



A Model-Independent Test on Variations in the Peak Luminosity of Type Ia Supernovae.

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Cosmology from Home
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Work Based on
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Motivation:

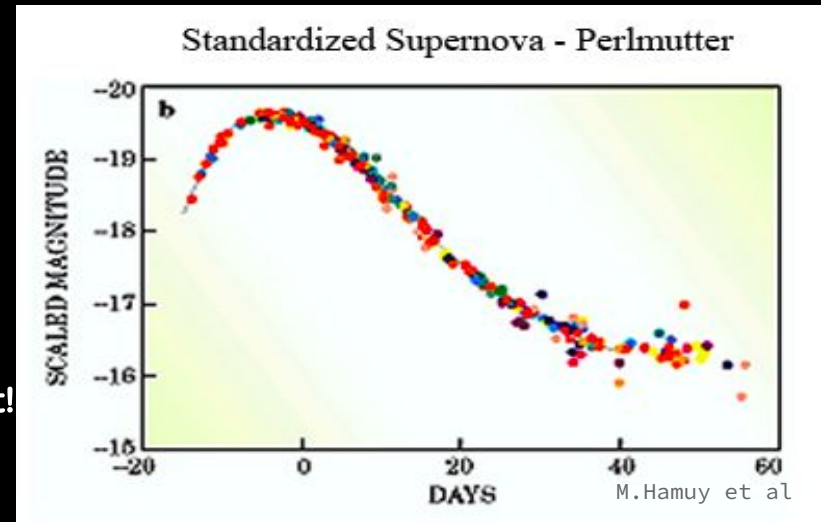
● **Type Ia SNa: Standard Candle:** direct evidence for the accelerating universe

→ **Assumption:** Intrinsic Luminosity (or M_B) independent to redshift

→ **Intrinsic Luminosity Depends:**

- ✧ Host morphology
- ✧ Host mass
- ✧ Local star formation rate

● **AIM** → Evolution of Luminosity with time or redshift!



Contents:

- Basics of Cosmology
- Observations
- Statistics
- Results
- Conclusions

Basics of Cosmology:

- **Cosmological Principle:** Spatially Homogeneous and Isotropic at large scale.
- **The Friedmann–Lemaître–Robertson–Walker metric:**

$$ds^2 = -dt^2 + a^2(t) \left[\frac{dr^2}{1 - kr^2} + r^2 d\theta^2 + r^2 \sin^2 \theta d\phi^2 \right]$$

where, $a(t)$ = Scale factor, $c = 1$, $k = -1, 0, +1$ for open, flat, close universe.

- **Einstein Equations:**

$$R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} + \Lambda g_{\mu\nu} = 8\pi GT_{\mu\nu}$$

$R_{\mu\nu}$ = Ricci tensor, R = Ricci scalar, $g_{\mu\nu}$ = Metric tensor & Λ = Cosmological constant.

Cosmology Overview:

● Energy Momentum Tensor:

$$T^{\mu\nu} = (P + \rho) u^\mu u^\nu + P g^{\mu\nu}$$

u^μ is 4-velocity, P and ρ are pressure and energy density of perfect fluid.

● Friedmann Equations:

$$3 \frac{\dot{a}^2 + k}{a^2} - \Lambda = 8\pi G \rho$$

$$2 \frac{\ddot{a}}{a} + \frac{\dot{a}^2 + k}{a^2} - \Lambda = -8\pi G P$$

$$\frac{\ddot{a}}{a} = -\frac{4\pi G}{3}(\rho + 3P) + \frac{\Lambda}{3}$$

↑
Slow down expansion

↑
Speed up expansion

Basics of Cosmology:

● Hubble Parameter:

$$H(z) \equiv H_0 E(z) = H_0 \sqrt{\Omega_{m0}(1+z)^3 + \Omega_{k0}(1+z)^2 + \Omega_{\Lambda0}}$$
$$H_0 = \frac{\dot{a}(t_0)}{a(t_0)} = \text{Hubble Constant}$$

● Cosmological Redshift:

$$z \equiv \frac{\lambda_0 - \lambda_e}{\lambda_e} \quad \frac{a(t_0)}{a(t_e)} \equiv z + 1$$

