



Ultra-light dark matter:

the light and fuzzy side of dark matter

Elisa G. M. Ferreira

Kavli IPMU & University of Sao Paulo

Cosmology from Home 2022

Evidences for dark matter

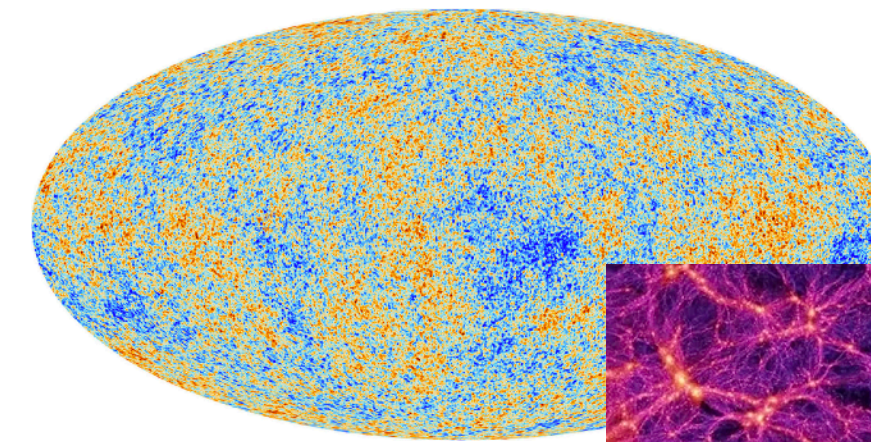
We can observe its effects in

Galaxies



NASA and ESA

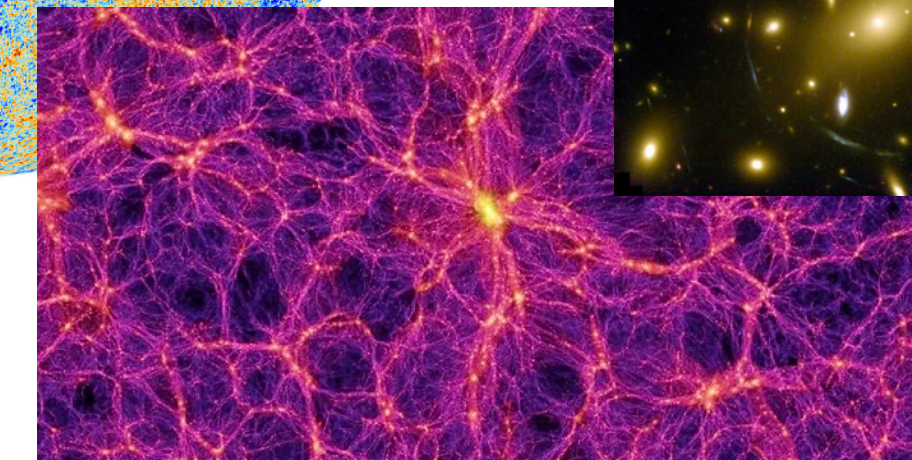
CMB+LSS



ESA and the Planck Collaboration

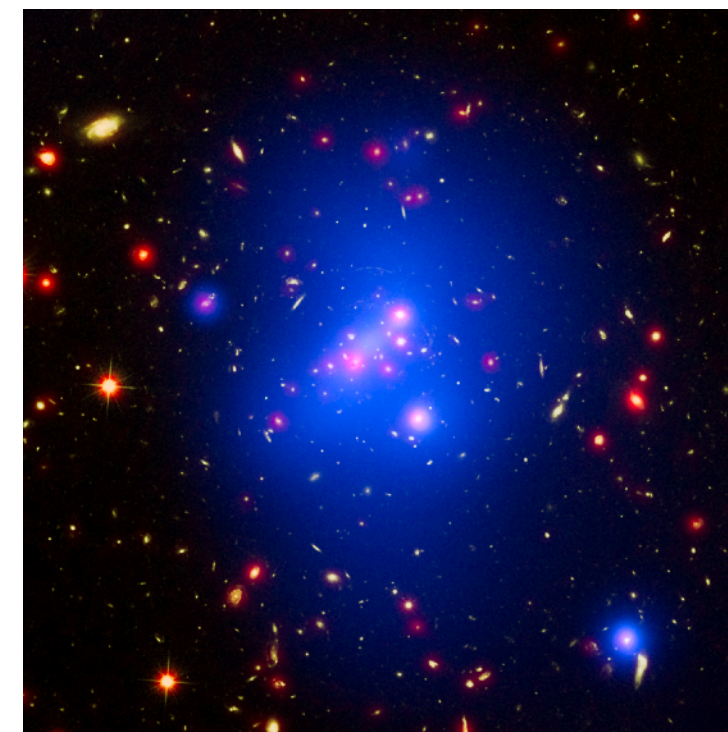


NASA and ESA



Springel & others / Virgo Consortium

Clusters

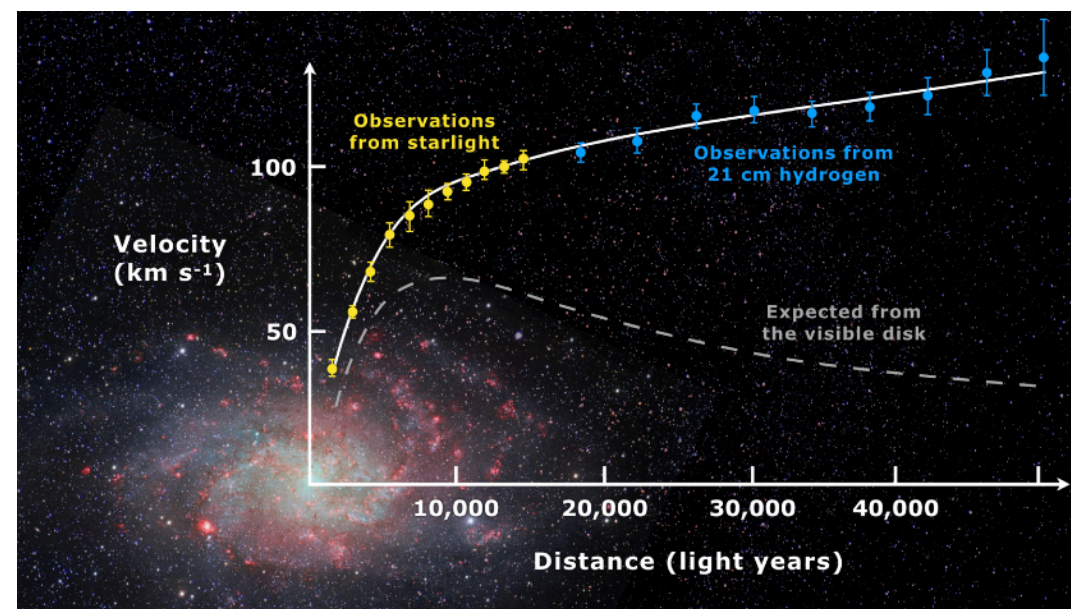


CC BY 4.0

Huge amount of evidence
From **all scales**

Evidences for dark matter

Galaxy rotation curves



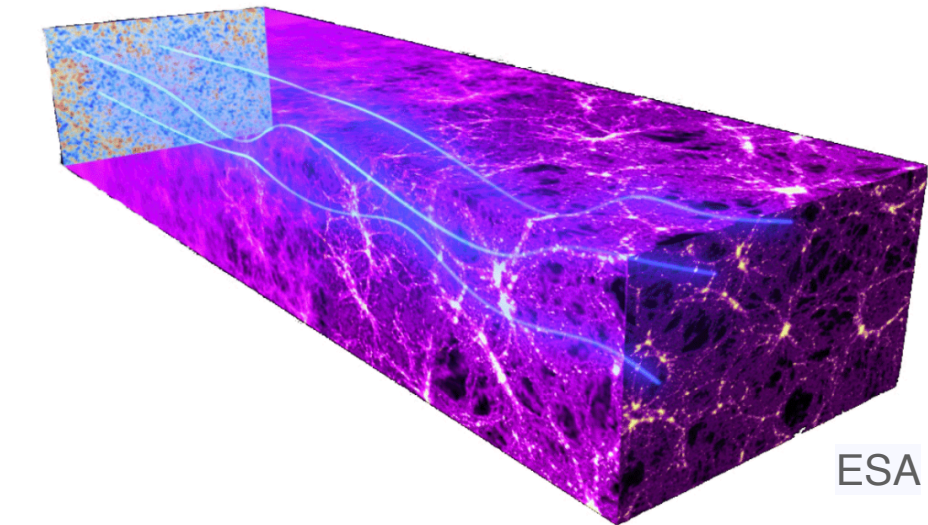
- Mass fraction
- Distribution

Clusters



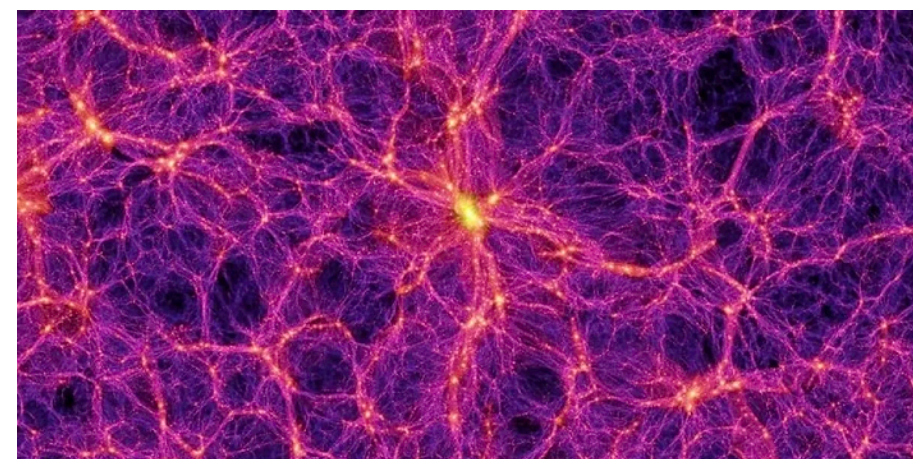
- Mass fraction
- Distribution

Lensing



- | | | |
|-----------------|----------------|-----------------|
| Strong lensing | Weak lensing | Micro lensing |
| • Mass fraction | • Distribution | • Mass fraction |
| • Distribution | • Shape | • Smoothness |
| | • Structure | |

Large Scale Structure



Springel & others / Virgo Consortium

- CMB/LSS
- Ratio of DM/collisional matter
- Thermal history

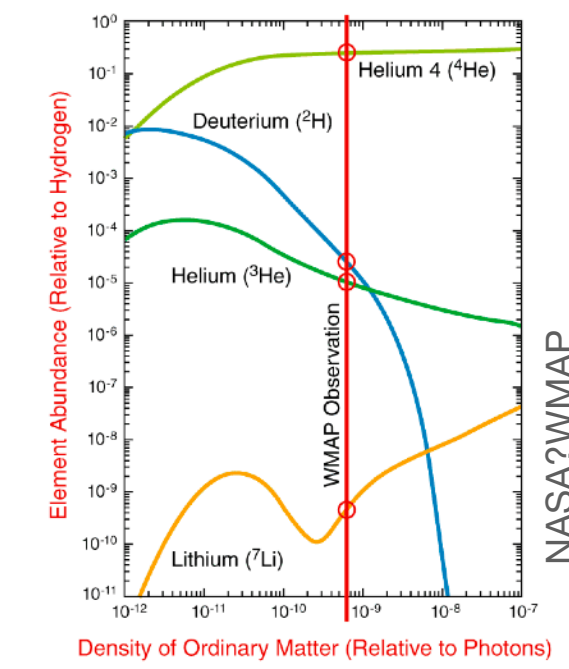
Cluster collision



NASA/CXC/CfA and NASA/STScI

- Distribution
- Separation from collisional matter
- Self-interaction

Big Bang Nucleosynthesis



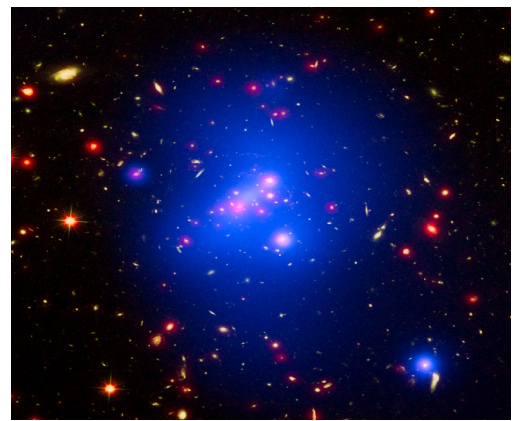
- Amount of baryons

What we *know* about dark matter

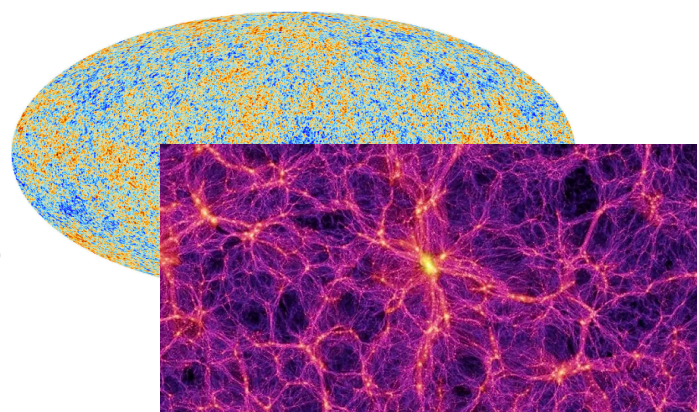
Galaxies



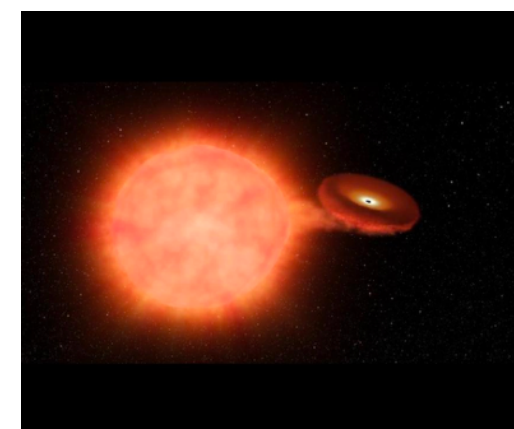
Clusters



Large scales

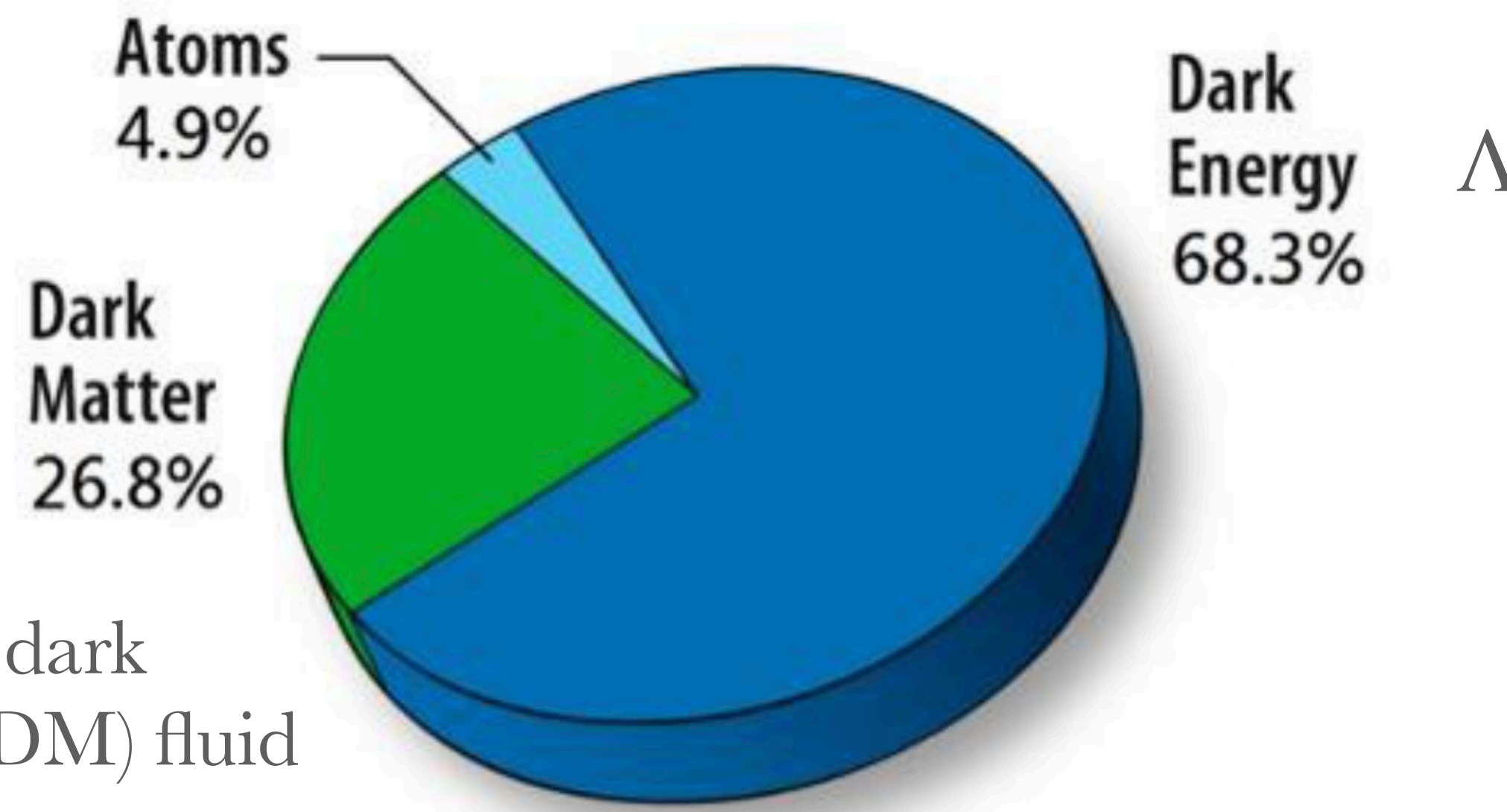


Sn Ia



Λ CDM – the **standard cosmological model**

Successful description of our universe with 6 free parameters, tested to sub-percent precision.

