



Minkowski Functionals in Joint Galaxy Clustering & Weak Lensing Analyses

Cosmology from Home 2022

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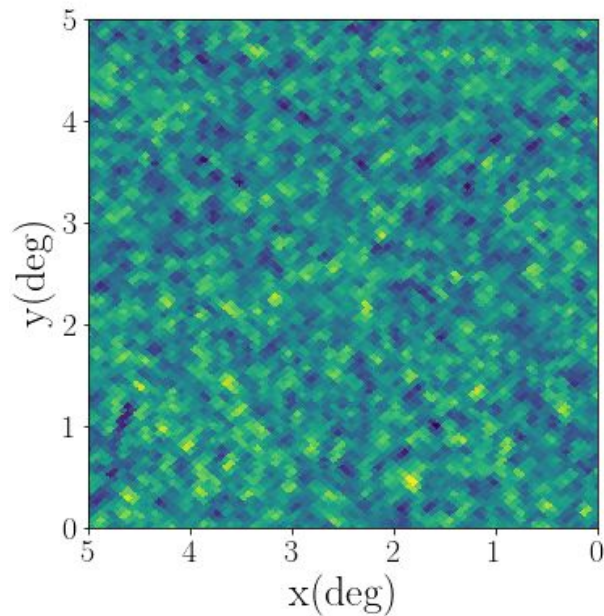
- Power spectra measured from convergence and clustering maps have high constraining power
- Minkowski functionals measured from convergence maps have high constraining power

Goal: Investigate the constraining power of the higher order statistics Minkowski functionals measured from density clustering maps