● Cosmological Density Parameters:

$$\Omega_{m0} = \frac{8\pi G \rho_m}{3H_0^2}; \quad \Omega_{k0} = \frac{-k}{H_0^2 a_0^2}; \quad \Omega_{\Lambda0} = \frac{\Lambda}{3H_0^2}$$

$$\Omega_{m0} + \Omega_{k0} + \Omega_{\Lambda0} = 1$$

Distances in Cosmology:

Comoving Distance:

$$d_{co} = \frac{d_p(z)}{\left(\frac{a(t)}{a(t_0)}\right)} = (1 + z)d_p(z)$$

Angular Diameter Distance: Standard Ruler

$$d_A(z) = \frac{d_{co}}{1 + z}$$

Luminosity Distance: Standard Candle

$$d_L(z) = d_{co}(1 + z)$$

Distances in Cosmology:

$$d_A(z) = \frac{d_{co}}{(1+z)} = \frac{d_L(z)}{(1+z)^2} = \begin{cases} \frac{1}{(1+z)H_0\sqrt{\Omega_{k0}}} \sinh\left(\sqrt{\Omega_{k0}} \int_0^z \frac{dz'}{E(z')}\right) & \text{for } \Omega_{k0} > 0 \\ \frac{1}{(1+z)H_0} \int_0^z \frac{dz'}{E(z')} & \text{for } \Omega_{k0} = 0 \\ \frac{1}{(1+z)H_0\sqrt{-\Omega_{k0}}} \sin\left(\sqrt{-\Omega_{k0}} \int_0^z \frac{dz'}{E(z')}\right) & \text{for } \Omega_{k0} < 0 \end{cases}$$

Standard Candle: Type Ia Supernova

Flux:

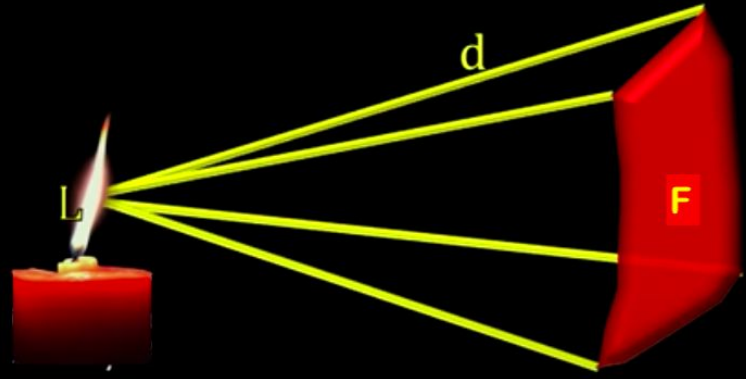
$$F = \frac{L}{4\pi d_L^2}$$

Luminosity Distance:

$$d_L(z; M_B) = 10^{(m_B - M_B - 25)/5} \text{ [Mpc]}$$

CDDR:

$$d_A = \frac{d_L}{(1+z)^2}$$

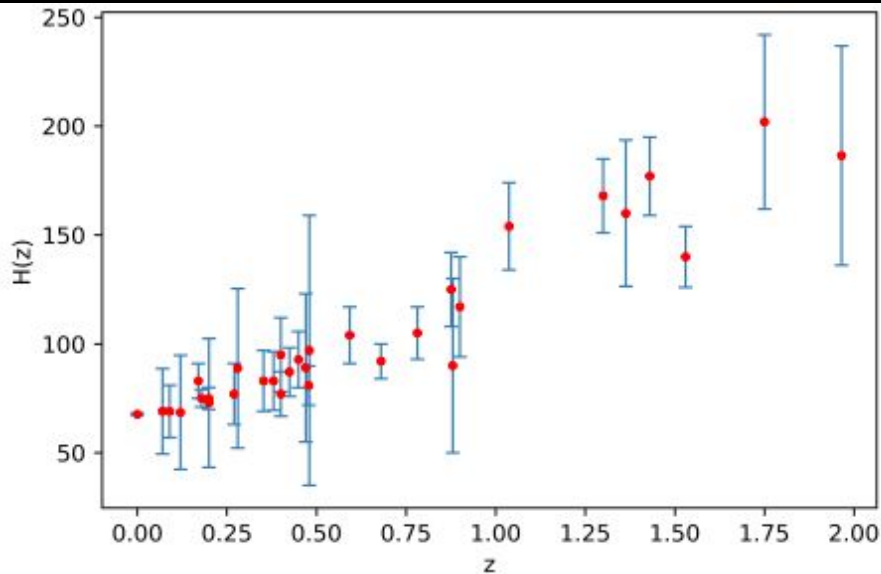


$$m_B(z; \Omega_{k0}, M_B) = 5 \log_{10} \left(d_A(z; \Omega_{k0}) (1+z)^2 \right) + M_B + 25$$