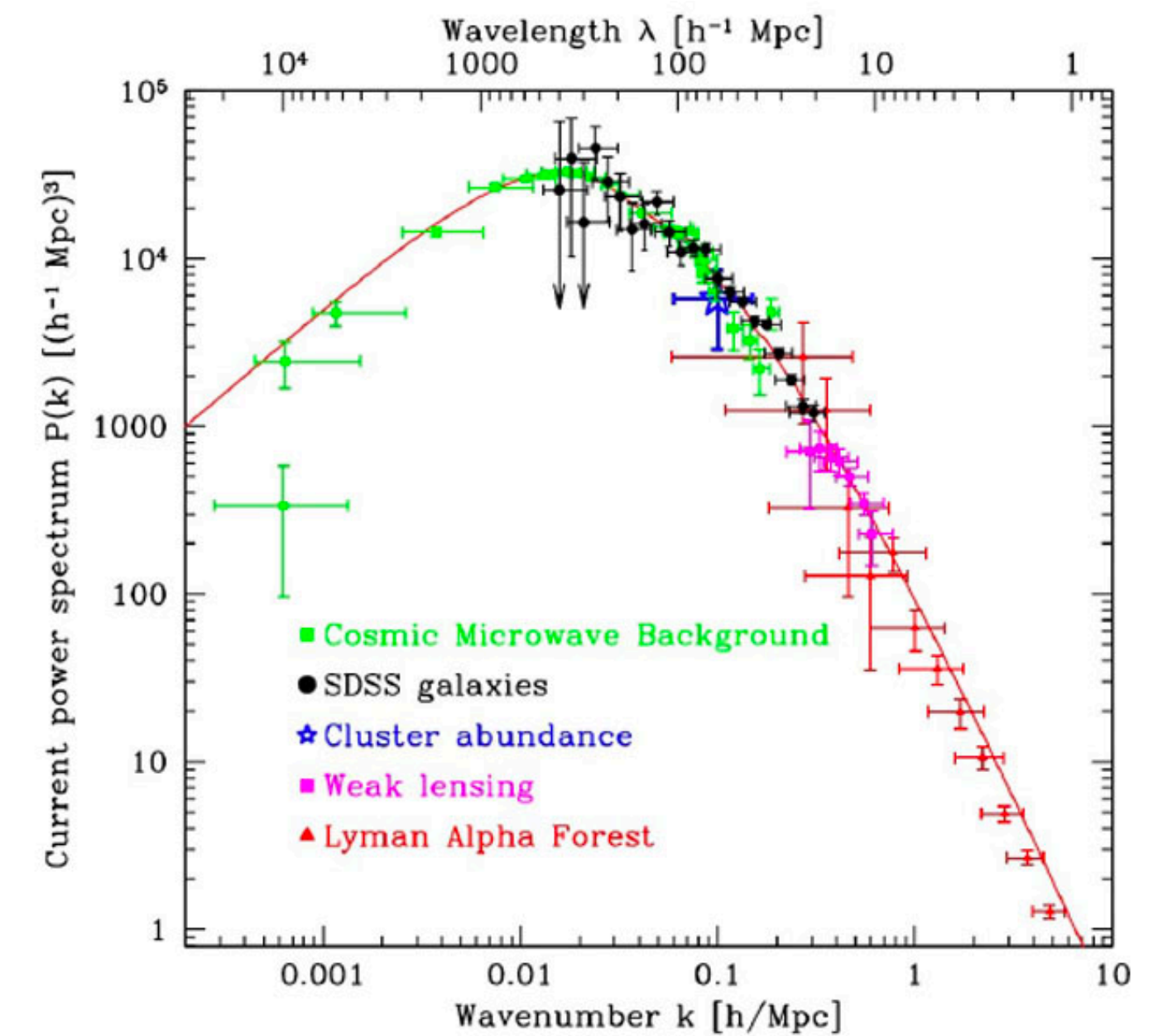


DM: cold dark matter (CDM) fluid

Λ CDM
simple but exotic model!

Cold dark matter

- **Cold:** moves much slower than c
- **Pressureless:** gravitational attractive, clusters
- **Dark** (transparent): no/weakly electromagnetic interaction
- **Collisionless:** no/weakly self-interaction or interaction with baryons
- **Abundance:** amount of dark matter today known



What we *don't* know

- What is DM? Nature

- ~~Cold~~ →

How cold it is?

WDM

- ~~Pressureless~~ →

Cluster on all scales?

- ~~Dark~~ →

Non-gravitational interaction?

Milicharged DM

- ~~Collisionless~~ →

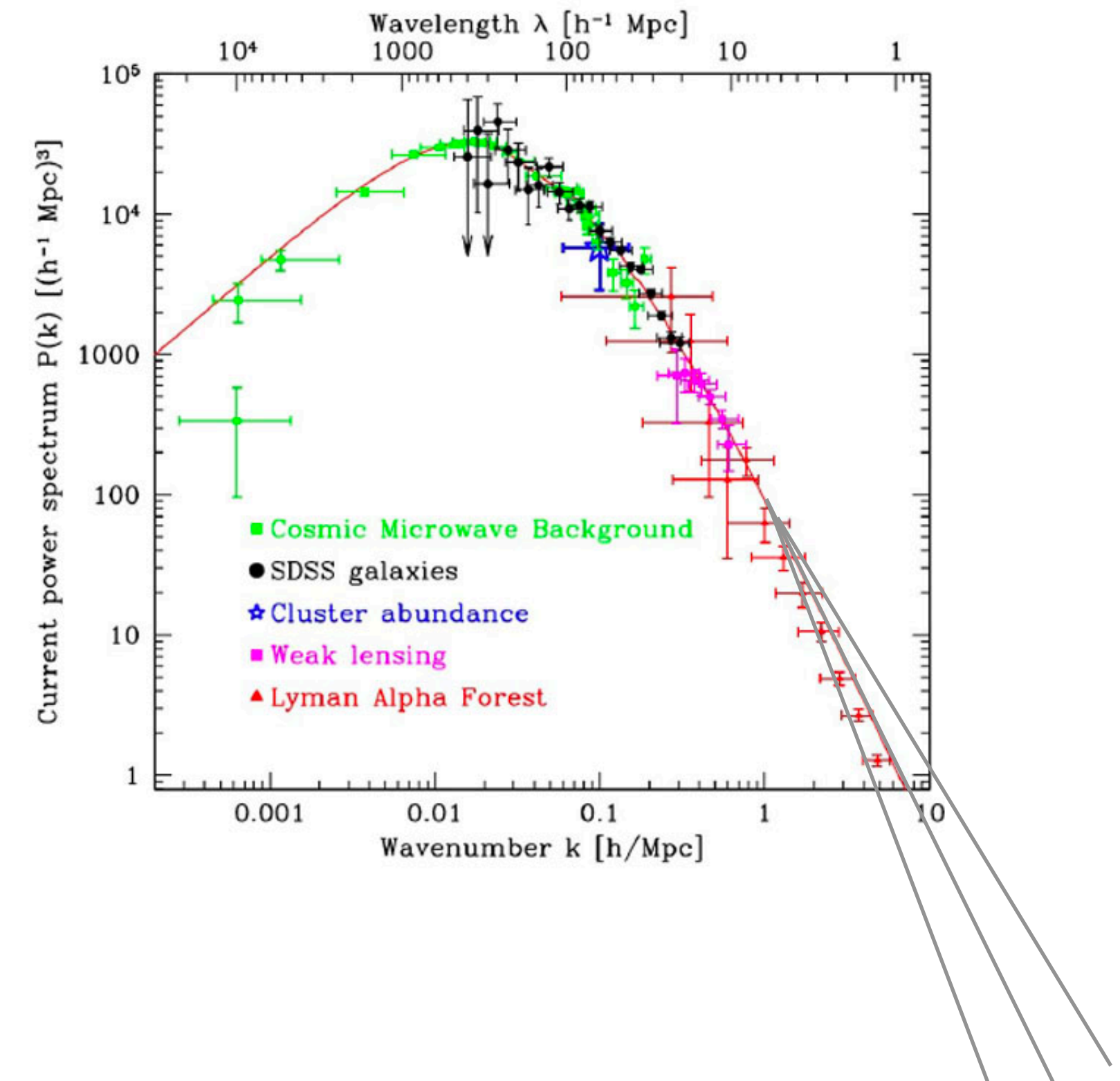
How small self-interaction?

SIDM

Although still behaves like CDM on large scales

Small scale behaviour: still “weakly” constrained and small scale challenges

Small scale curiosities: **cusp-core**, missing satellites, BTFR, ...



What we *don't* know

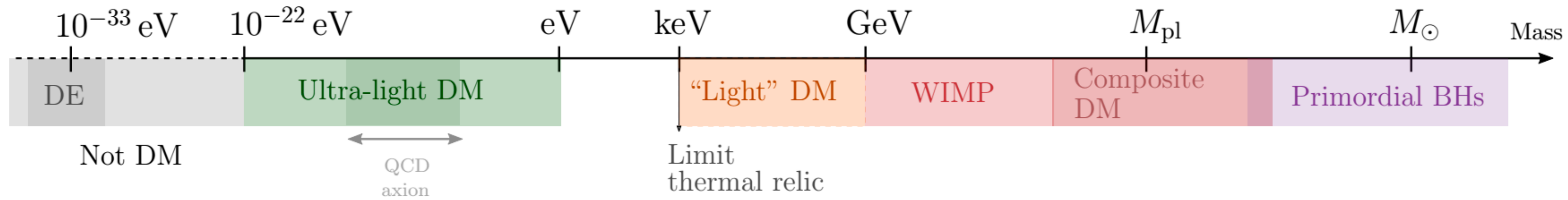
- What is DM? What is the nature of DM?

State of the “art”

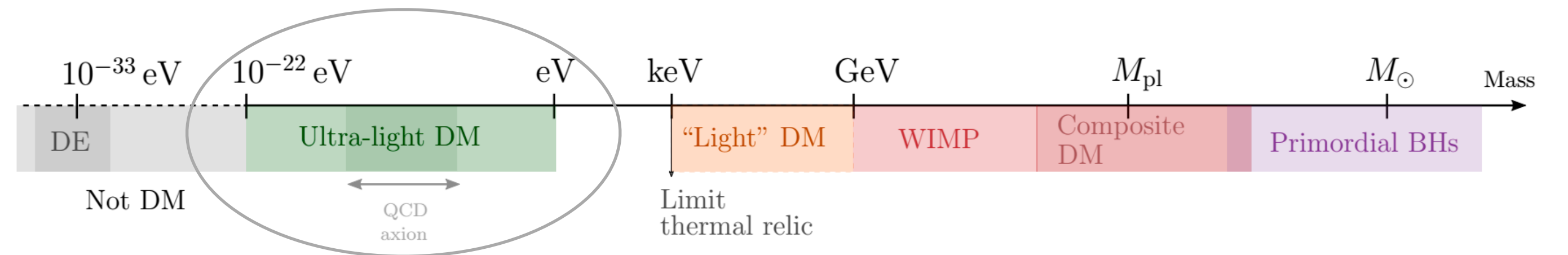


Mass scale of DM

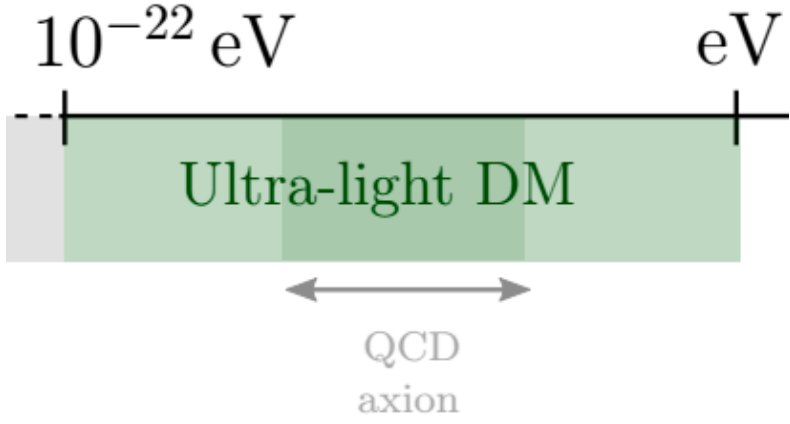
80 orders of magnitude



Ultra-light dark matter

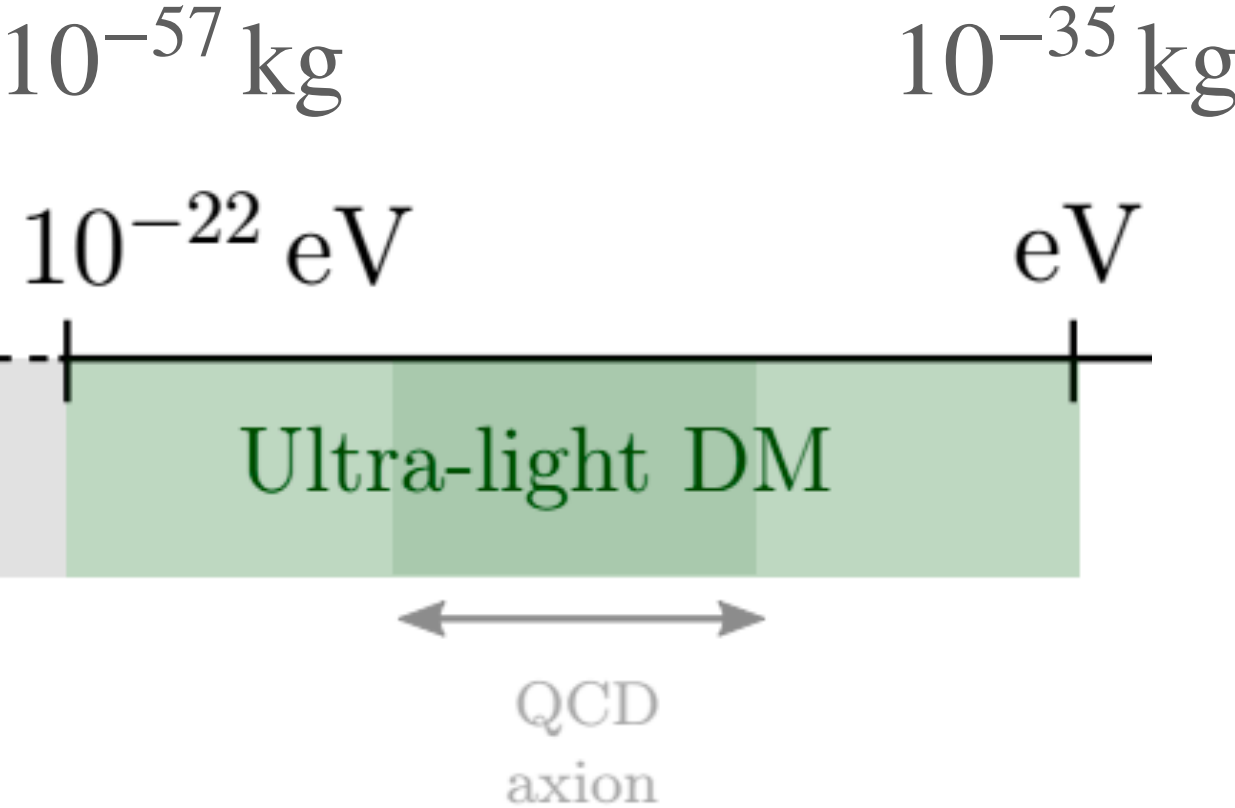
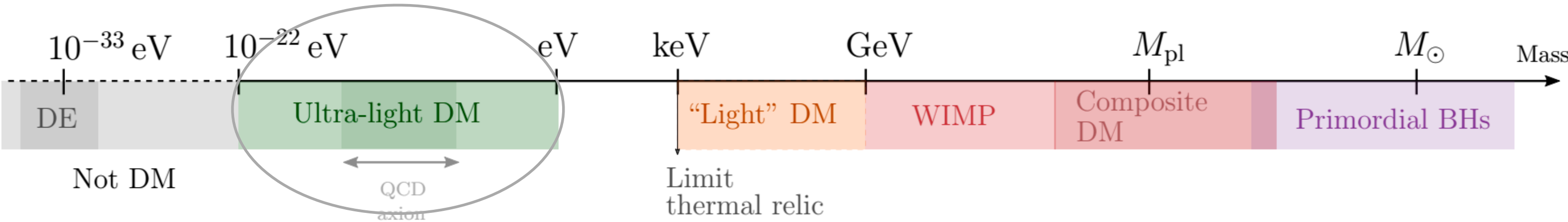


Ultra-light Dark Matter



Ultra-light candidate, cold \longrightarrow Large $\lambda_{\text{dB}} \sim 1/mv$