Simulations

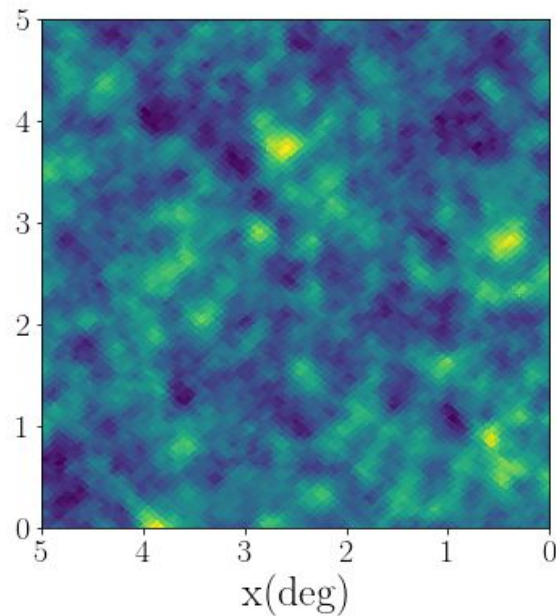


Convergence



-0.05 0.00 0.05

Clustering

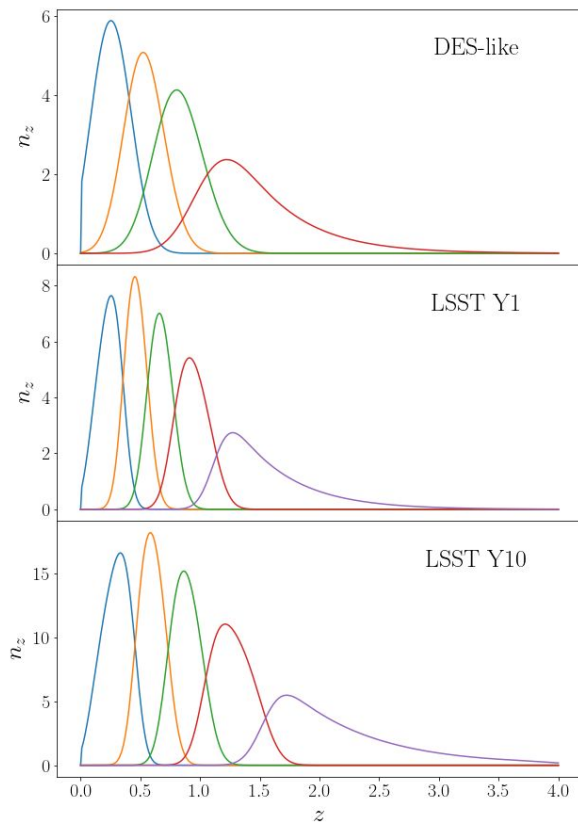