Observable Datasets:

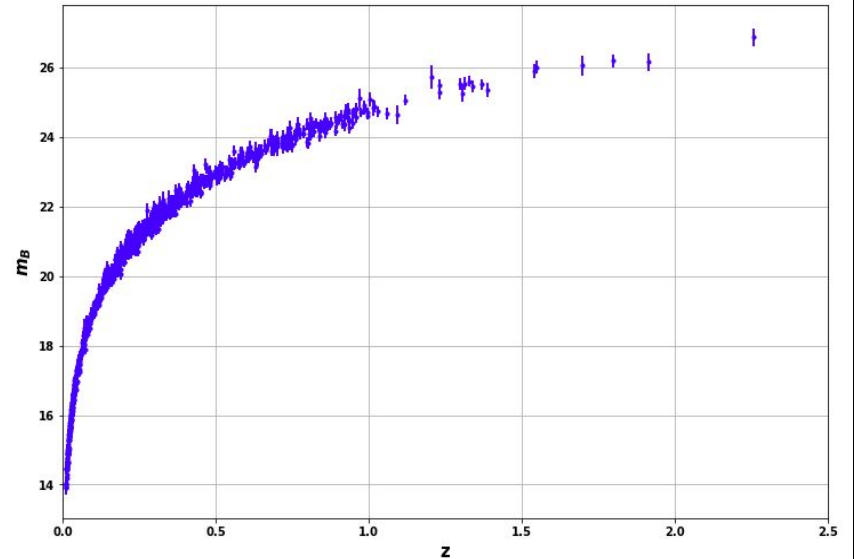
● Hubble Parameter Dataset (CC):

31 data points of $H(z)$ with redshifts in the range $0 < z < 2$



● SNIa Dataset (Pantheon):

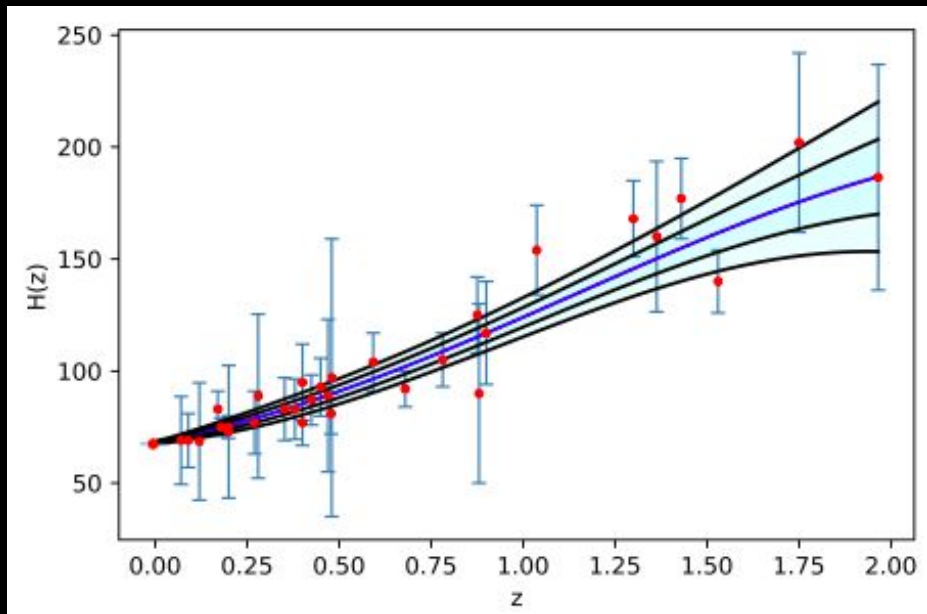
1048 data points of $m(z)$ with redshifts in the range $0 < z < 2$



Statistical Tools:

● Dataset Reconstruction [GP]:

● Parameter Estimation [EMCEE]:



$$\chi^2 = \Delta m^T \cdot C^{-1} \cdot \Delta m$$

$$\Delta m = m_B^{\text{obs}}(z_i) - m_B^{\text{th}}(z_i; \eta, M_B, \Omega_{k0})$$