Lightest possible candidate for DM



\longrightarrow

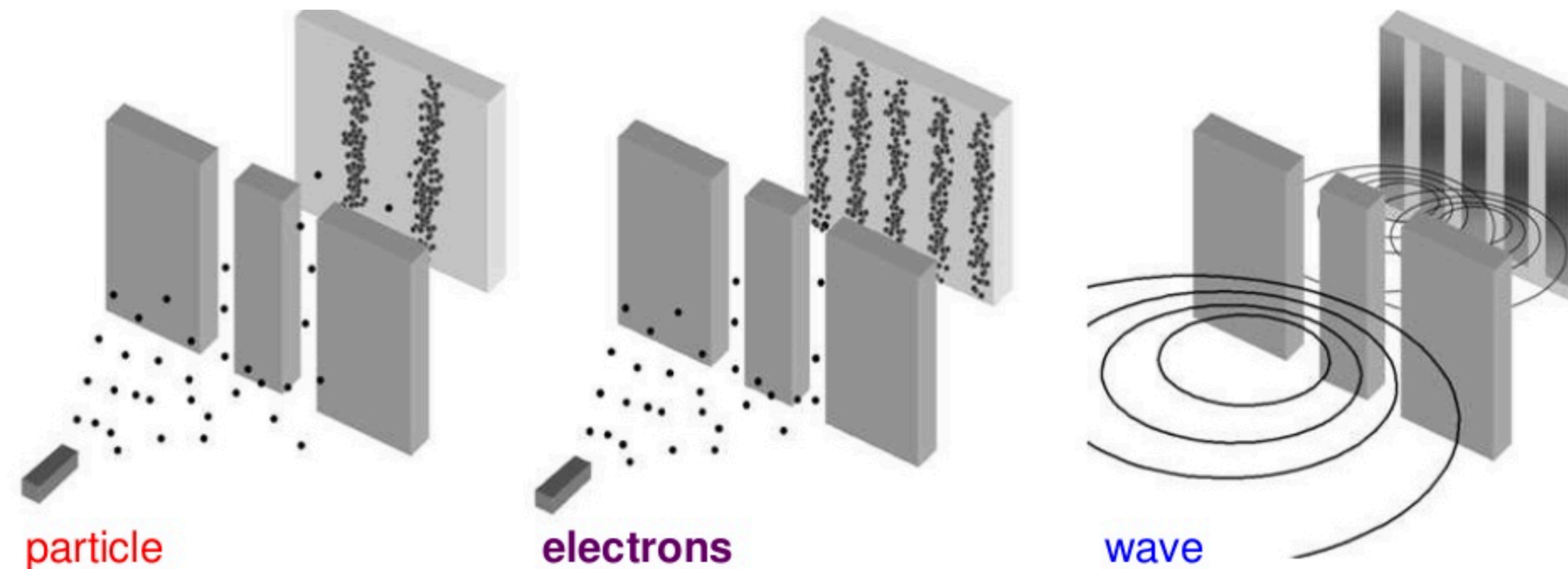
Bosons

Non-thermally produced

Wave-Particle duality

All matter exhibits a wave behaviour

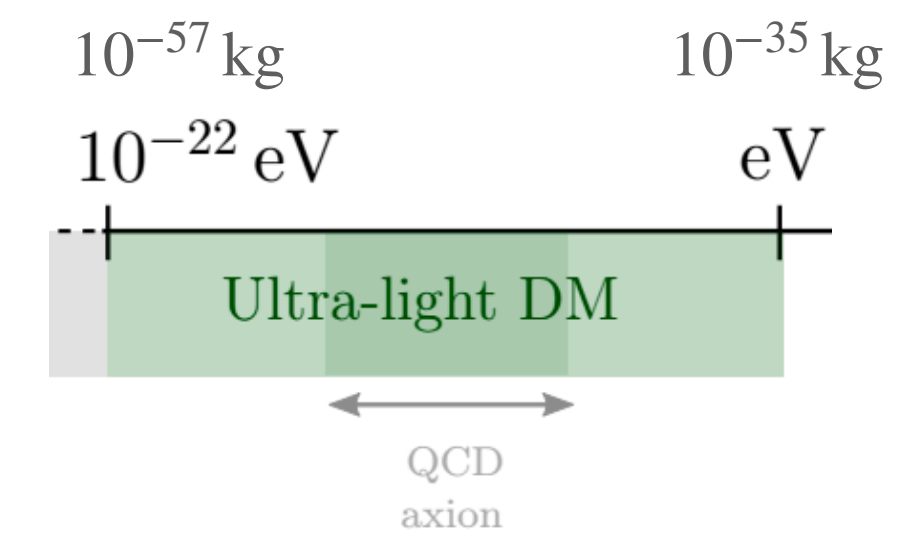
De Broglie 1924



$$\lambda_{dB} \sim \frac{1}{mv}$$

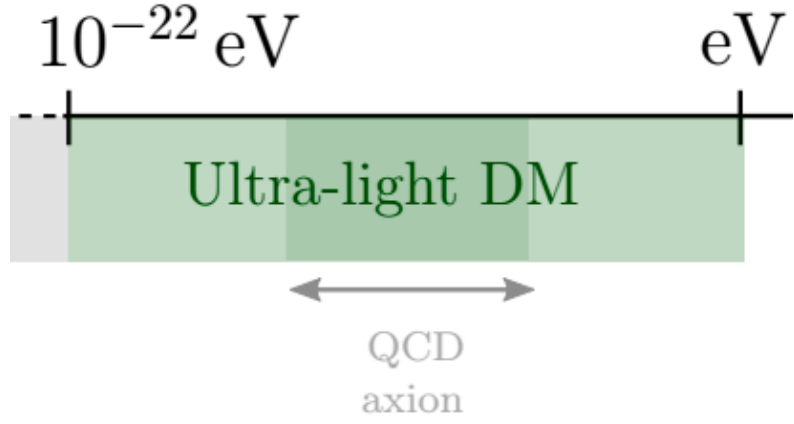
$$\lambda_{dB} \sim 1/\sqrt{2\pi mk_B T}$$

	Mass (kg)	Speed (m/s)	λ_{dB} (m)
Accelerated e-	9.1×10^{-31}	5.9×10^6	1.2×10^{-10}
Golf ball	0.045	220	4.8×10^{-30}



$$\lambda_{dB}^{ULDM} \sim \text{pc} - \text{kpc}$$

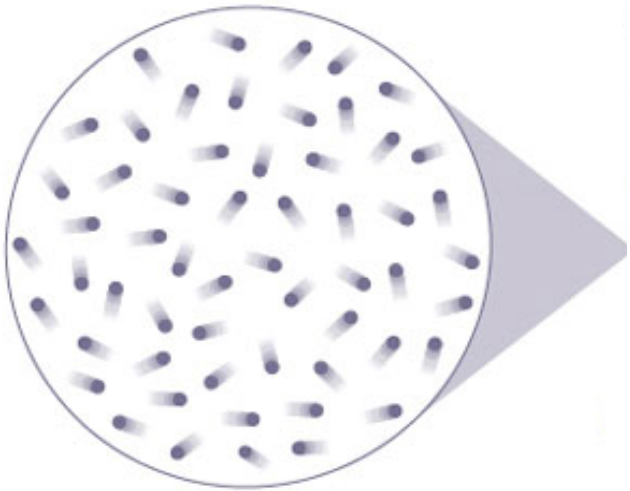
Ultra-light Dark Matter



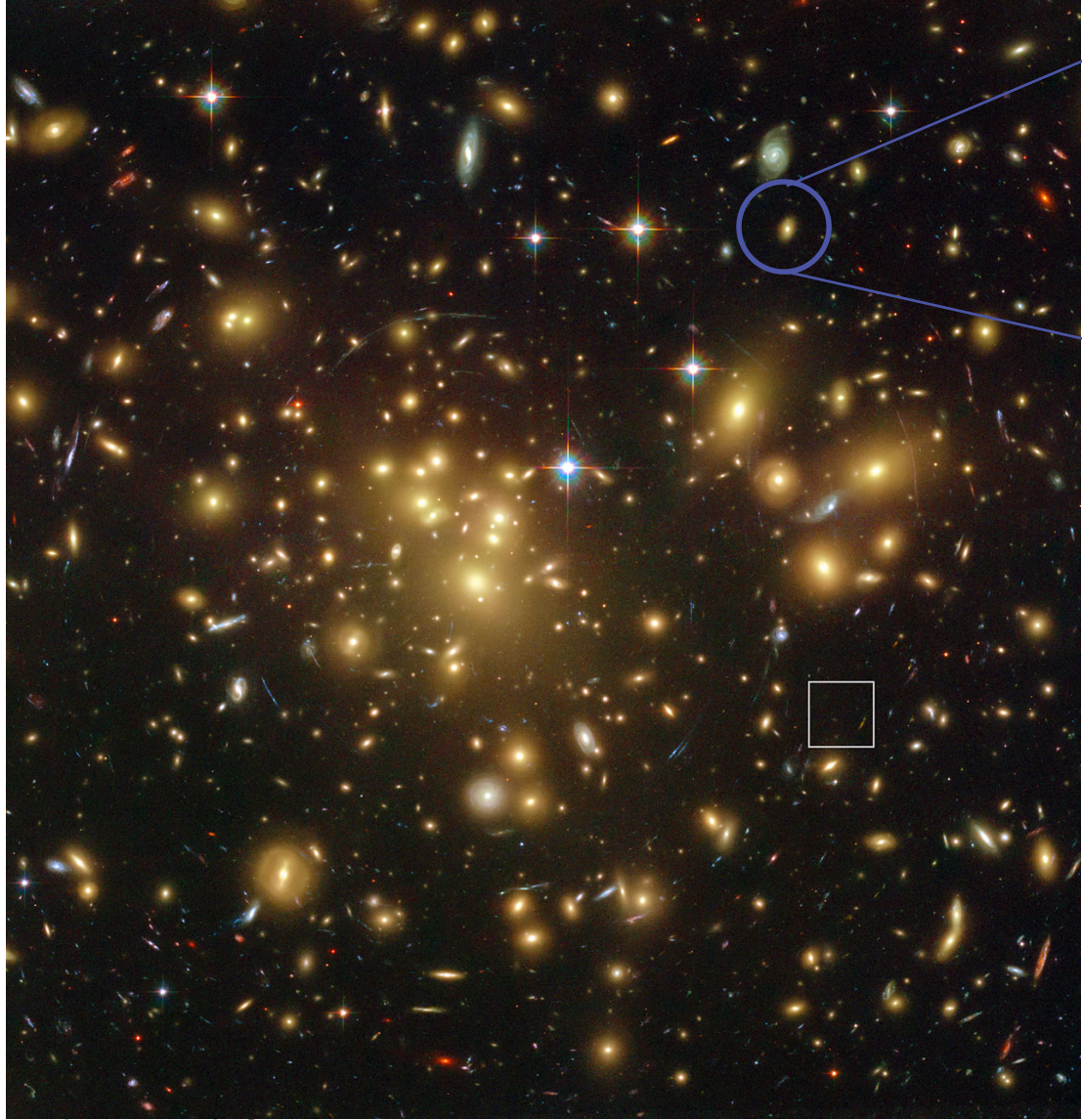
Ultra-light candidate \longrightarrow Large $\lambda_{dB} \sim 1/mv$

Lightest possible candidate for DM

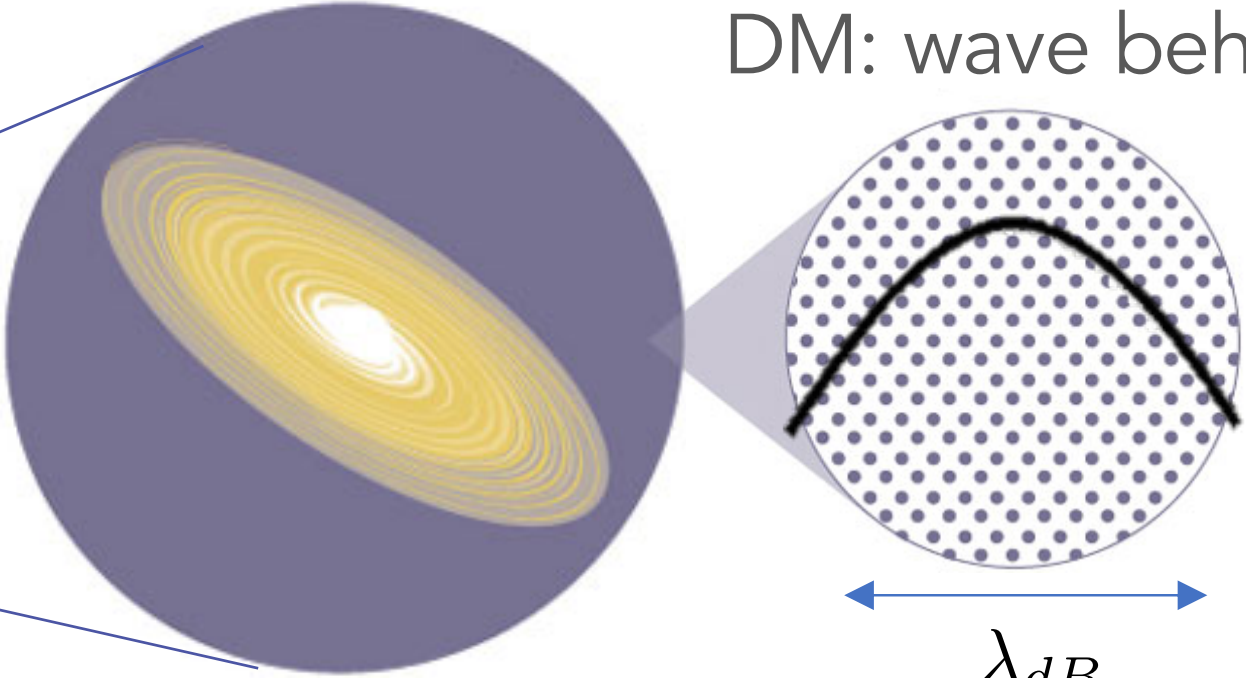
Large scales:
DM behaves like standard particle DM (**CDM**).



DM: particles
 $d \gg \lambda_{dB}$



Adapted from Quanta



Galaxy halo

DM: wave behaviour

λ_{dB}
 $d \ll \lambda_{dB}$

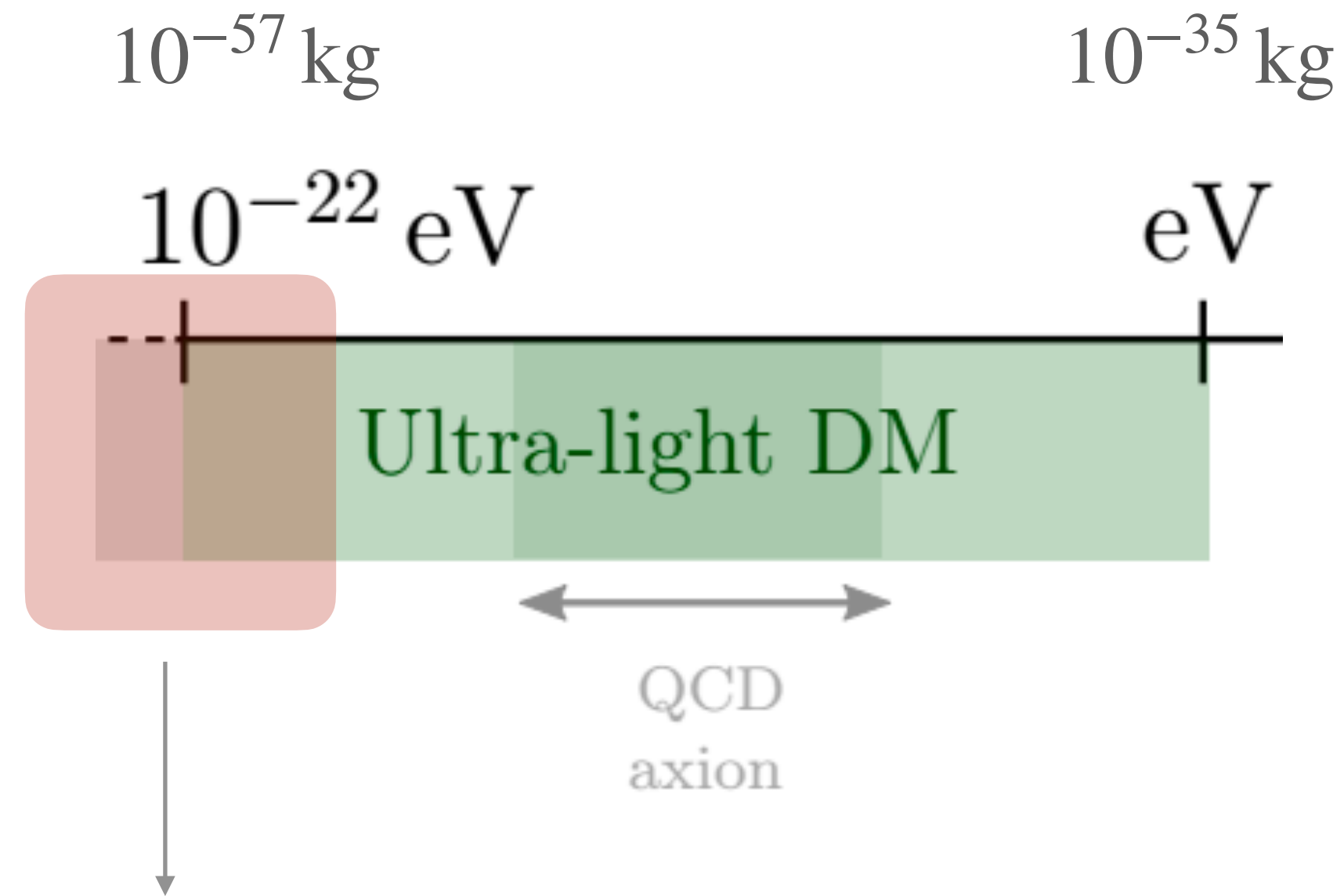
Small scales:
DM behaves like a **wave**

$$10^{-25} \text{ eV} \lesssim m \lesssim \text{eV}$$

$$\lambda_{dB}^{ULDM} \sim \text{pc} - \text{kpc}$$

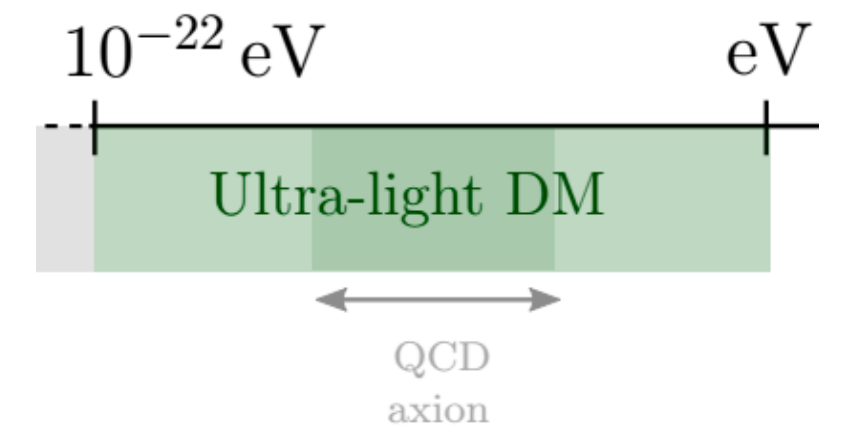
Ultra-light Dark Matter

Ultra-light candidate, cold \longrightarrow Large $\lambda_{\text{dB}} \sim 1/mv$