-0.5 0.0 0.5

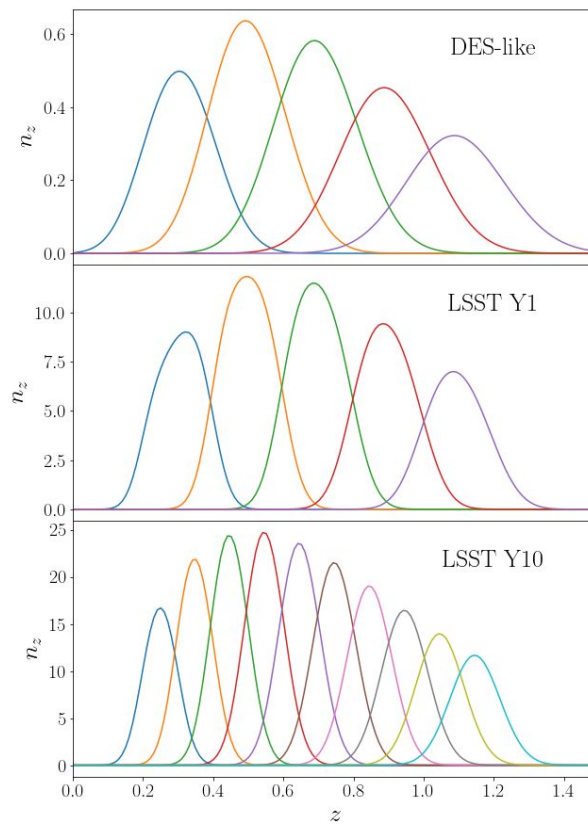
Redshift Distributions



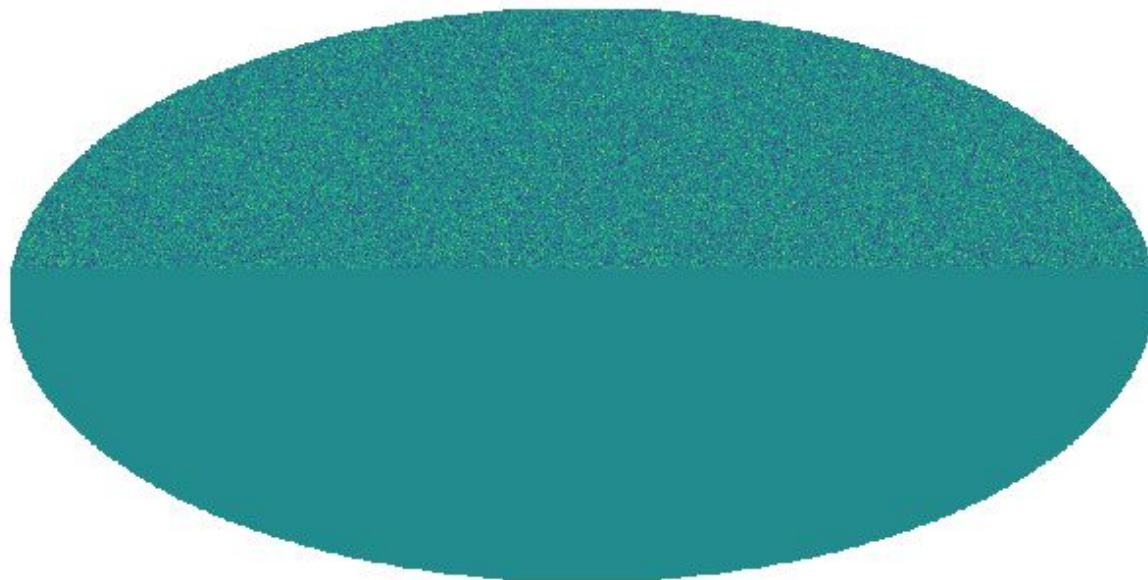
Convergence