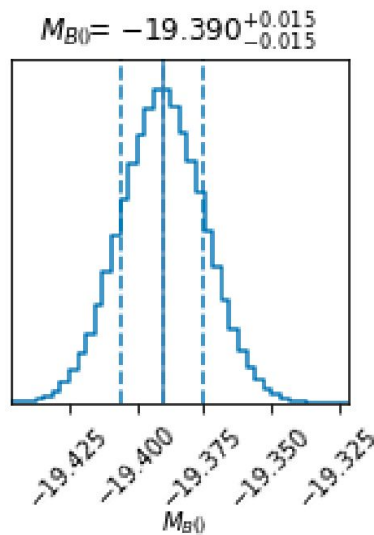
$$C = D_{\text{stat}} + C_{\text{sys}}$$

Results:

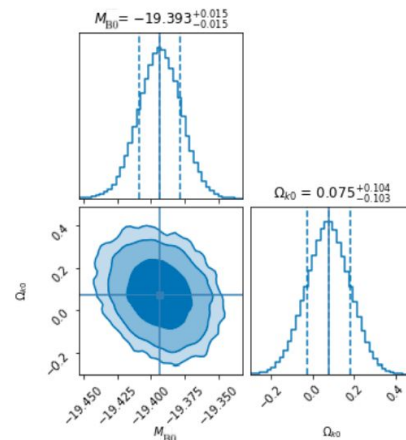
arXiv:2107.04784

● P1. $M_B = M_{B0}$

Parameter	Flat Universe	Non-Flat Universe
M_{B0}	$-19.390^{+0.015}_{-0.015}$	$-19.393^{+0.015}_{-0.015}$
Ω_{k0}	—	$0.075^{+0.104}_{-0.103}$



(a) Flat Universe



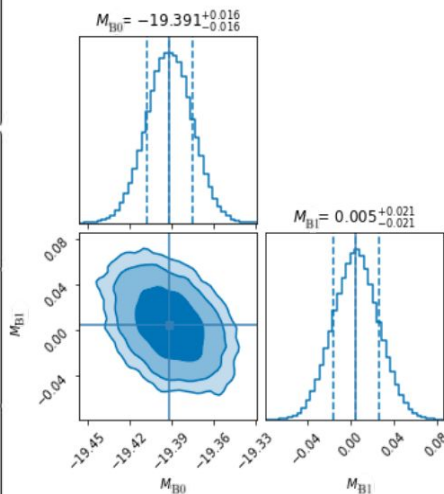
(b) Non-Flat Universe

Results:

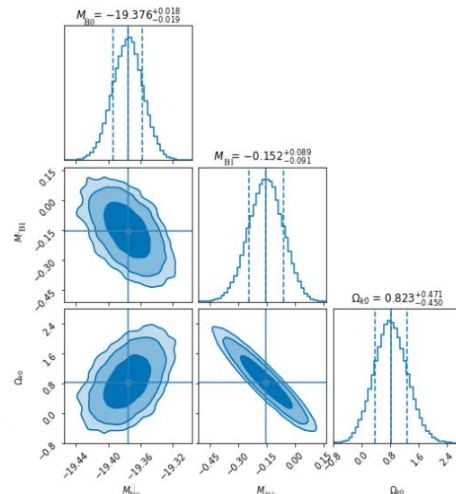
arXiv:2107.04784

● **P2.** $M_B = M_{B0} + M_{B1}z$

Parameter	Flat Universe	Non-Flat Universe
M_{B0}	$-19.391^{+0.016}_{-0.016}$	$-19.376^{+0.018}_{-0.019}$
M_{B1}	$0.005^{+0.021}_{-0.021}$	$-0.152^{+0.089}_{-0.091}$
Ω_{k0}	—	$0.823^{+0.471}_{-0.450}$