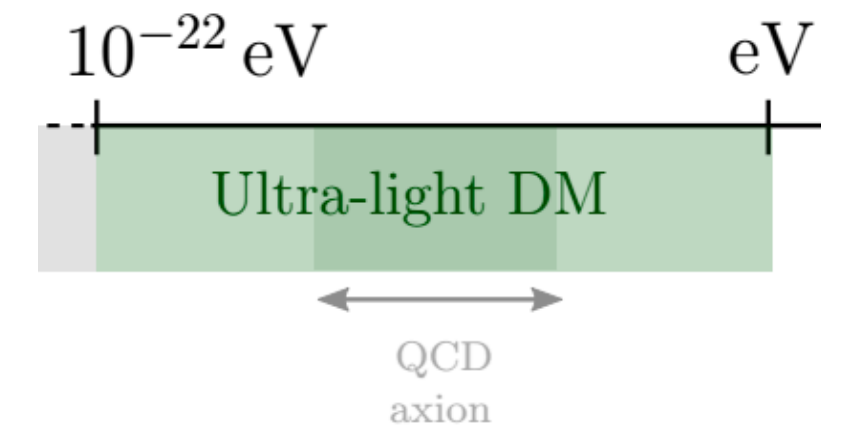
Gravitational probes

$$10^{-24} \text{ eV} \lesssim m_{\text{fdm}} \lesssim 10^{-18} \text{ eV}$$

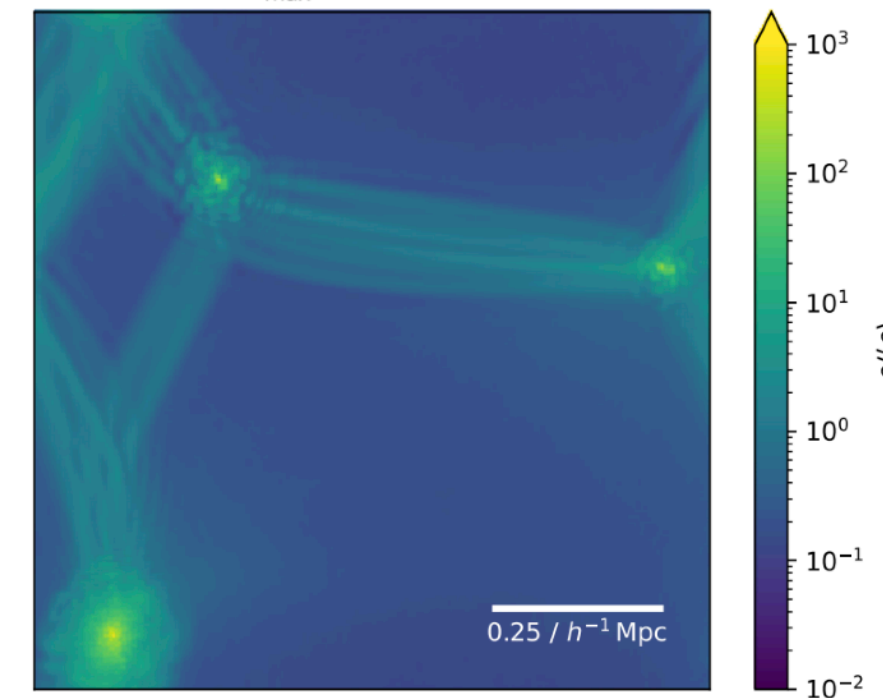


Motivations of the ULDM

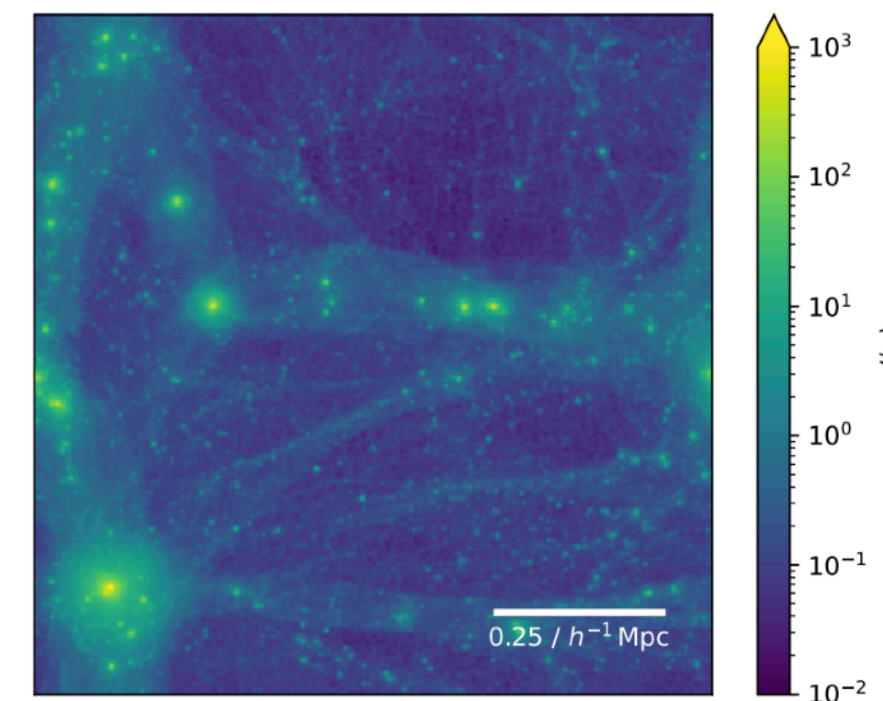
- **Rich phenomenology on small scales:**
 - **Wave** nature manifest on galactic scales
- Particle physics/HEP/condensed matter motivation
 - Candidates: Axions, ALPs, UL particles, ...*
- Might address small scales problems



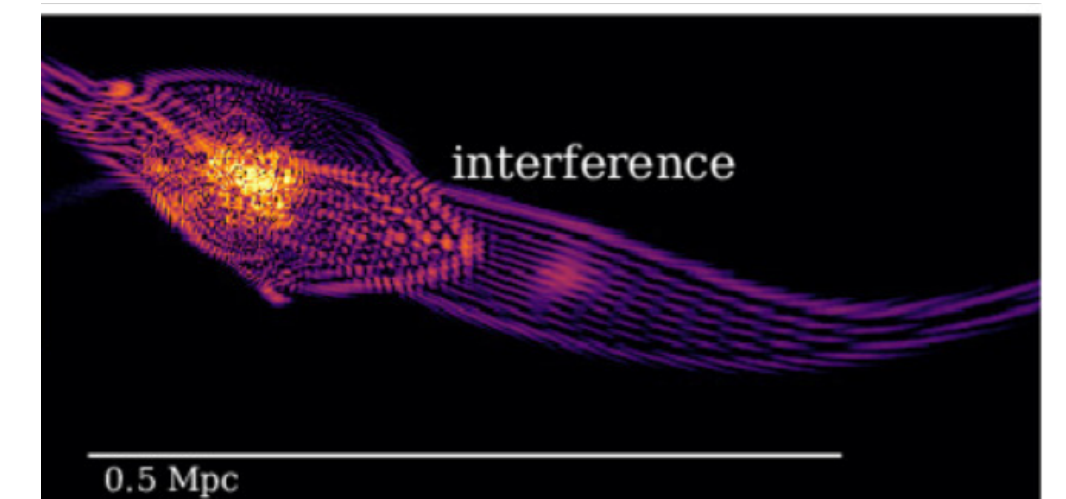
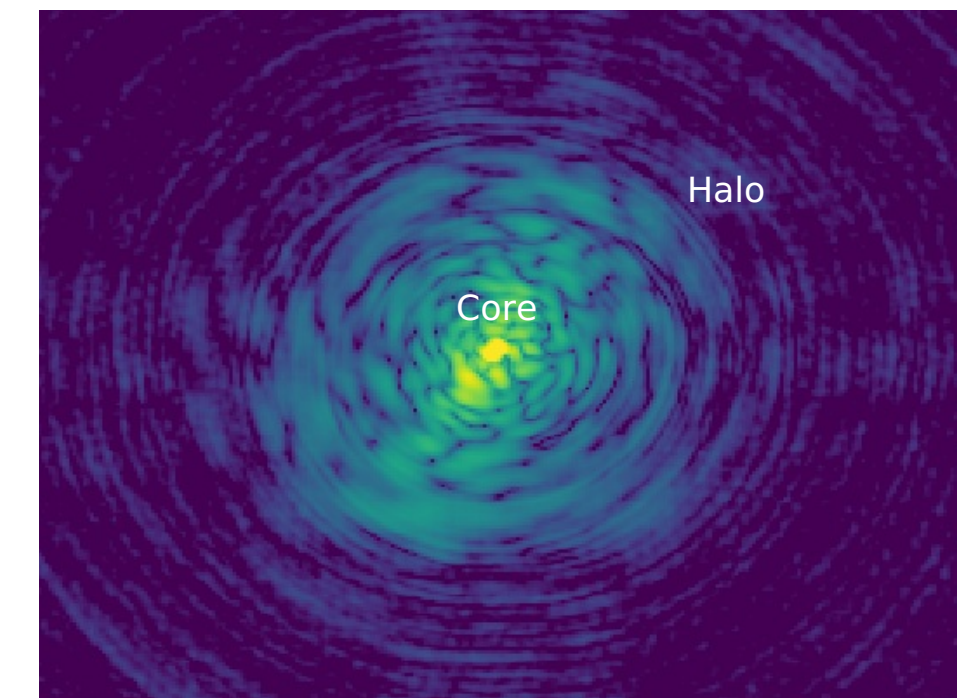
FDM: 256^3 , $mc^2 = 1.75 \times 10^{-23}$ eV, $z = 0.00$
 $v_{\max} = 88.1$ km/s



CDM: 256^3 , $z = 0.00$

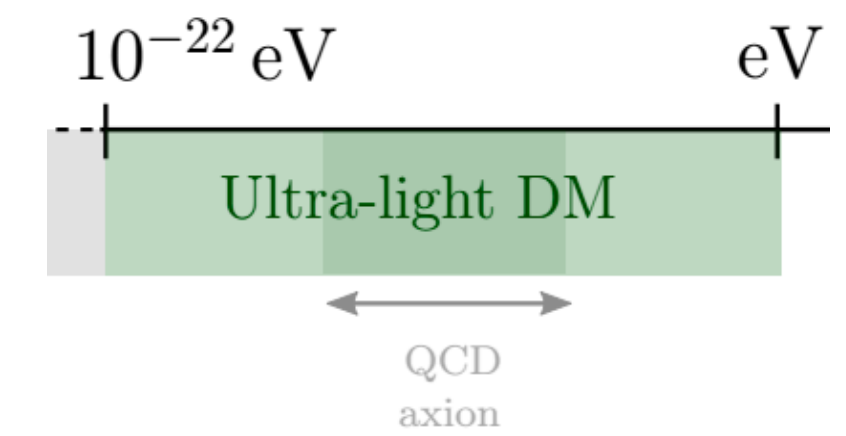


S. May et al. 2021

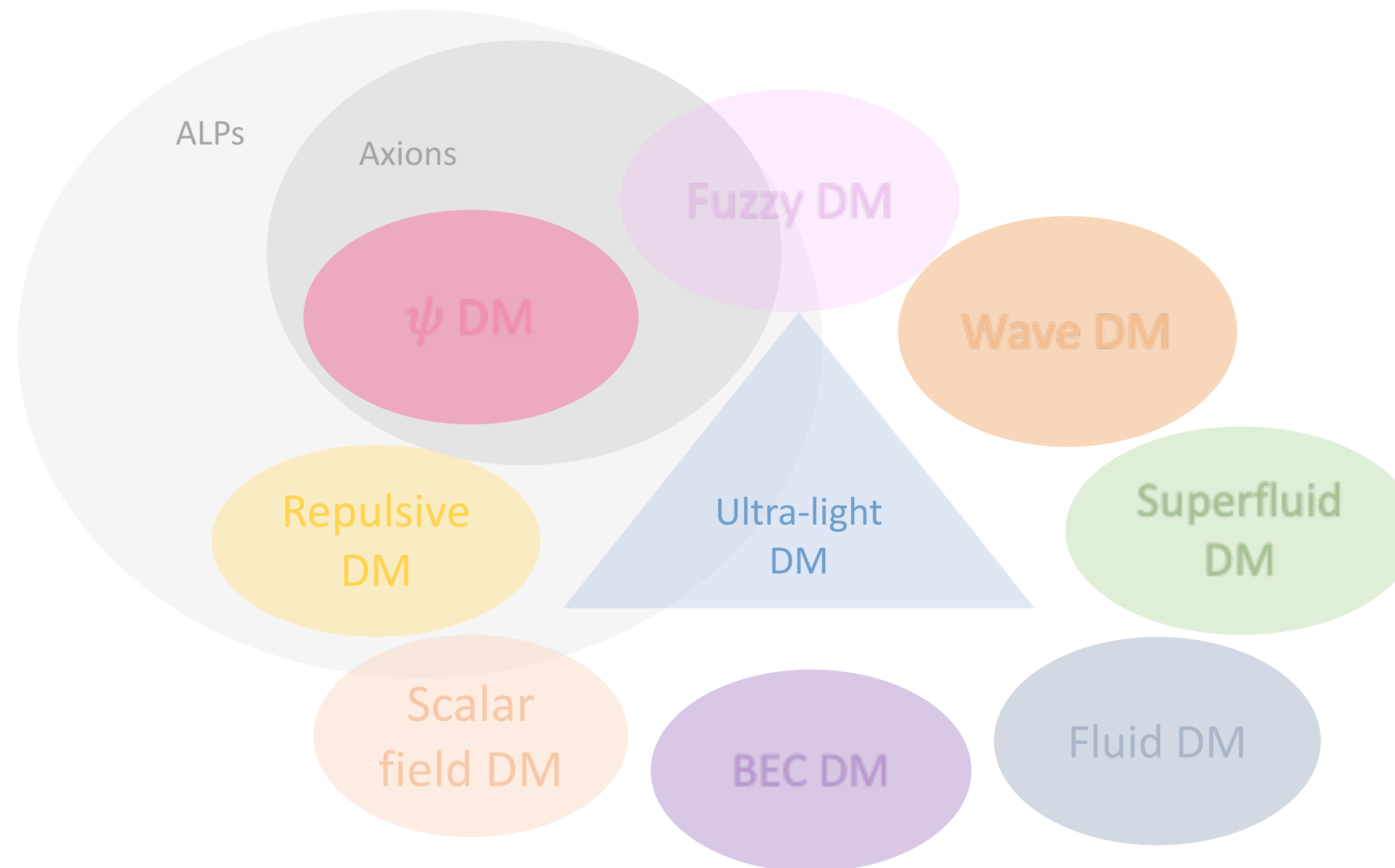


Mocz et al. 2017

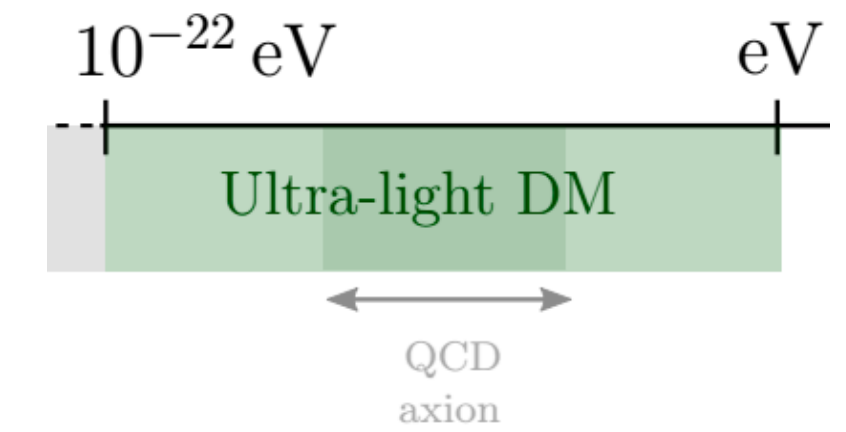
Ultra-light Dark Matter - models



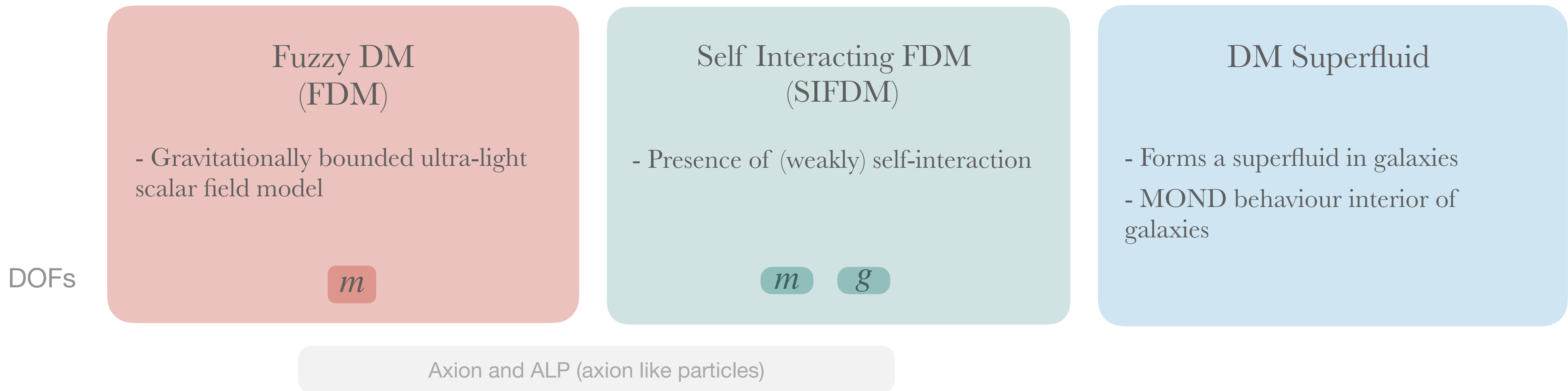
There are many ways to have a DM with this property \rightarrow many ULDM models in the literature
However, each of these models presents a different dynamics on small scales - different **phenomenology**



Ultra-light Dark Matter -classes



3 classes:



$$i\dot{\psi} = \left(-\frac{1}{2m} \nabla^2 + \frac{g}{8m^2} |\psi|^2 - m\Phi \right) \psi$$

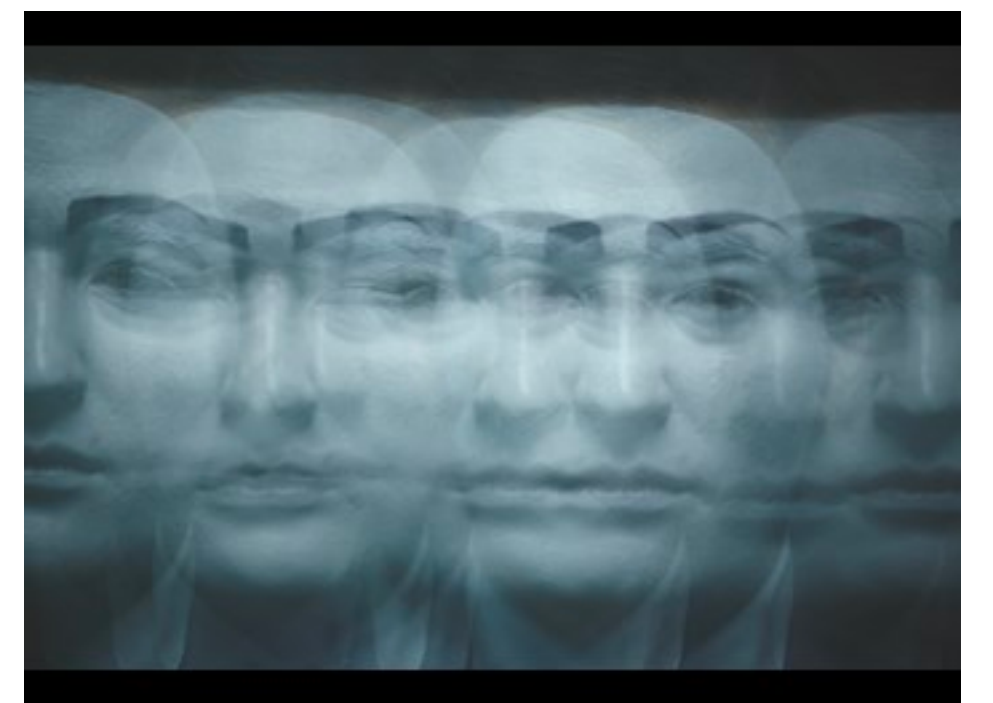
$$\mathcal{L} = P(X)$$

→ Connection with condensed matter and particle physics!