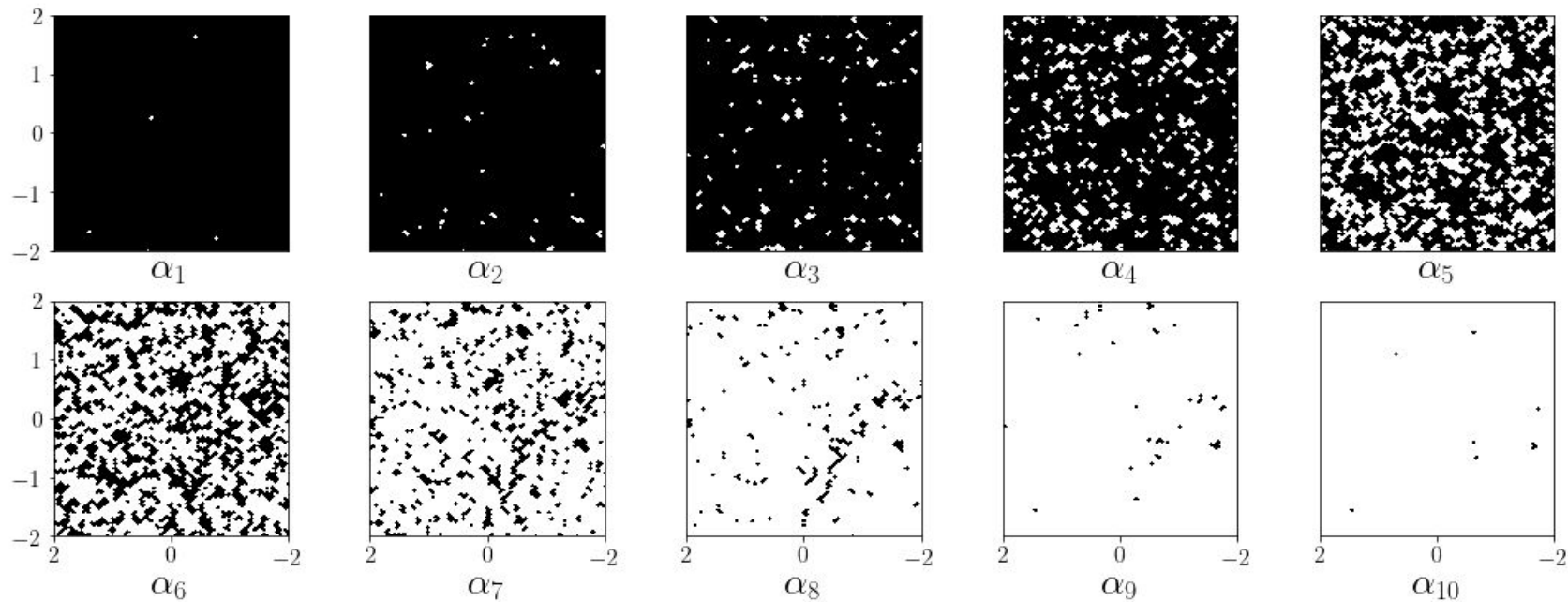
Clustering



Simplified Sky Masking



Excursion Sets



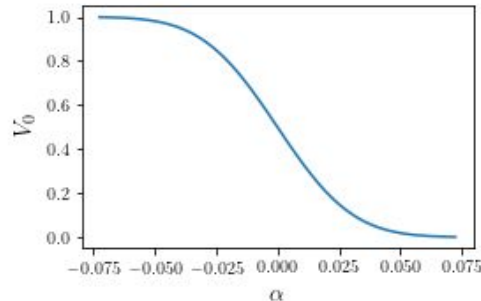
Minkowski Functionals (MF)

