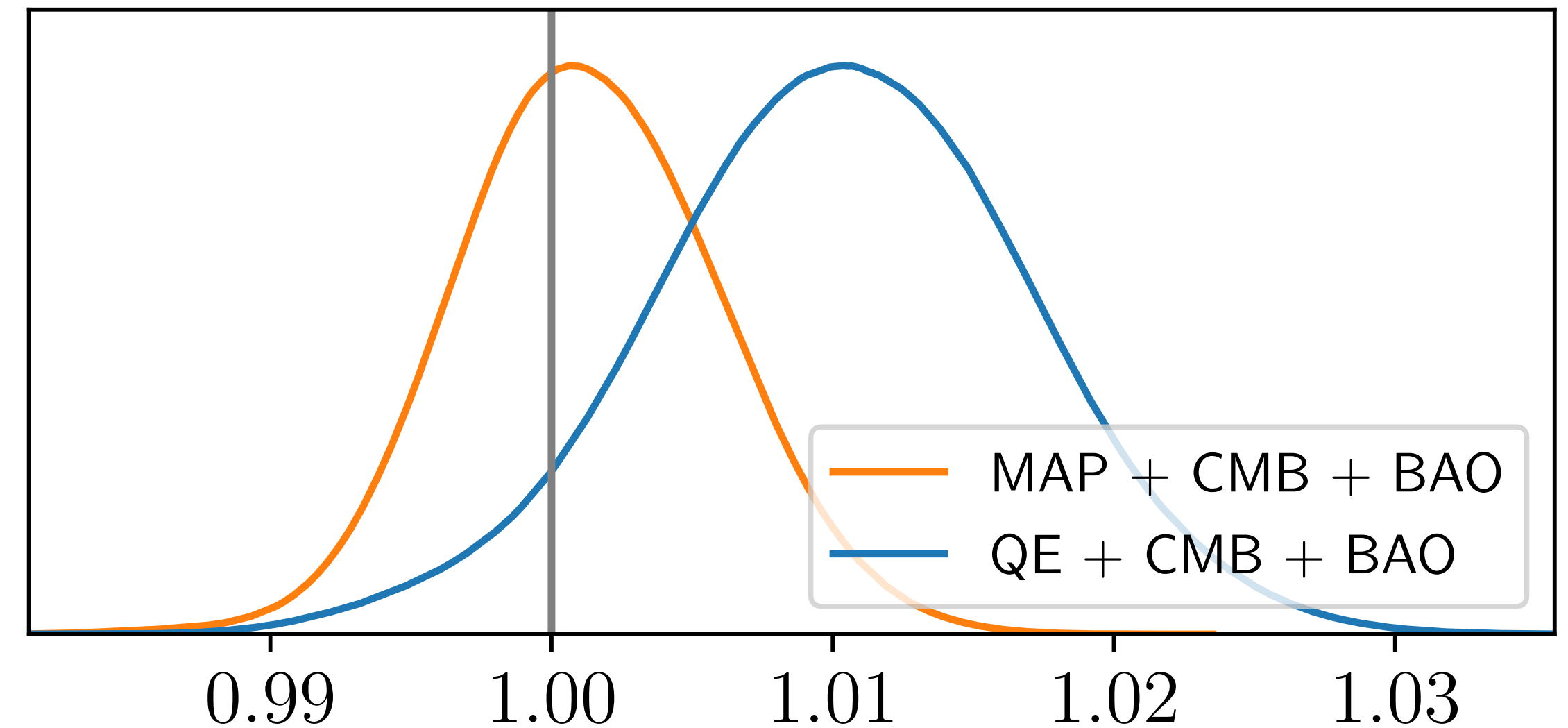
NEUTRINO MASS ESTIMATES

- ▶ Combining MAP likelihood with:
 - ▶ Unlensed CMB-S4 likelihood
 - ▶ DESI BAO likelihood
- ▶ Varying 6 LCDM parameters + Sum of the neutrino mass
- ▶ Fiducial $\sum m_\nu = 0.06 \text{ eV}$
- ▶ Strong prior on tau: $\sigma(\tau) = 0.002$ (LiteBIRD constraints)
- ▶ CMB-S4 will allow for a 4σ detection of massive neutrinos



COMPARING MAP TO QE CONSTRAINTS

- ▶ Combining MAP with CMB and BAO, we get $\sigma_{M_\nu} = 0.016$
- ▶ No improvement compared to the QE spectrum
- ▶ Due to remaining degeneracies between parameters
- ▶ We perform a PCA on $\sum m_\nu, \Omega_m, \tau$ combination
- ▶ Improvement of 40%



$$I = (1 + \sum m_\nu - (\sum m_\nu)^{\text{fid}}) (\Omega_m / \Omega_m^{\text{fid}})^{-1.7} (\tau / \tau^{\text{fid}})^{-0.18}$$

CONCLUSION

- ▶ Iterative methods will reconstruct optimally the lensing potential for next generation CMB surveys
- ▶ We introduced a **simple and robust** end-to-end pipeline to get an **optimal estimation of the lensing spectrum**
- ▶ Increases the signal to noise ratio of the lensing amplitude by 80%
- ▶ Robust to uncertainties in fiducial cosmology and observational noise
- ▶ Will get constraints on cosmological parameters of interest, such as the sum of neutrino mass