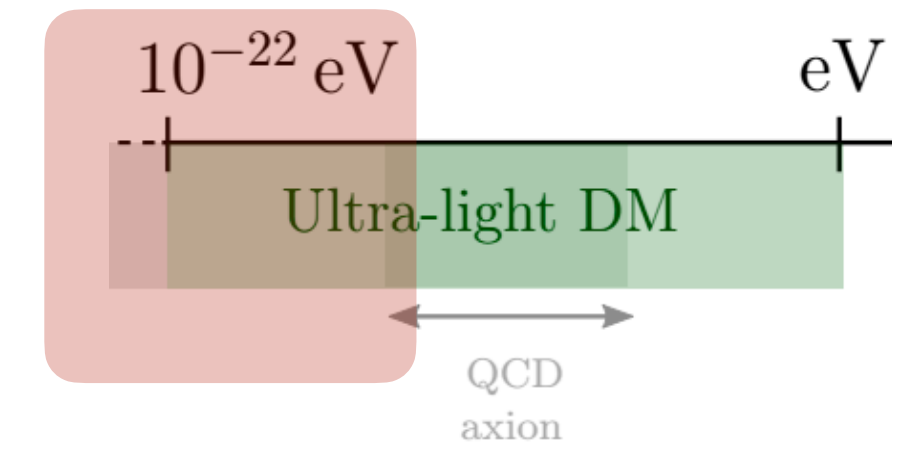
“Ultra-light dark matter”, **E.Ferreira**, 2020. *The Astronomy and Astrophysics Review*.

Fuzzy dark matter

Self interacting fuzzy dark matter



Fuzzy dark matter



Fuzzy DM (FDM)

- Gravitationally bounded ultra-light scalar field model

m

Wave DM Ultra-light axions

Self Interacting FDM (SIFDM)

- Presence of (weakly) self-interaction

m

g

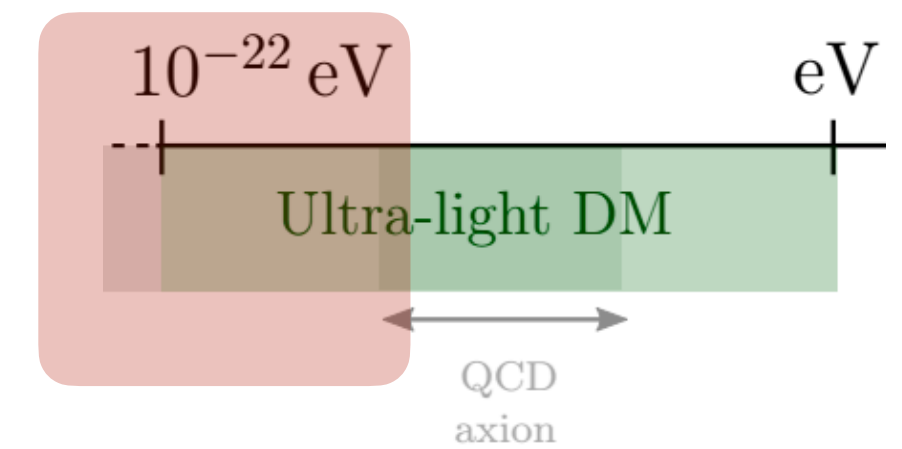
Hu W, Barkana R, Gruzinov A (2000 a,b)
(Reviews: EF (2021), J. Niemeyer (2019), L. Hui (2021))

Idea:

$$m_{\text{fdm}} \sim 10^{-22} \text{ eV}$$

address the small scale problems+ rich phenom.

Fuzzy dark matter



Fuzzy DM (FDM)

- Gravitationally bounded ultra-light scalar field model

m

Wave DM Ultra-light axions

Focus in spin 0 particles here!

(Some of the grav. phenom. is carried for vectors, for example)

Hu W, Barkana R, Gruzinov A (2000 a,b)
(Reviews: *EF (2021)*, *J. Niemeyer (2019)*, *L. Hui (2021)*)

Idea:

$$m_{\text{fdm}} \sim 10^{-22} \text{ eV}$$

address the small scale problems+ rich phenom.

Motivation: particle physics

FDM candidates

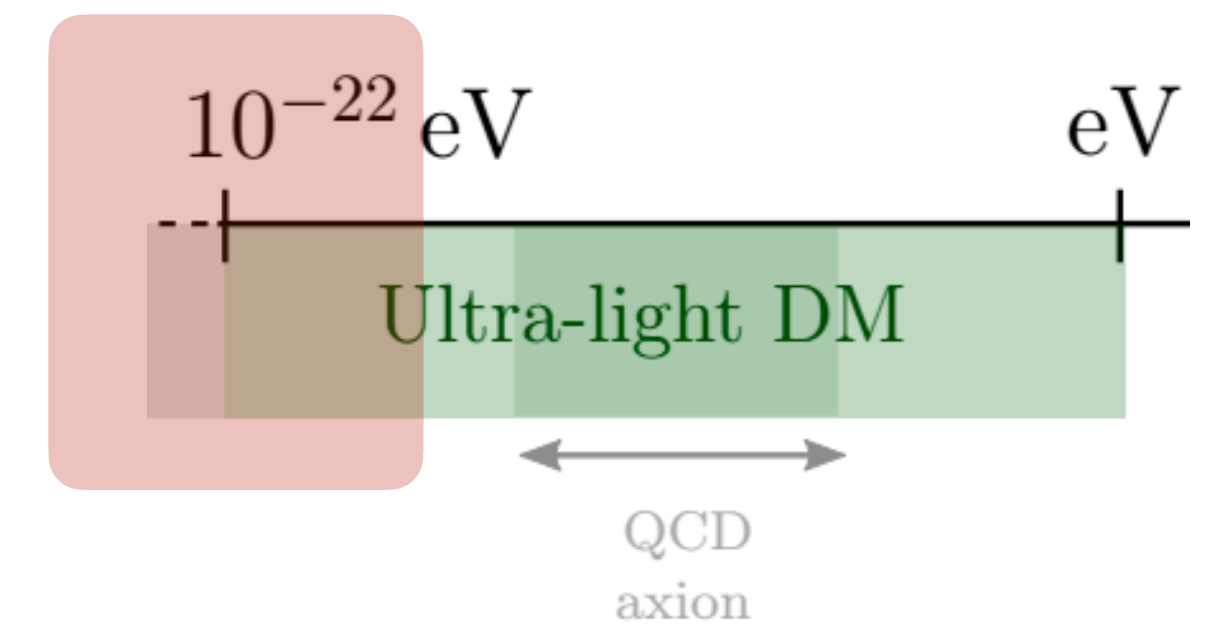
- Natural candidate for a light scalar field is a pseudo-Nambu Goldstone boson

Known PNGB: QCD axion

(Peccei and Quinn 1977; Weinberg 1978; Wilczek 1978)

Axion-like particles

→ Candidate for DM



Axions or Axion like particles (ALP)

Axions and ALPs are pseudo Nambu Goldstone bosons from the spontaneous symmetry breaking of a $U_{PQ}(1)$ ($U(1)$) symmetry, and are described by the complex field: $\Psi = v e^{i\phi/f_a}$

$$v_{0,ssb} = f_a/\sqrt{2} \quad \longrightarrow \quad \phi \rightarrow \phi + c$$

Non-perturbative effects (from string theory or instantons) induce a potential:

$$V(\phi) = \Lambda_a^4 [1 - \cos(\phi/f_a)] \xrightarrow{\phi \ll f_a} \frac{1}{2} m^2 \phi^2 + \frac{g}{4} \phi^4 + \dots$$

Motivation: particle physics

FDM candidates

- Natural candidate for a light scalar field is a pseudo-Nambu Goldstone boson

Known PNGB: QCD axion

(Peccei and Quinn 1977; Weinberg 1978; Wilczek 1978)

Candidate for DM

Axion-like particles or ultra-light axions:

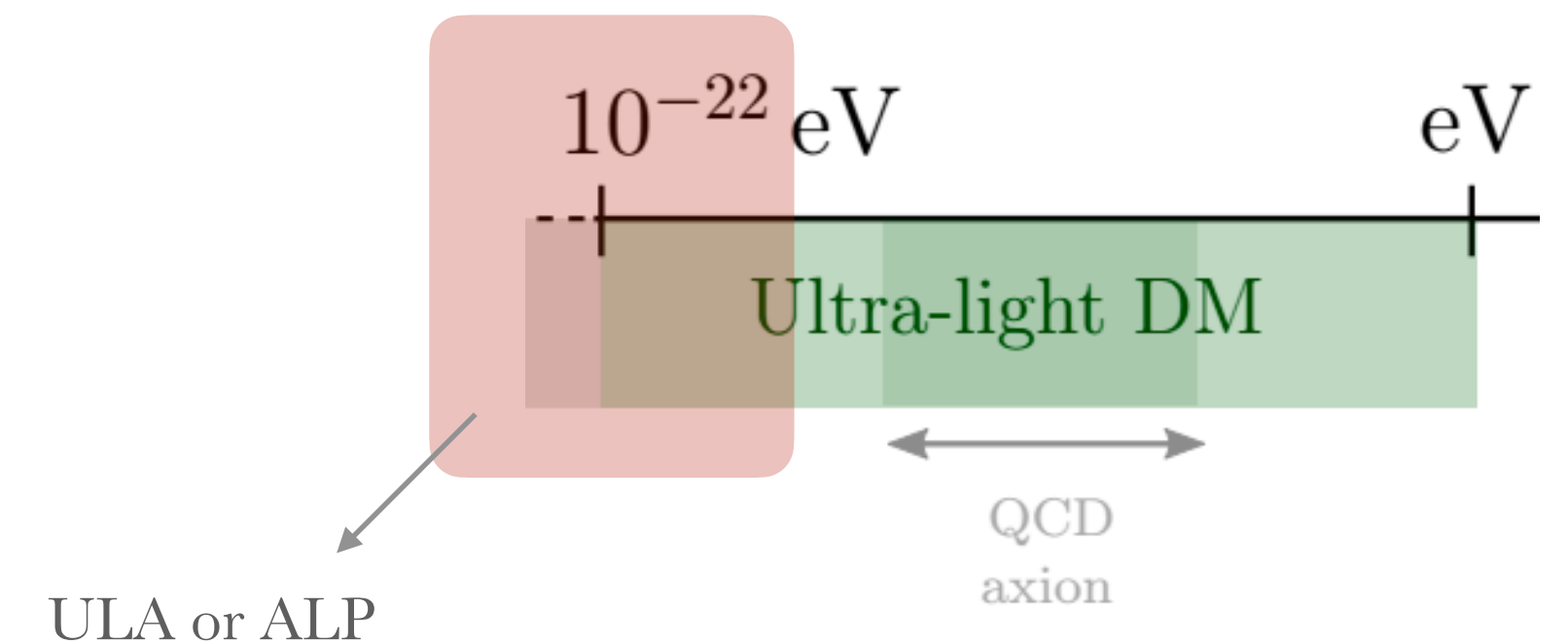
- ALPs expected in string theory (Arvanitaki et al., Svrcek, Witten)
- Can generate PNGB that are ultra-light

- Formation mechanism: needs to have a relic abundance that gives the correct DM abundance

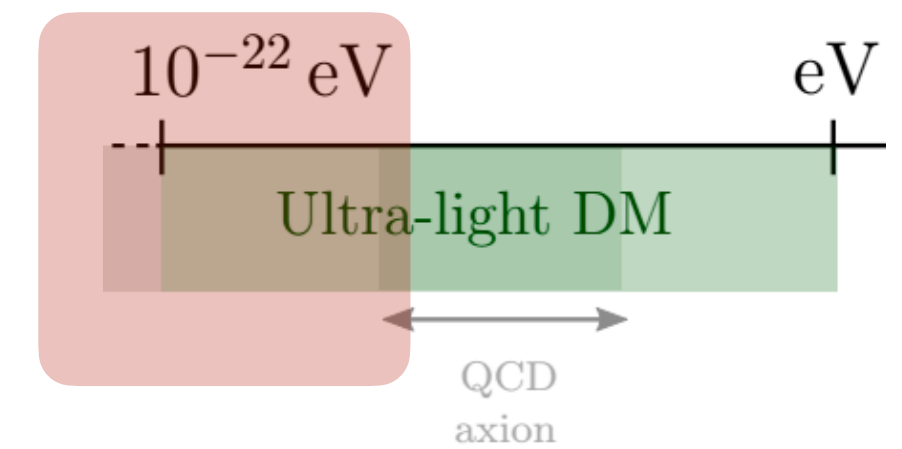
Non-thermal mechanism (e.g. mis-alignment)

$$\Omega_{\text{matter}} \sim 0.1 \left(\frac{f_a}{10^{17} \text{ GeV}} \right)^2 \left(\frac{m}{10^{-22} \text{ eV}} \right)$$

* Axion and ALP interact with **photons** (and neutrinos)

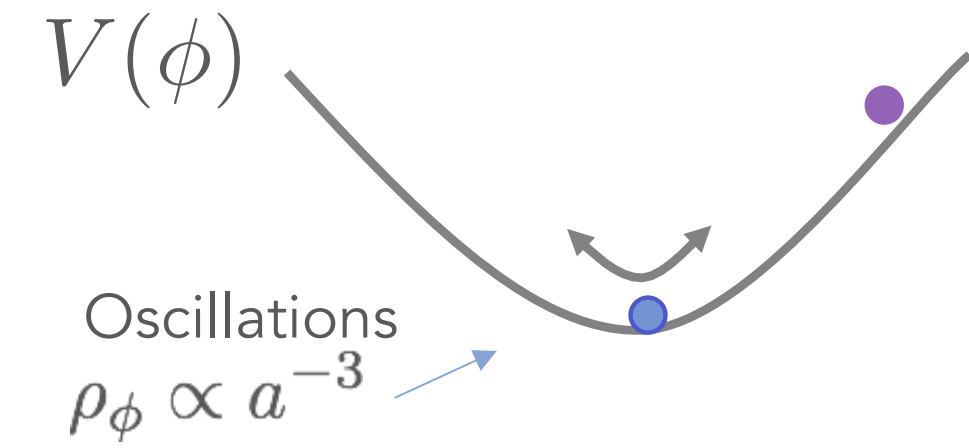


Cosmological evolution



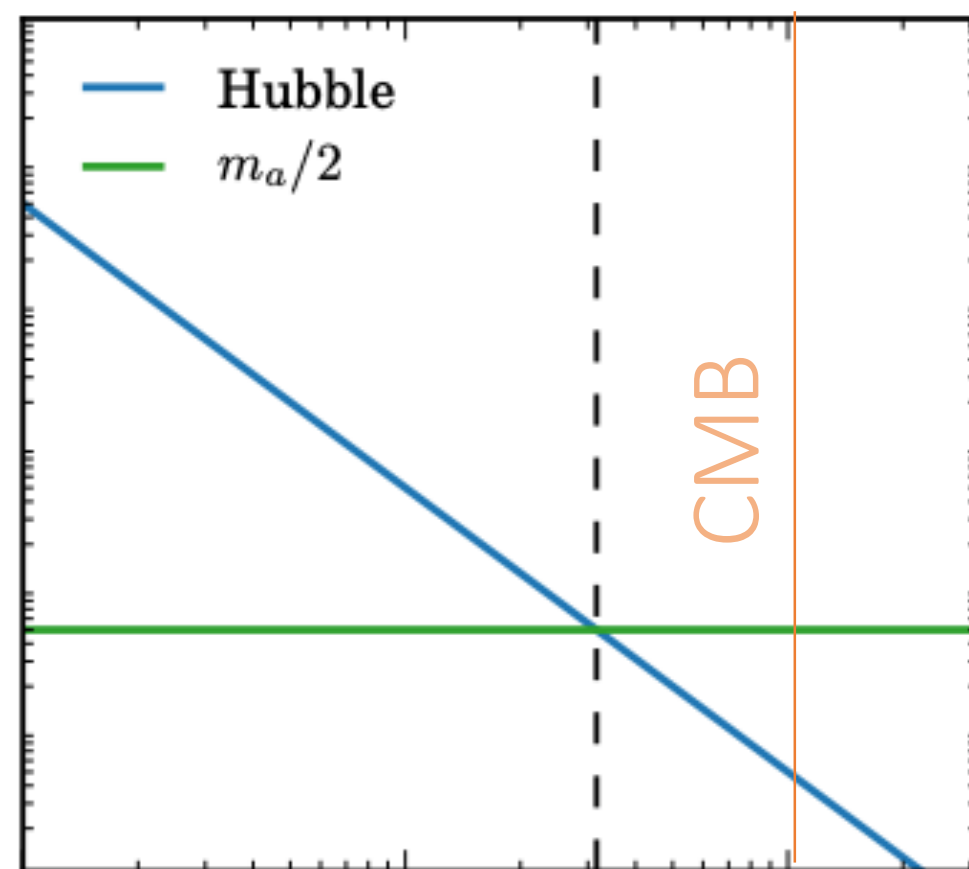
$$\ddot{\phi} + 3H\dot{\phi} + m^2\phi = 0$$

FDM

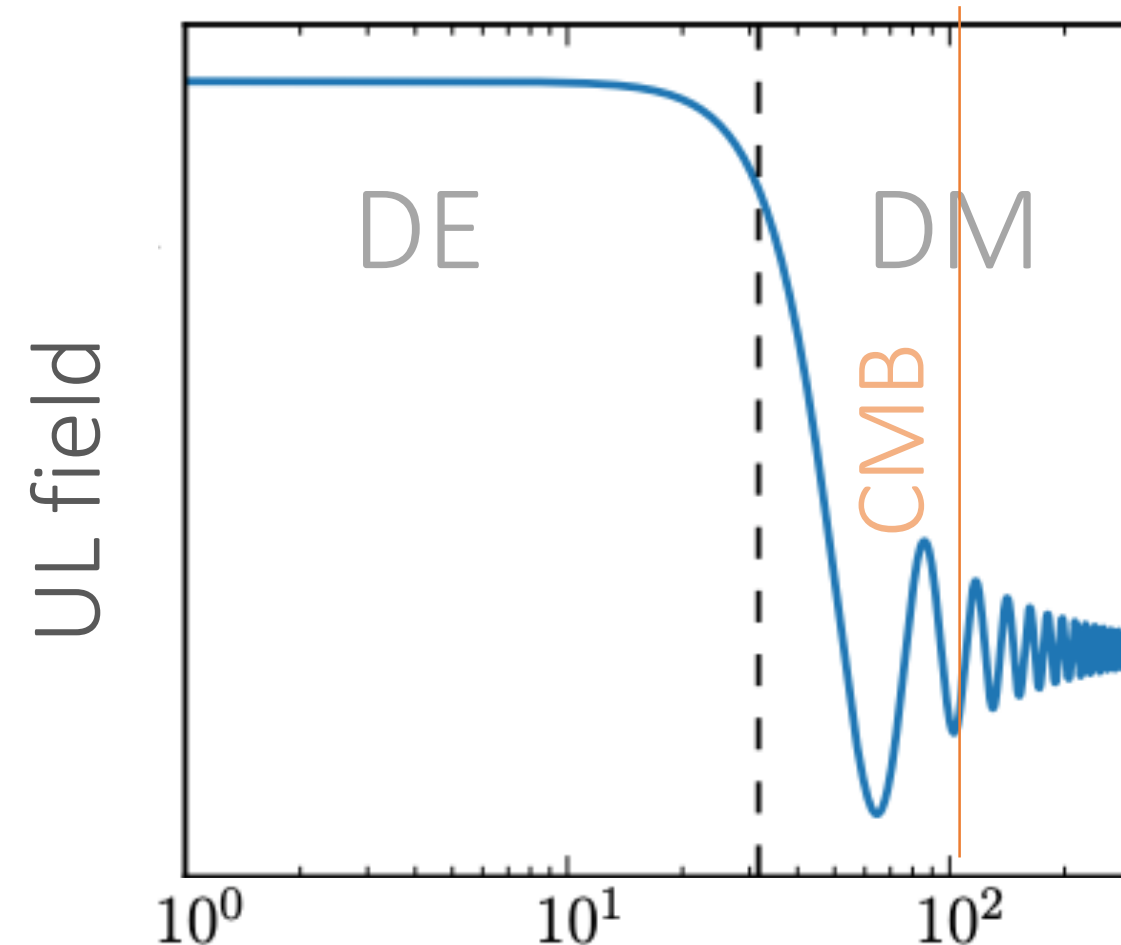


$H \gg m \implies \phi_{\text{early}} = \phi(t_i) \longrightarrow \omega = -1$ DE
 $H \ll m \implies \phi_{\text{late}} \propto e^{imt} \longrightarrow \langle \omega \rangle = 0$ DM