$$V_0(v) = \frac{1}{A} \int_A \Theta(\alpha(\mathbf{x}) - v) d\phi d\theta$$

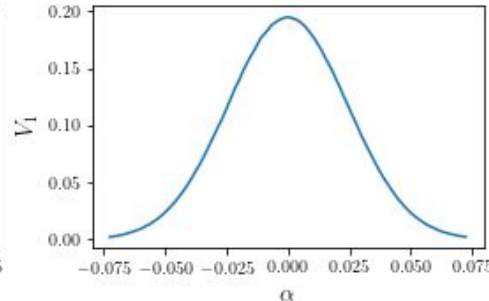
$$V_1(v) = \frac{1}{4A} \int_A \delta(\alpha(\mathbf{x}) - v) \sqrt{\alpha_\phi^2 + \alpha_\theta^2} d\phi d\theta$$

$$V_2(v) = \frac{1}{2\pi A} \int_A \delta(\alpha(\mathbf{x}) - v) \frac{2\alpha_\phi \alpha_\theta \alpha_{\phi\theta} - \alpha_\phi^2 \alpha_{\theta\theta} - \alpha_\theta^2 \alpha_{\phi\phi}}{\alpha_\phi^2 + \alpha_\theta^2} d\phi d\theta$$

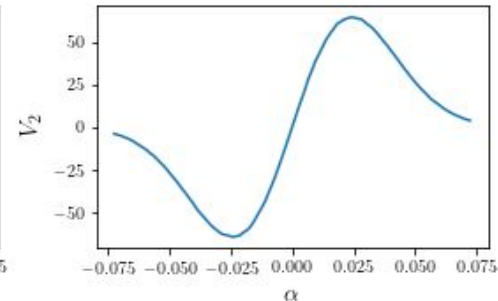
Area



Perimeter

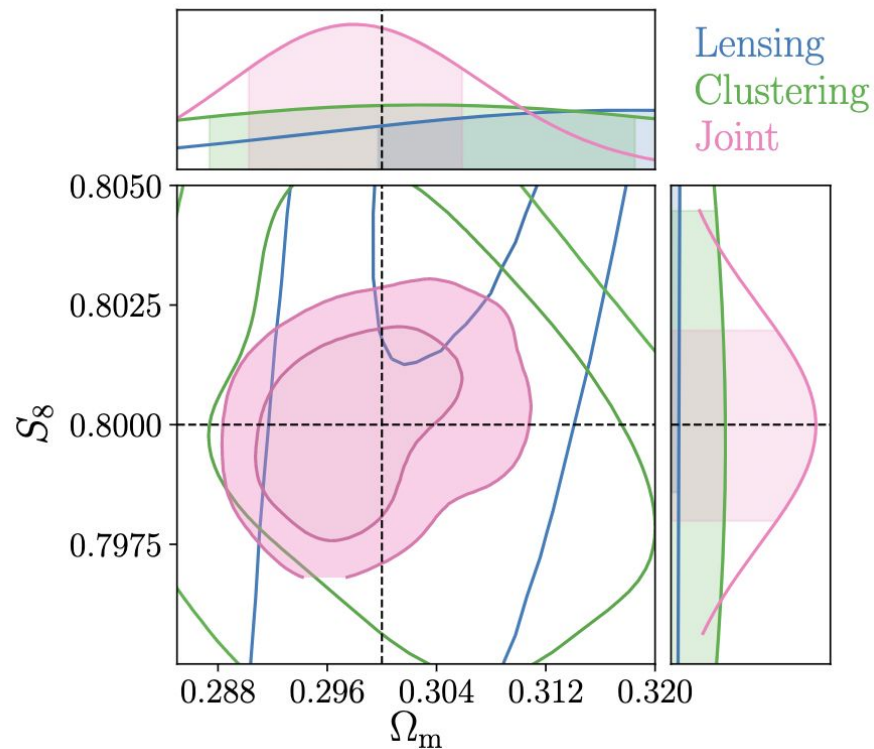
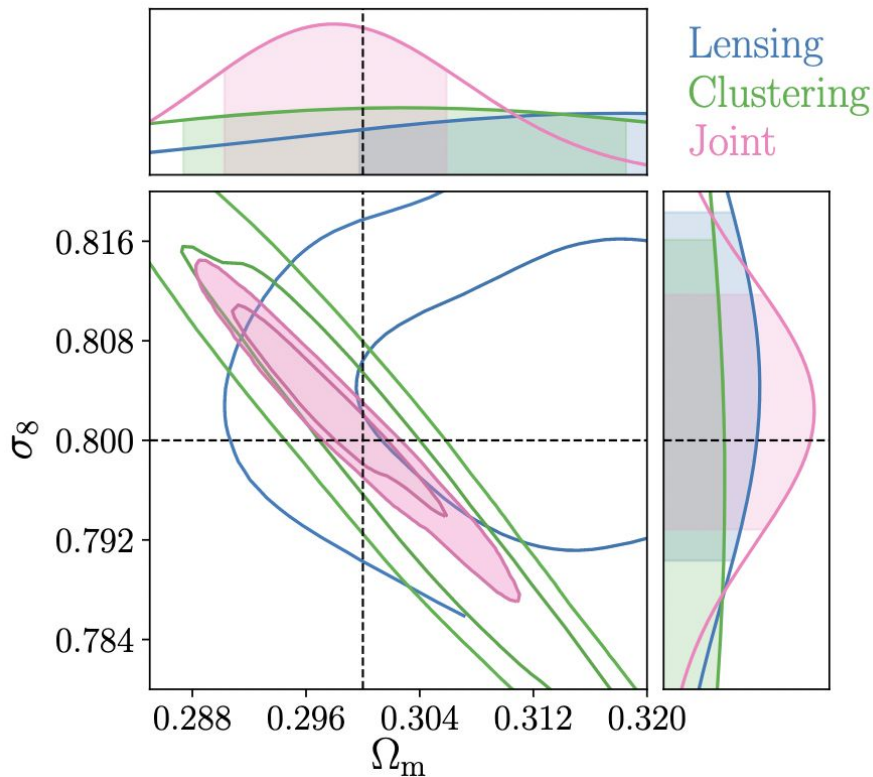