(a) Flat Universe



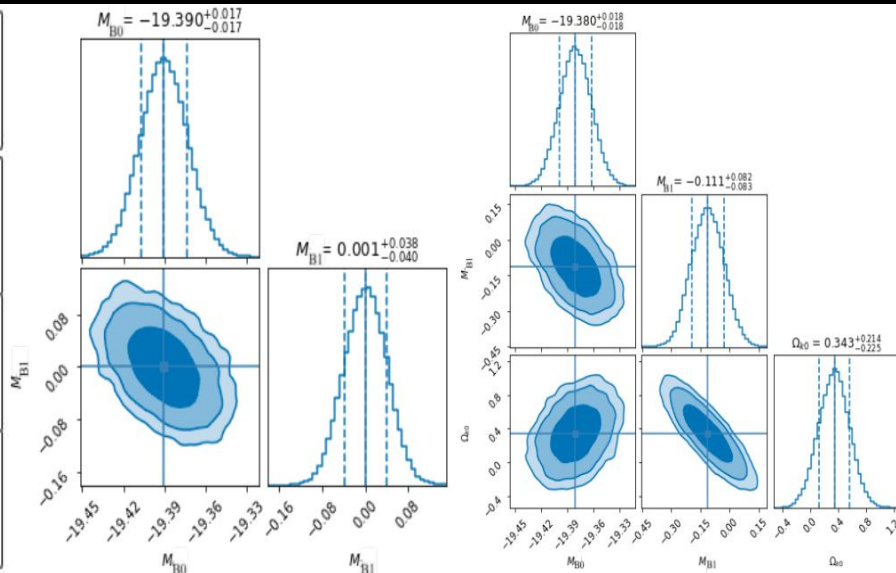
(b) Non-Flat Universe

Results:

arXiv:2107.04784

● **P3.** $M_B = M_{B0} + M_{B1} \frac{z}{1+z}$

Parameter	Flat Universe	Non-Flat Universe
M_{B0}	$-19.390^{+0.017}_{-0.017}$	$-19.380^{+0.018}_{-0.018}$
M_{B1}	$0.001^{+0.038}_{-0.040}$	$-0.111^{+0.082}_{-0.083}$
Ω_{k0}	—	$0.343^{+0.214}_{-0.225}$

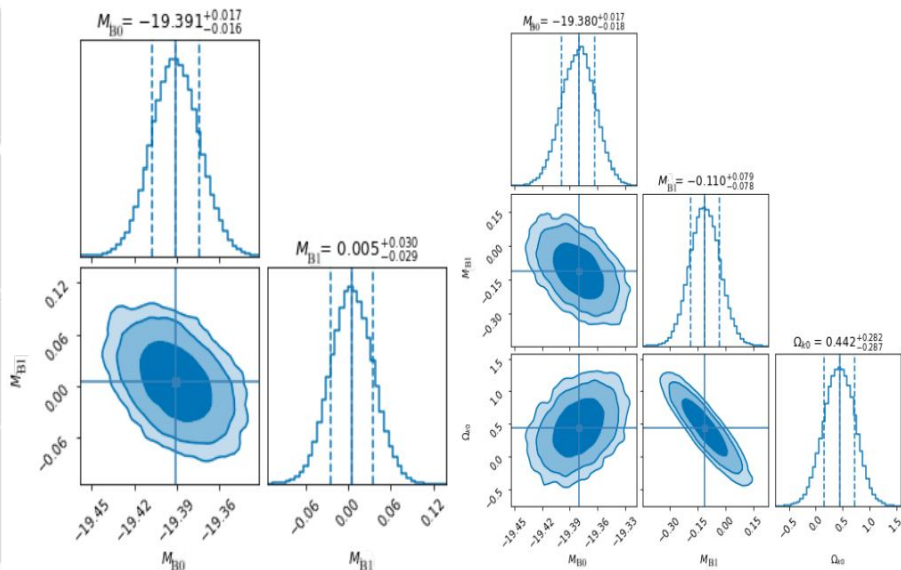


Results:

arXiv:2107.04784

● P4. $M_B = M_{B0} + M_{B1} \ln z$

Parameter	Flat Universe	Non-Flat Universe
M_{B0}	$-19.391^{+0.017}_{-0.016}$	$-19.380^{+0.017}_{-0.018}$
M_{B1}	$0.005^{+0.030}_{-0.029}$	$-0.110^{+0.079}_{-0.078}$
Ω_{k0}	—	$0.442^{+0.282}_{-0.287}$



Conclusions:

- In the flat and non-flat universe cases, all parametrizations support no evolution of absolute magnitude with redshift with 2σ confidence level.
- For all parametrizations of the absolute magnitude M_B , the best fit value of Ω_k suggests a flat universe at 2σ confidence level.
- However, in the parametrizations P2, P3 and P4, the best fit value of Ω_k show mild preference for a non-flat universe.
- From the 1D and 2D contours of all four parametrizations of $M_B(z)$ for non-flat case, we observed a negative correlation between the absolute magnitude and cosmic curvature which should be analysed further.

THANK YOU!