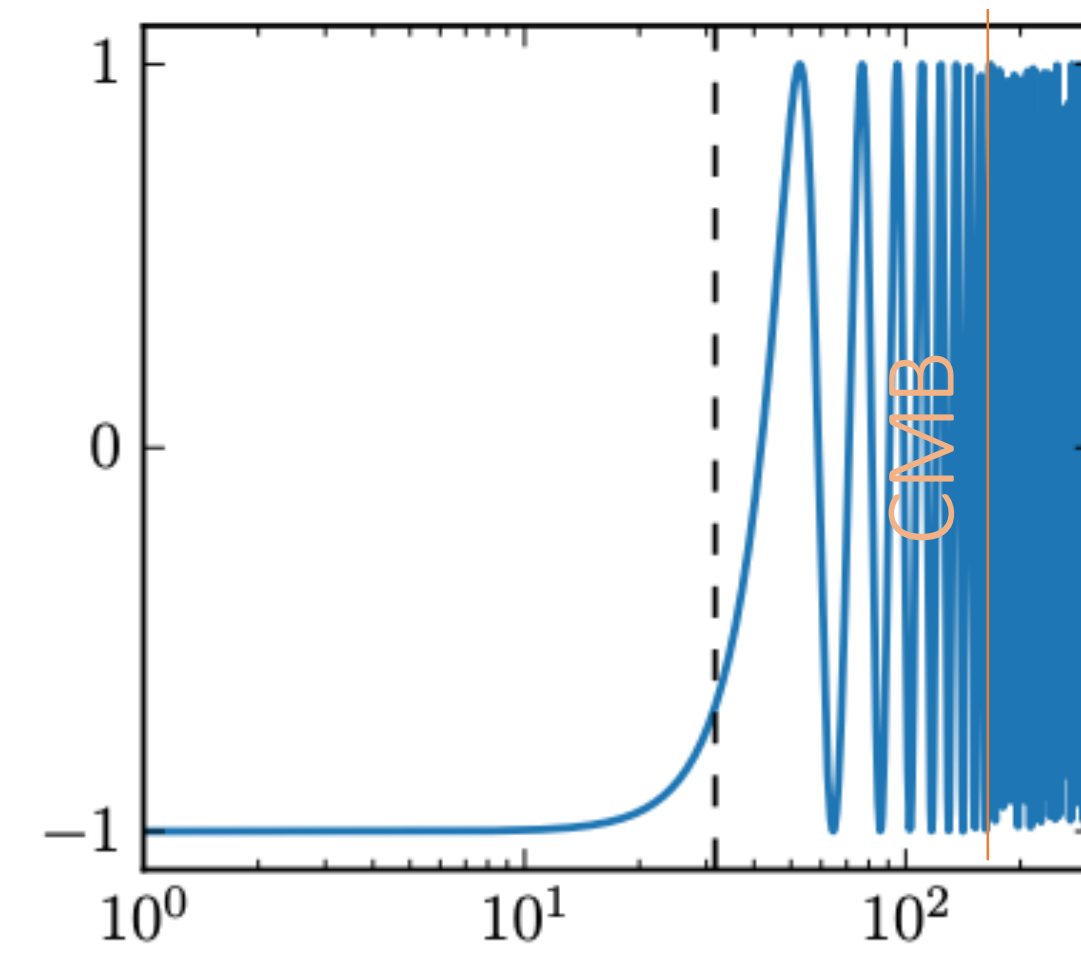
$H(t_*) = m$



Scale factor $a(t)$



Scale factor $a(t)$

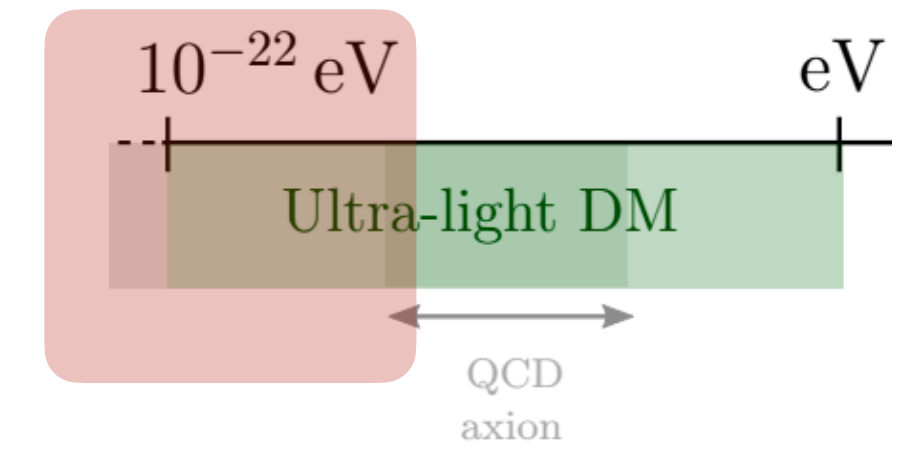


Scale factor $a(t)$

Marsh, 2016

In order to **behave like DM**: start oscillating before matter-radiation equality $m > 10^{-28} \text{ eV} \sim H(a_{\text{eq}})$

Structure formation - *non-relativistic regime*



Evolution on small scales: take non-relativistic regime of the theory, relevant for structure formation.

Schrödinger-Poisson system : describe the FDM and the SIFDM

$$\left\{ \begin{array}{l} i\dot{\psi} = \left(-\frac{1}{2m}\nabla^2 + \frac{g}{8m^2}|\psi|^2 - m\Phi \right) \psi \\ \nabla^2\Phi = 4\pi G(m|\psi|^2 - \bar{\rho}) \end{array} \right.$$

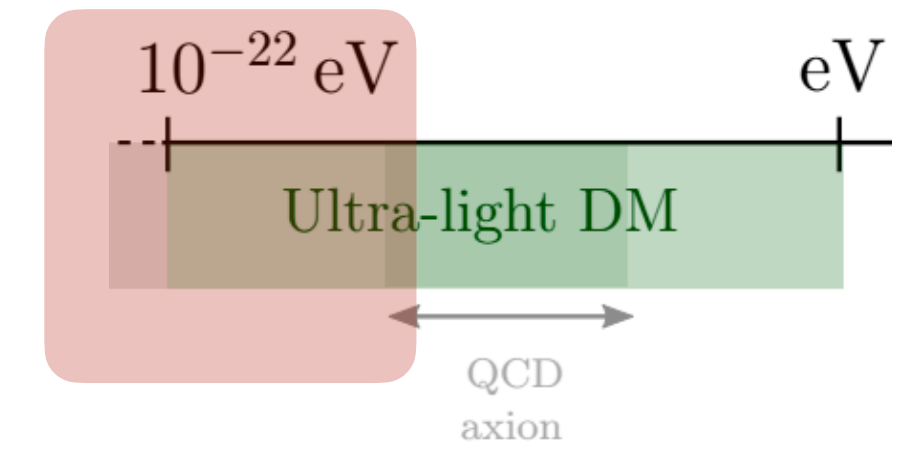
Schrödinger equation
(Gross-Pitaevskii)

Poisson equation

$g = 0 \longrightarrow$ FDM
 $g \neq 0 \longrightarrow$ SIFDM

Fundamentally different than
CDM/WDM/SIDM!

Structure formation - *non-relativistic regime*



Evolution on small scales: take non-relativistic regime of the theory, relevant for structure formation.

Schrödinger-Poisson system : describe the FDM and the SIFDM

$$\left\{ \begin{array}{l} i\dot{\psi} = \left(-\frac{1}{2m}\nabla^2 + \frac{g}{8m^2}|\psi|^2 - m\Phi \right) \psi \\ \nabla^2\Phi = 4\pi G(m|\psi|^2 - \bar{\rho}) \end{array} \right.$$

Schrödinger equation
(Gross-Pitaevskii)

Poisson equation

$g = 0 \longrightarrow$ FDM
 $g \neq 0 \longrightarrow$ SIFDM

Fundamentally different than
CDM/WDM/SIDM!

Madelung equations

$(\psi \equiv \sqrt{\rho/m} e^{i\theta} \text{ and } \mathbf{v} \equiv \nabla\theta/m)$

$$\dot{\rho} + \nabla \cdot (\rho \mathbf{v}) = 0$$

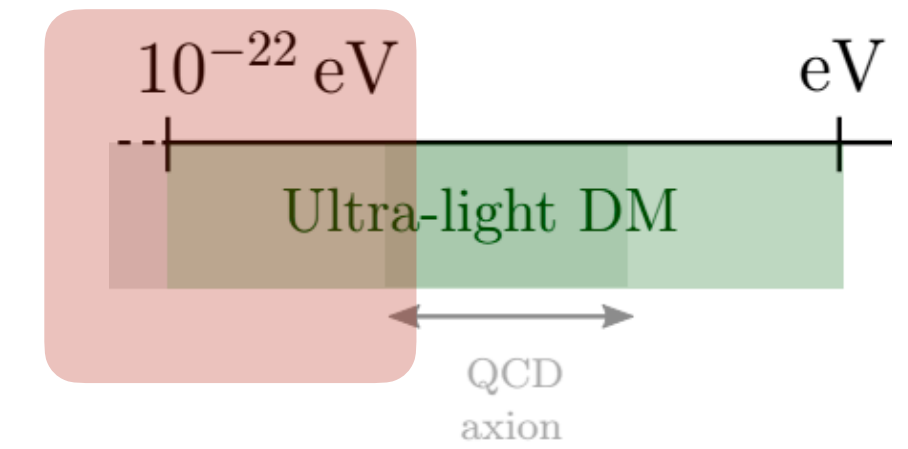
$$\dot{\mathbf{v}} + (\mathbf{v} \cdot \nabla)\mathbf{v} = -\frac{1}{m} \left(V_{grav} - P_{int} - \frac{1}{2m} \frac{\nabla^2 \sqrt{\rho}}{\sqrt{\rho}} \right)$$

$$P_{int} = K\rho^{(j+1)/j} = \frac{g}{2m^2}\rho^2$$

Quantum pressure

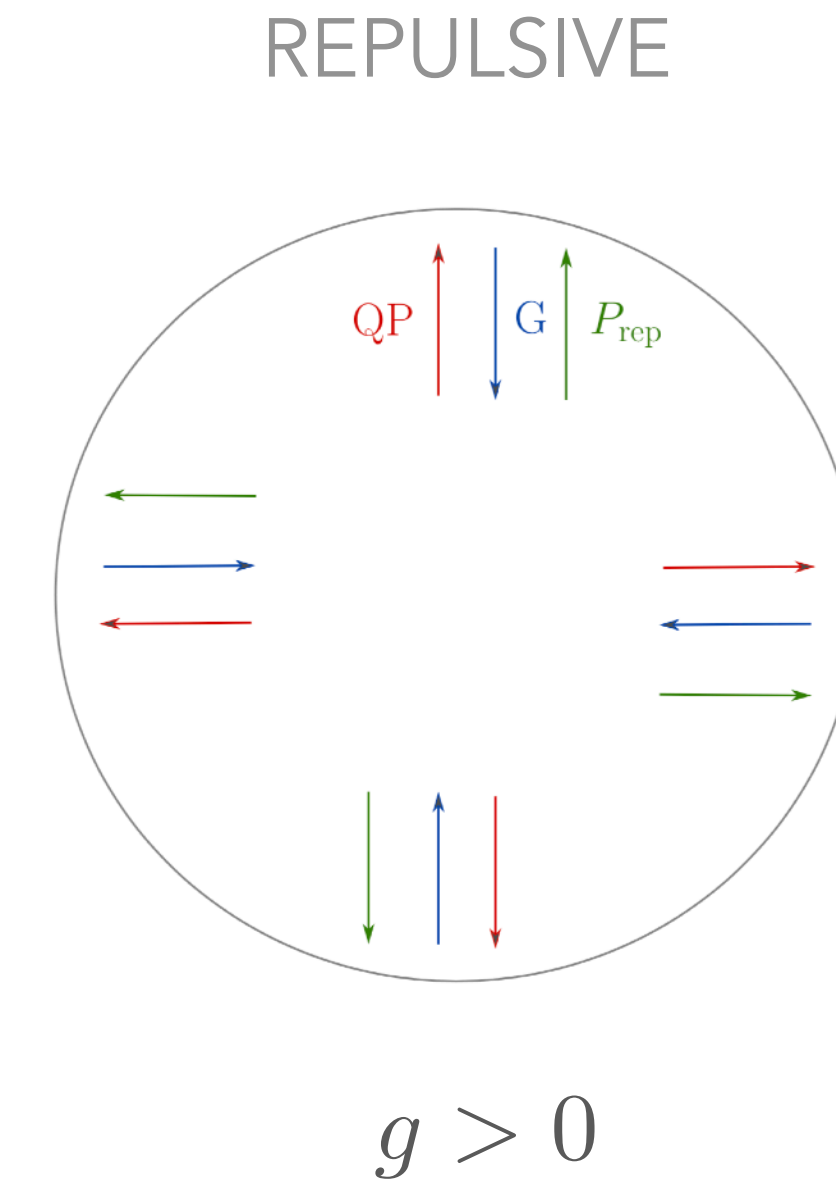
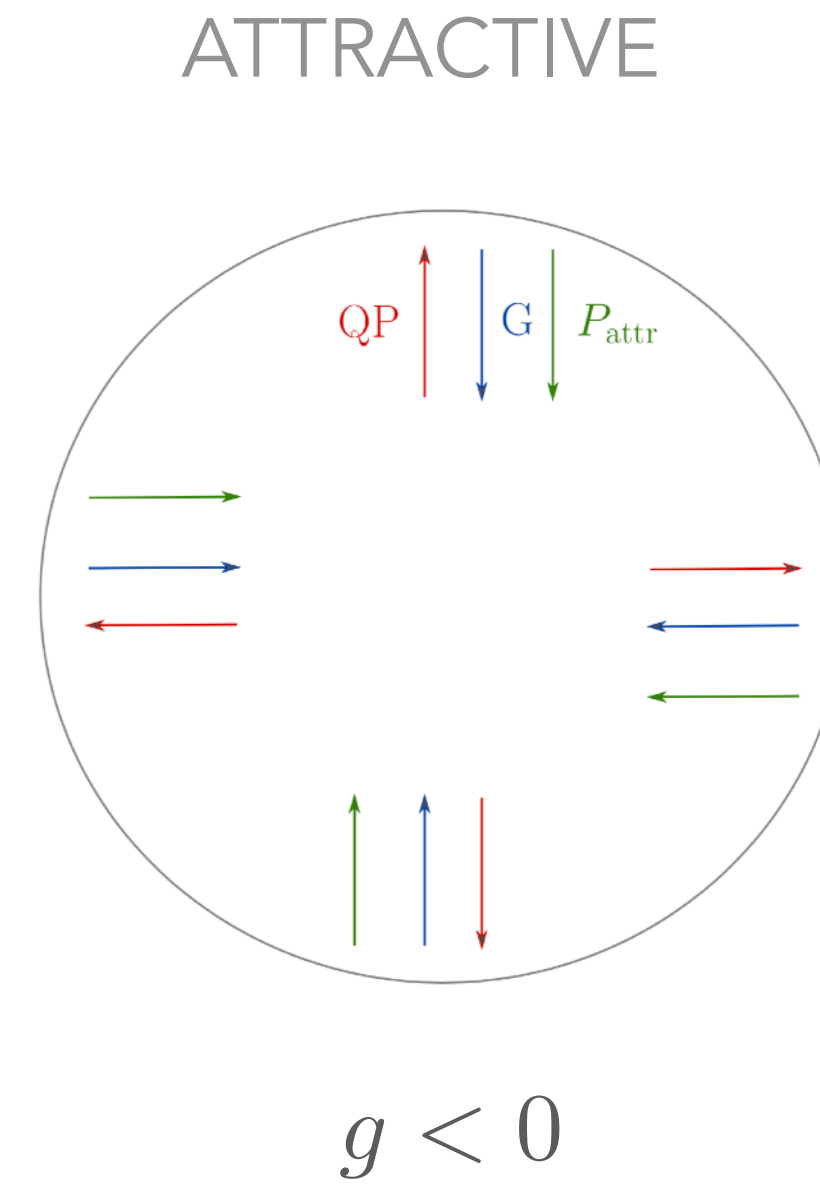
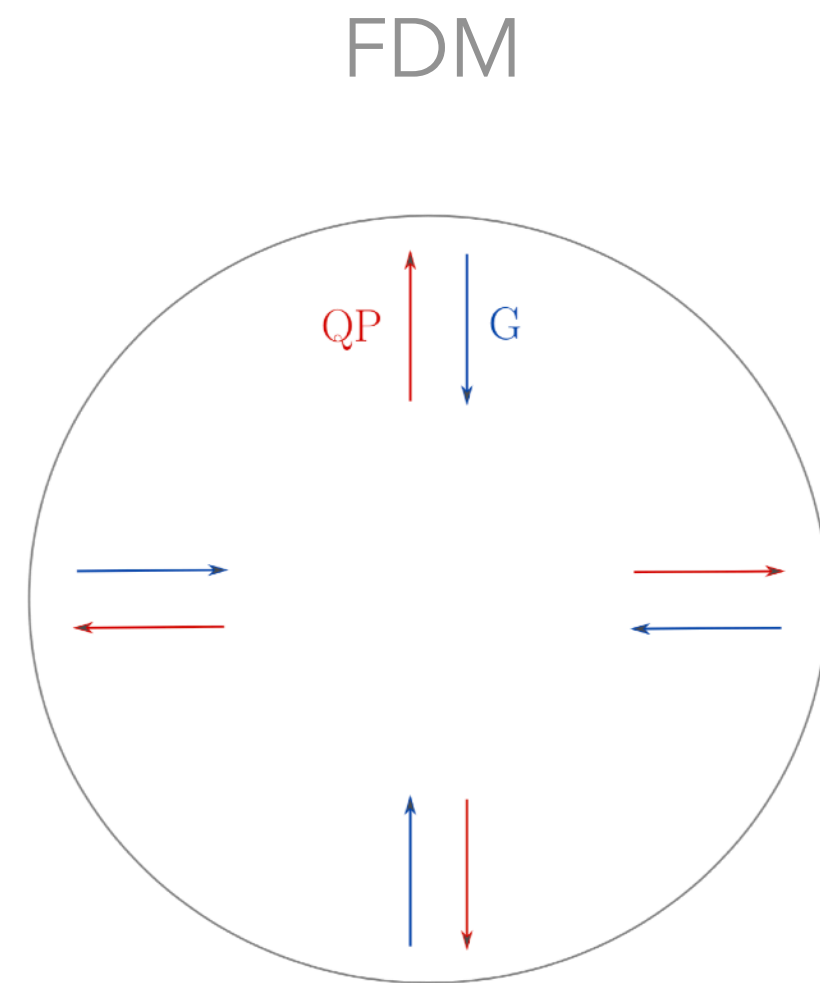
FLUID
DESCRIPTION