Curvature

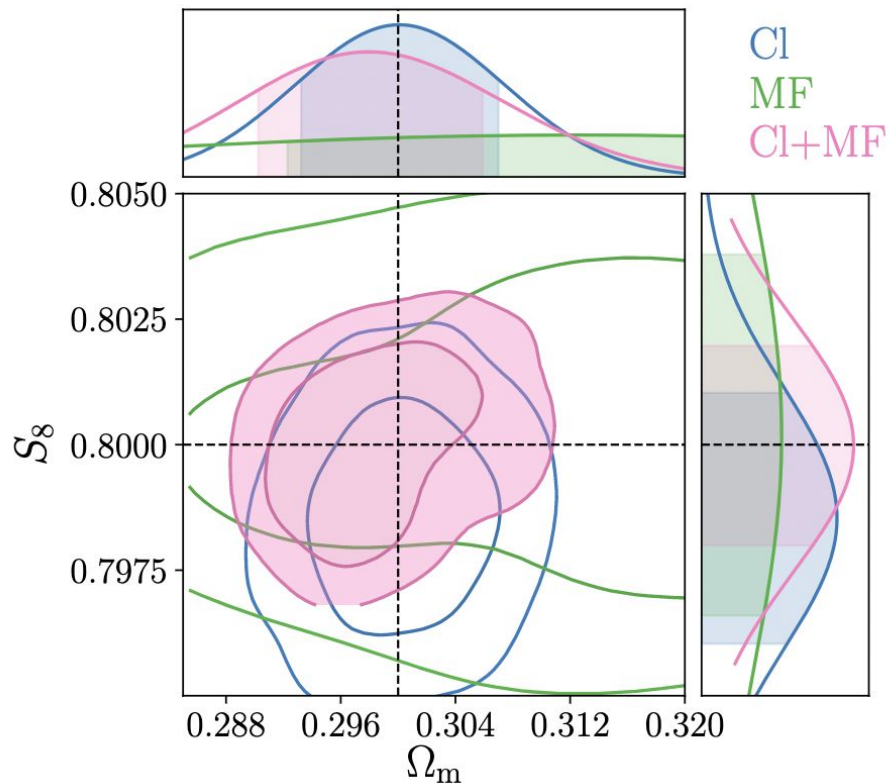
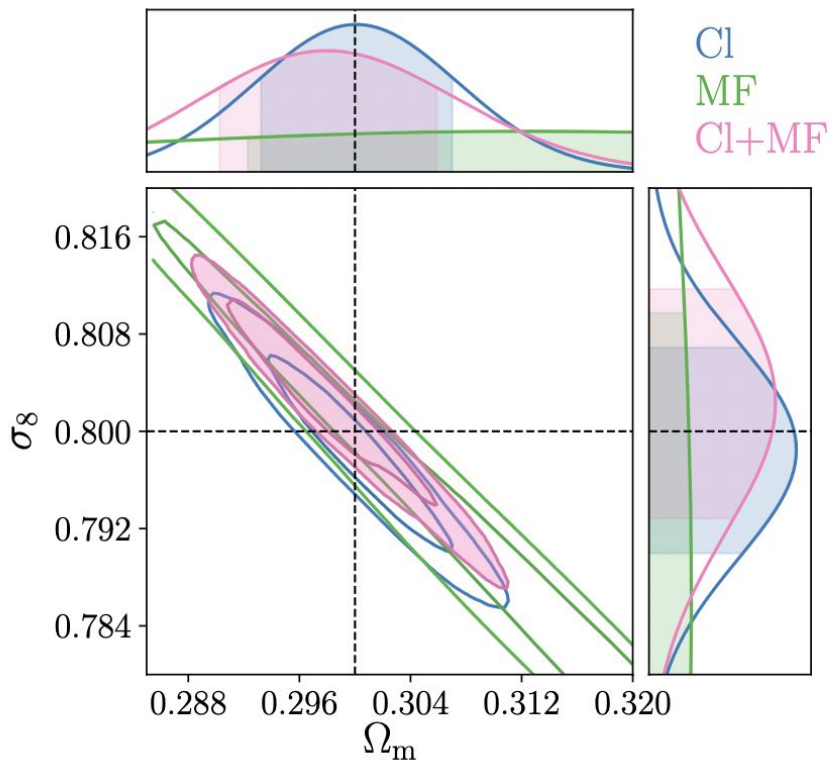


1. Generate simulated convergence and clustering maps
2. Calculate observables (MFs and/or power spectra Cls)
3. Calculate likelihood
 - Get covariance and mean from a set of simulations at fixed cosmology
4. Use Emcee via CosmoSIS to explore the parameter space

Results - Map Type (with MF+CI)



Results - Observables (with lens+clust)



Conclusion



- For a simplified model with both convergence and clustering, MFs don't add information not already contained by CIs
- Adding clustering to the analysis has a significant improvement on the constraints in an joint Minkowski and power spectra analysis, just as in the standard 3x2pt approach
- The S_8 degeneracy direction from MF measurements is the same as for power spectrum measurements
 - Compared to other parameters, it is a more useful diagnostic of constraining power with analysis type and map type

Future Work



- To get stronger constraints from MF calculations, one must study small-scale non-linear regimes with baryonic effects
- Speed up the slow likelihood calculations. Examples:
 - emulator
 - neural network
- Likelihood-free inference
- Other potential applications for MFs:
 - measuring them from shear maps instead of convergence maps
 - doing a cross correlation analysis



Thank you