Structure formation - perturbation and stability



Competition between gravity and pressure (quantum pressure and interaction)

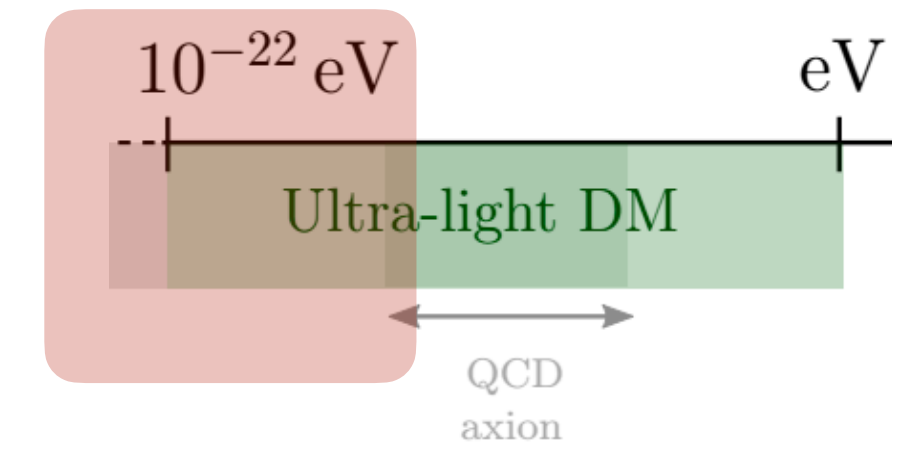
SIFDM



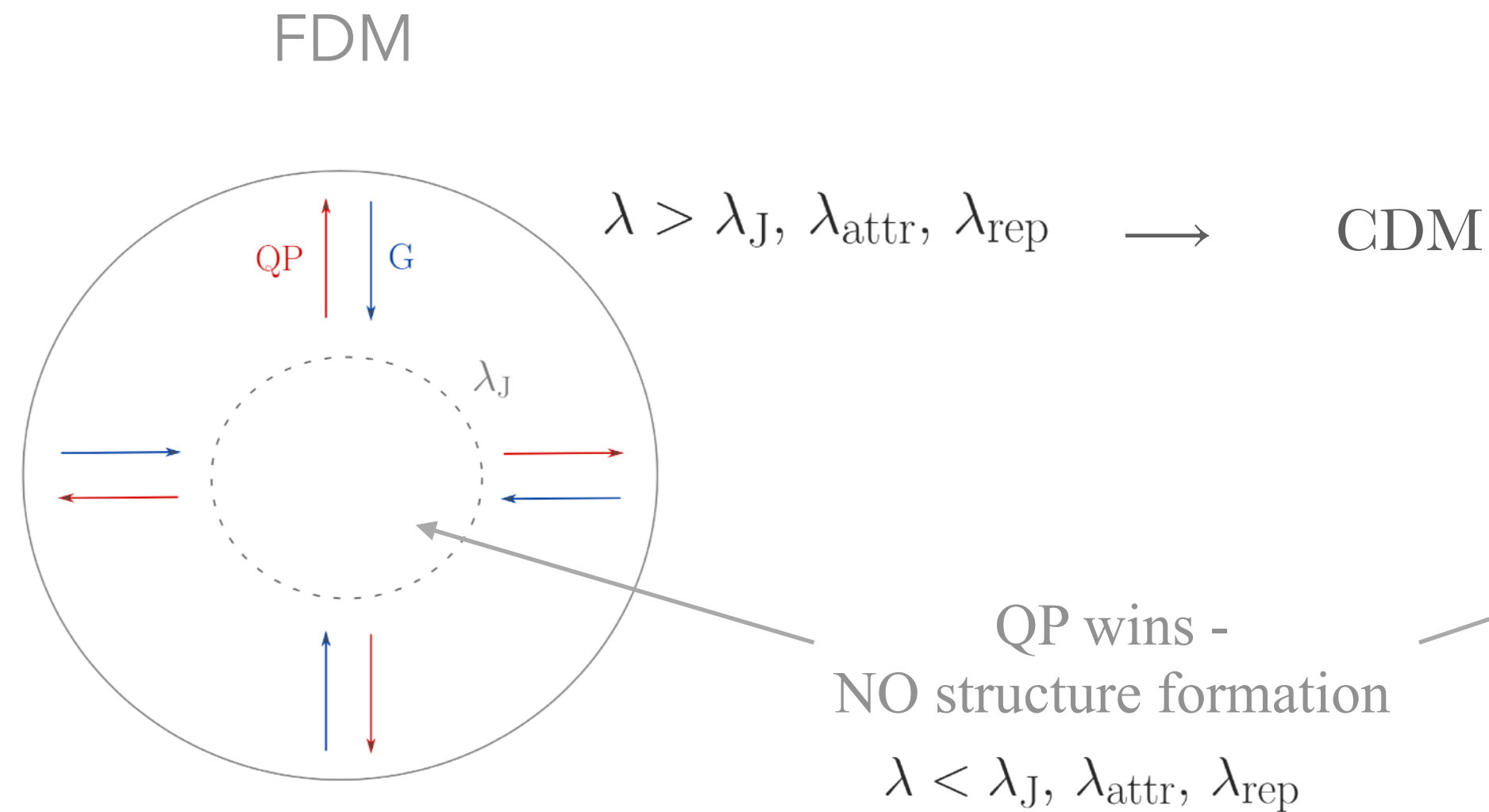
$$\dot{\rho} + \nabla \cdot (\rho \mathbf{v}) = 0$$

$$\dot{\mathbf{v}} + (\mathbf{v} \cdot \nabla) \mathbf{v} = -\frac{1}{m} \left(V_{grav} - \underbrace{P_{int}}_{P_{int} = \frac{g}{2m^2} \rho^2} - \underbrace{\frac{1}{2m} \frac{\nabla^2 \sqrt{\rho}}{\sqrt{\rho}}}_{\text{Quantum pressure}} \right)$$

Structure formation - perturbation and stability



Finite clustering scale - no structure formation on small scales



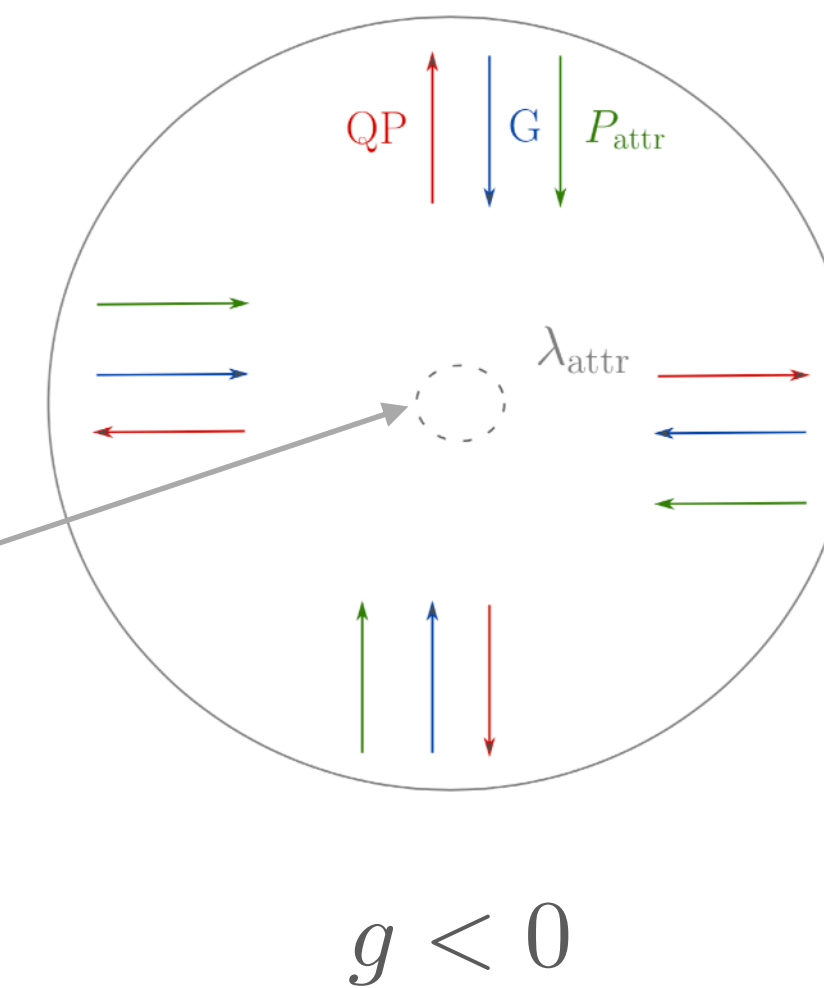
Finite size coherent core – Bose stars

$$\lambda_J = 55 \left(\frac{m}{10^{-22} \text{ eV}} \right)^{-1/2} \left(\frac{\rho}{\bar{\rho}} \right)^{-1/4} (\Omega_m h)^{-1/4} \text{ kpc}$$

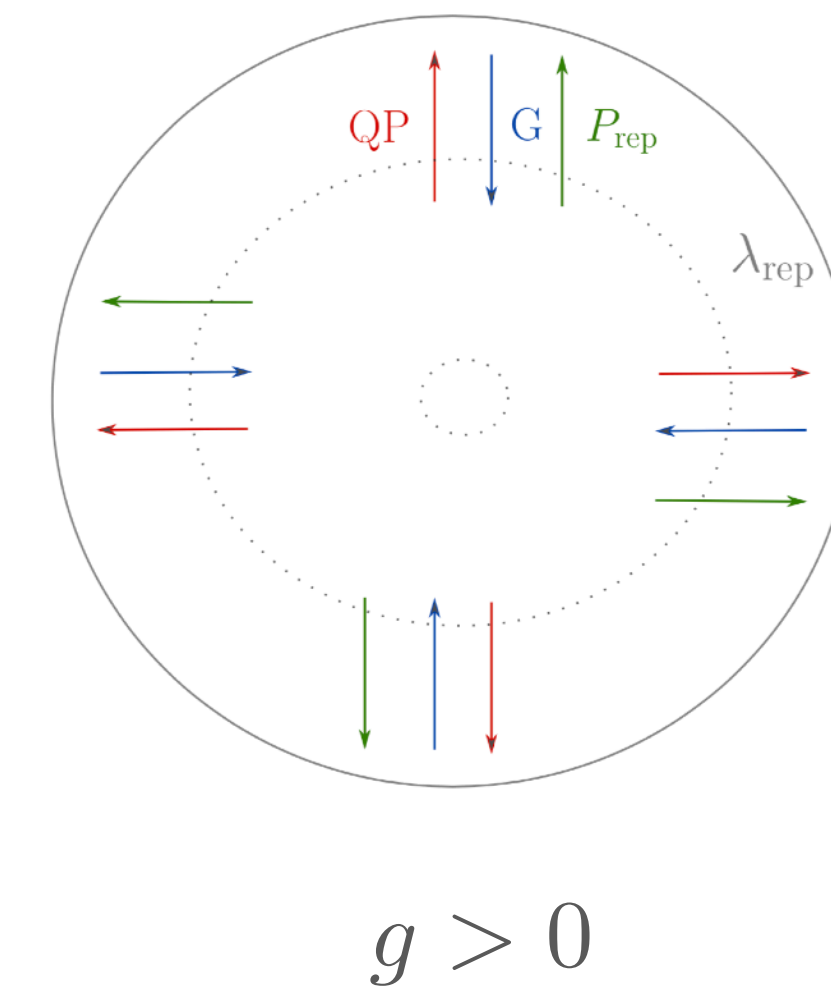
$m \leq 10^{-20} \text{ eV} \Rightarrow \lambda_{dB} > \mathcal{O}(\text{kpc})$ Galactic scales

SIFDM

ATTRACTIVE



REPULSIVE

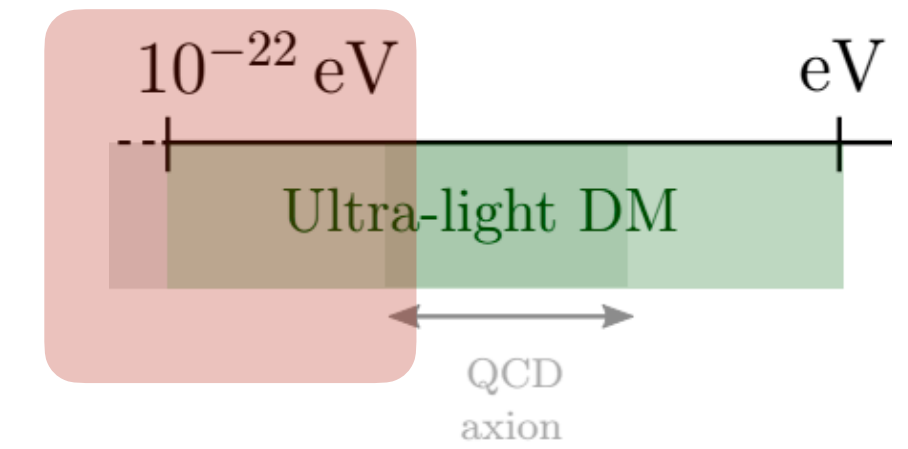


For attractive interactions can only form localized clumps (solitons)

QCD axion: $m \sim 10^{-5} \text{ eV}$
 $\lambda_a \sim -10^{-48}$ \rightarrow $l_{soliton} \sim 10^{-5} \text{ kpc}$

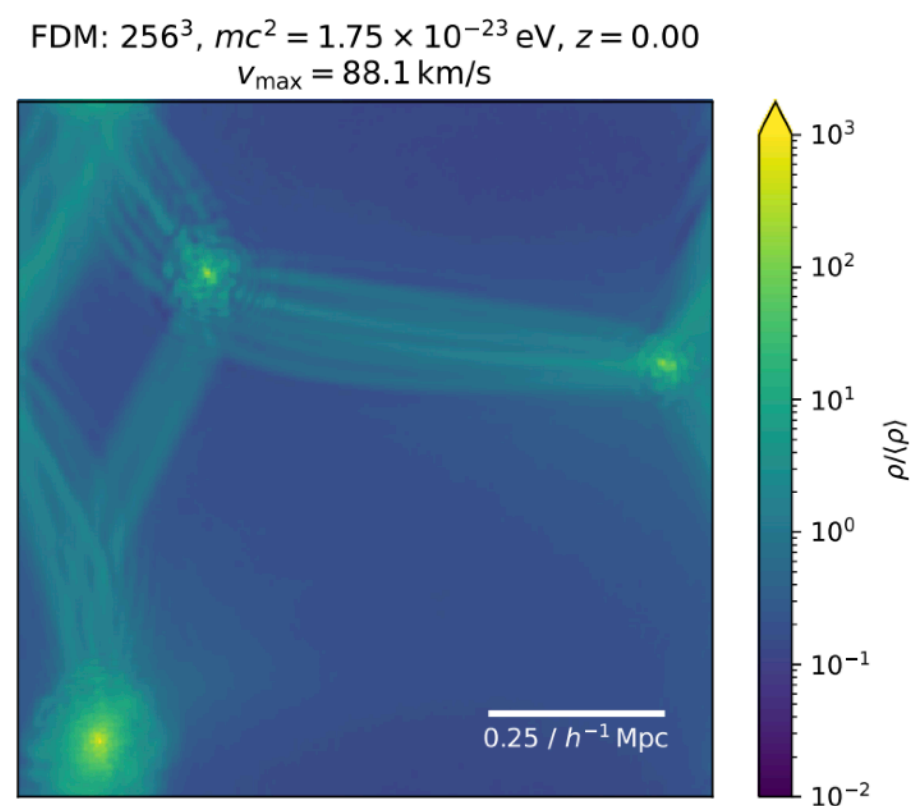
Phenomenology

RICH PHENOMENOLOGY ON SMALL SCALES

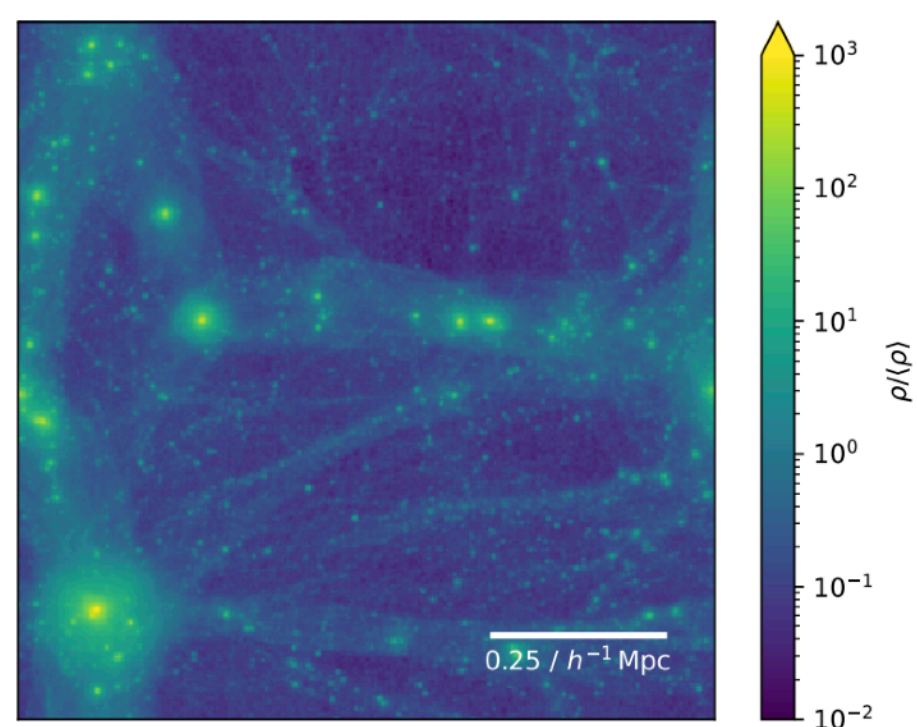


* Focus only in gravitational signatures

Suppression of small structures

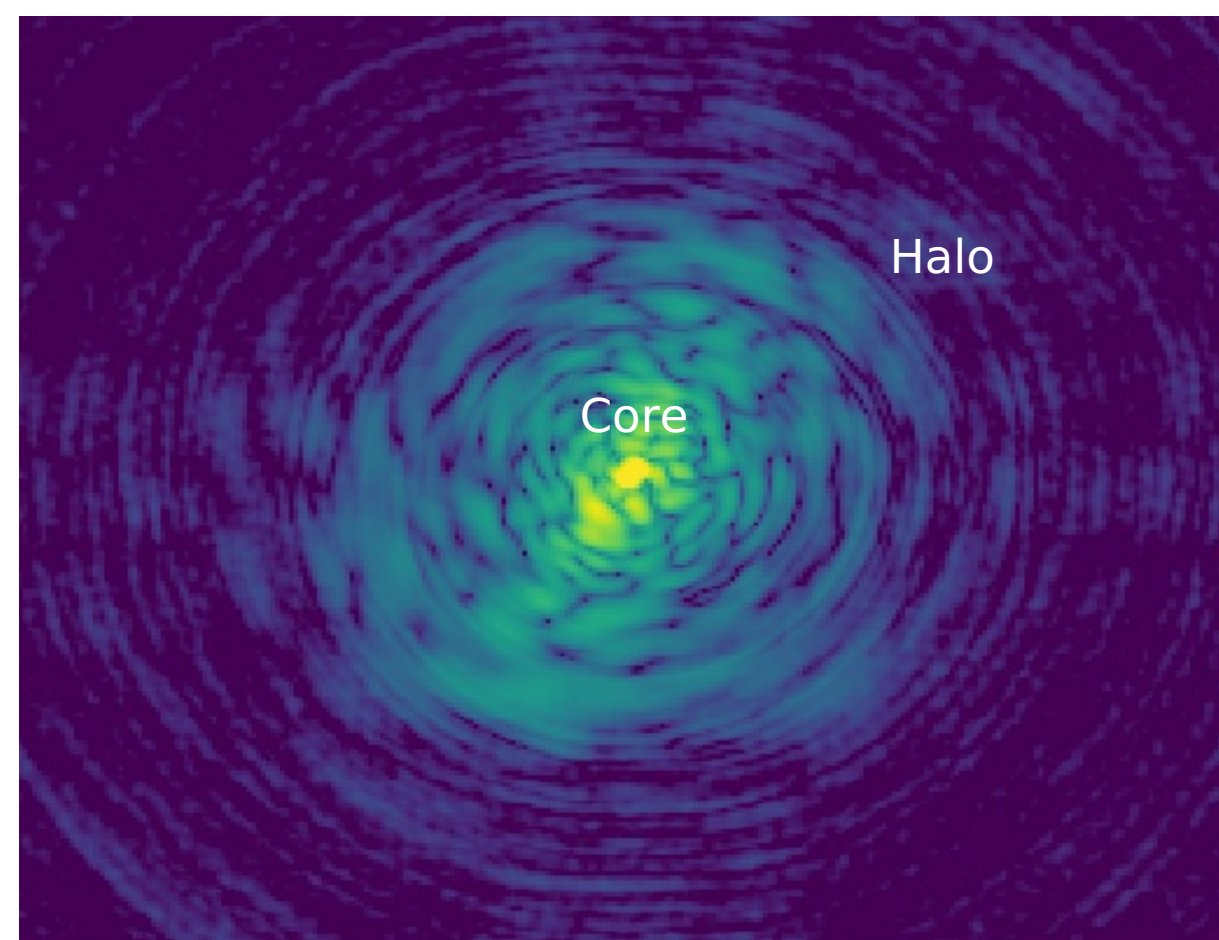


CDM: 256^3 , $z = 0.00$

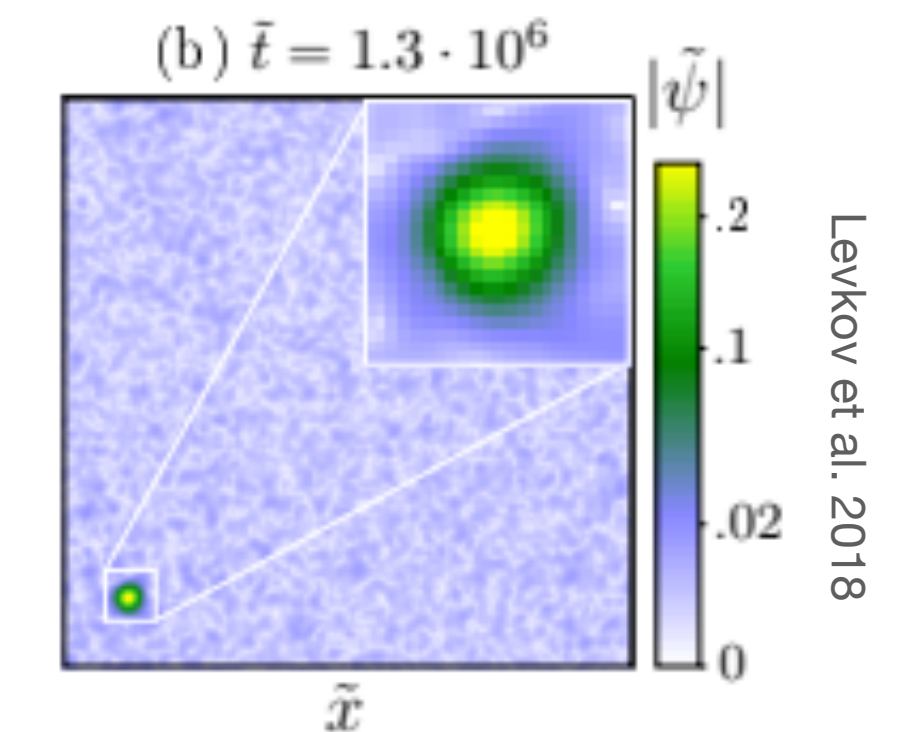


S. May et al. 2021

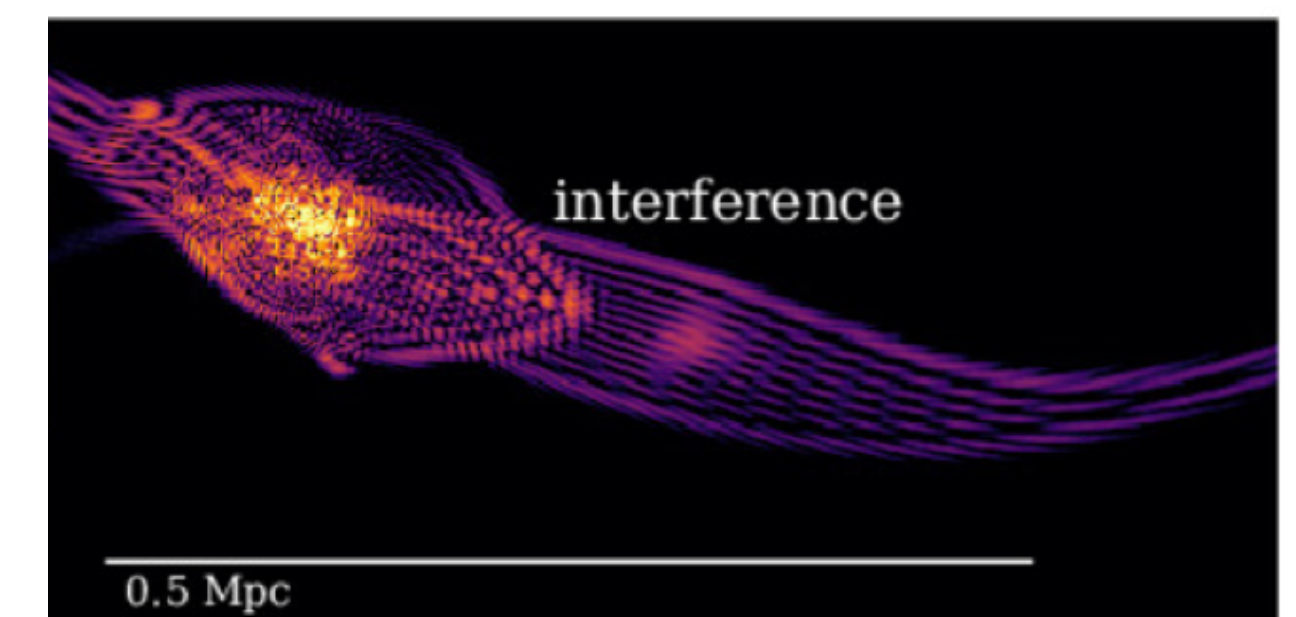
Formation of a solitonic core



Dynamical effects

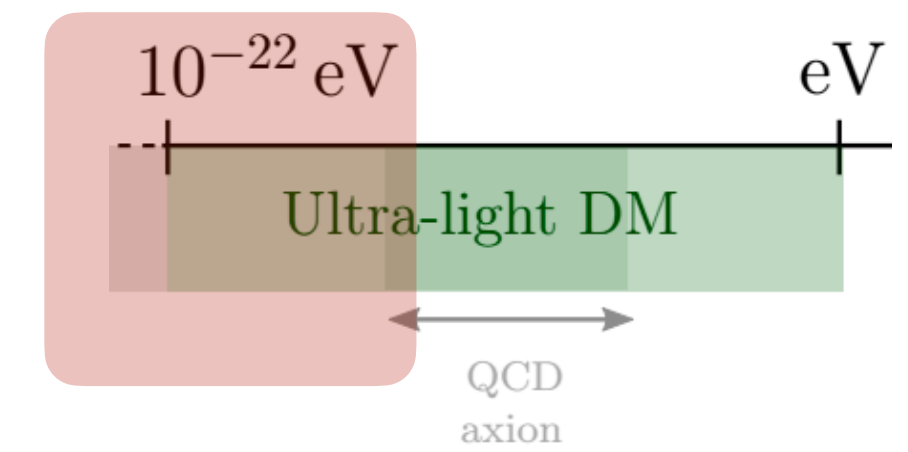


Wave interference



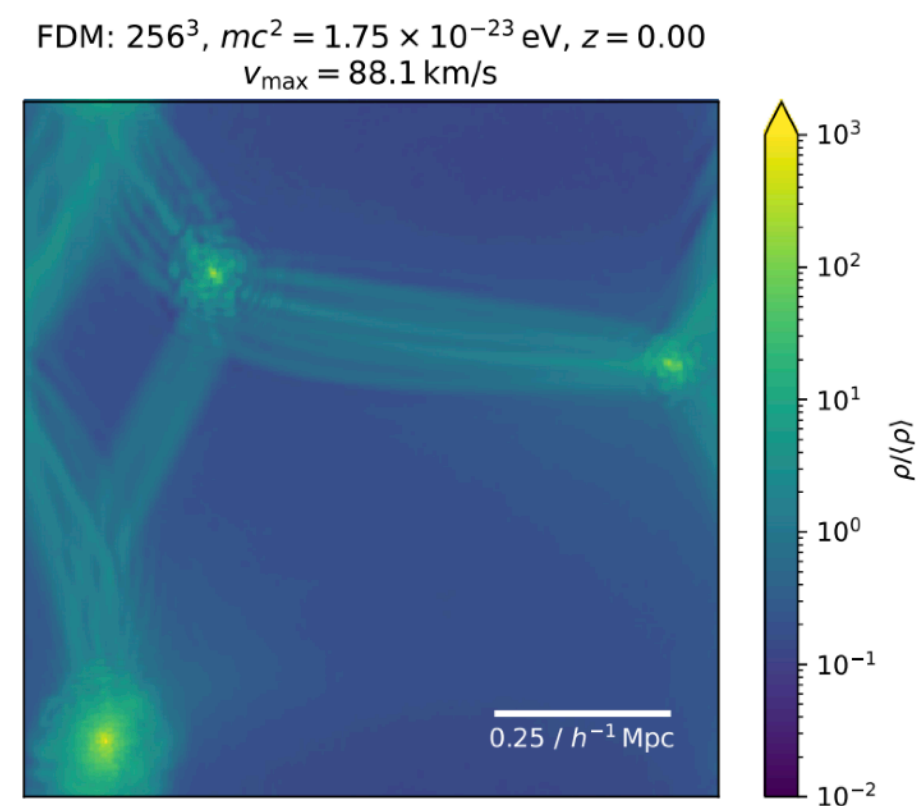
Mocz et al. 2017

Phenomenology

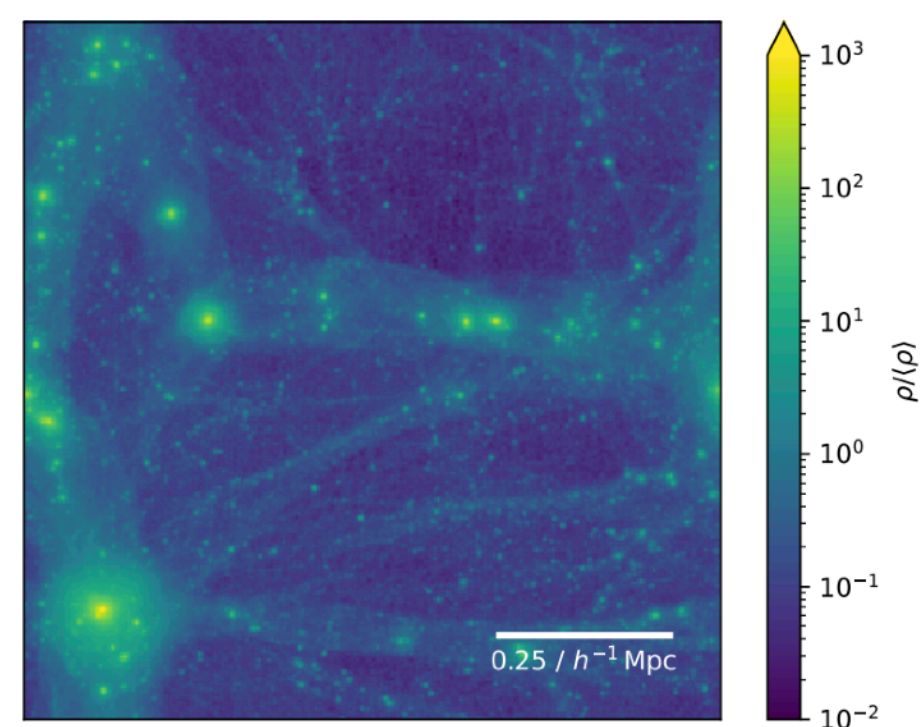


RICH PHENOMENOLOGY ON SMALL SCALES

Suppression of small structures

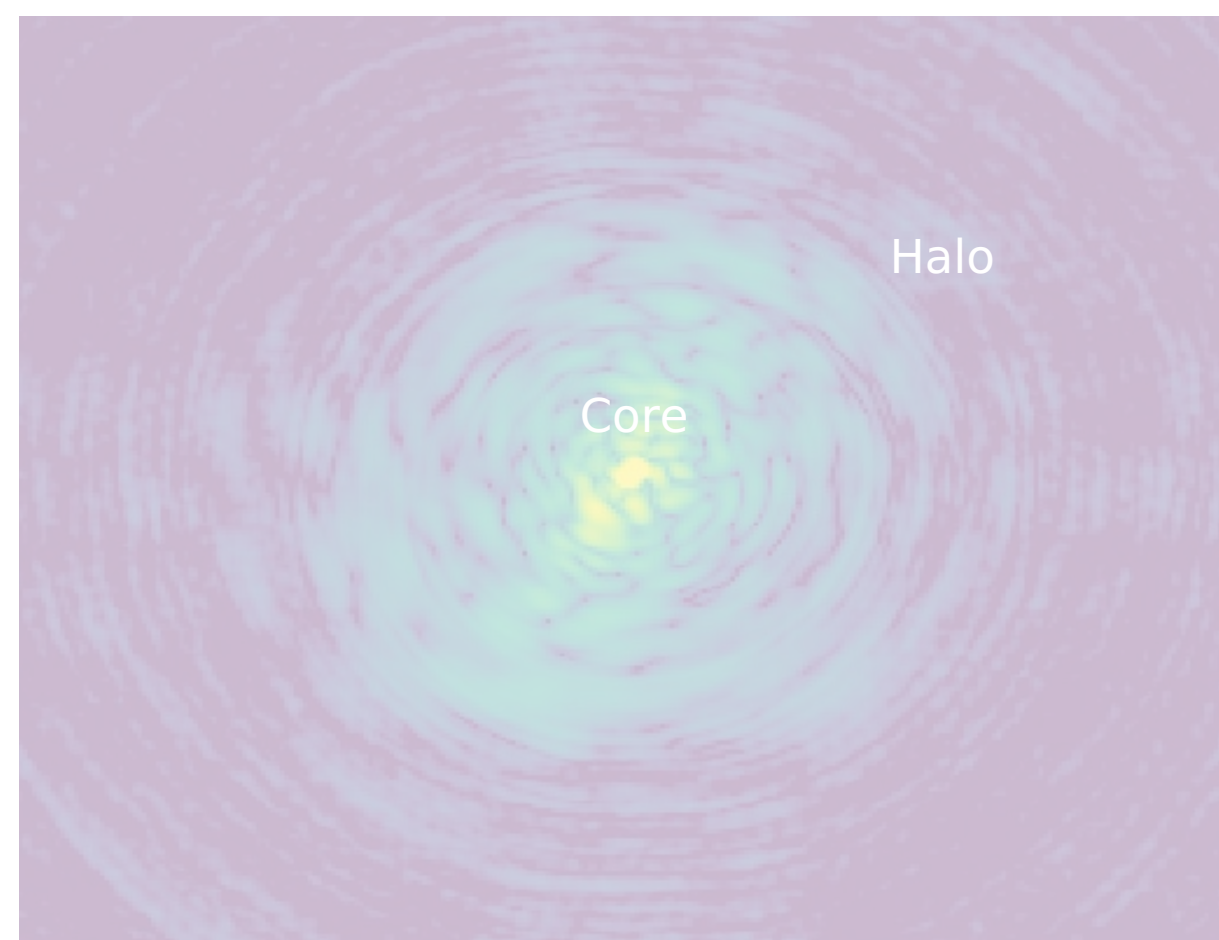


CDM: 256^3 , $z = 0.00$

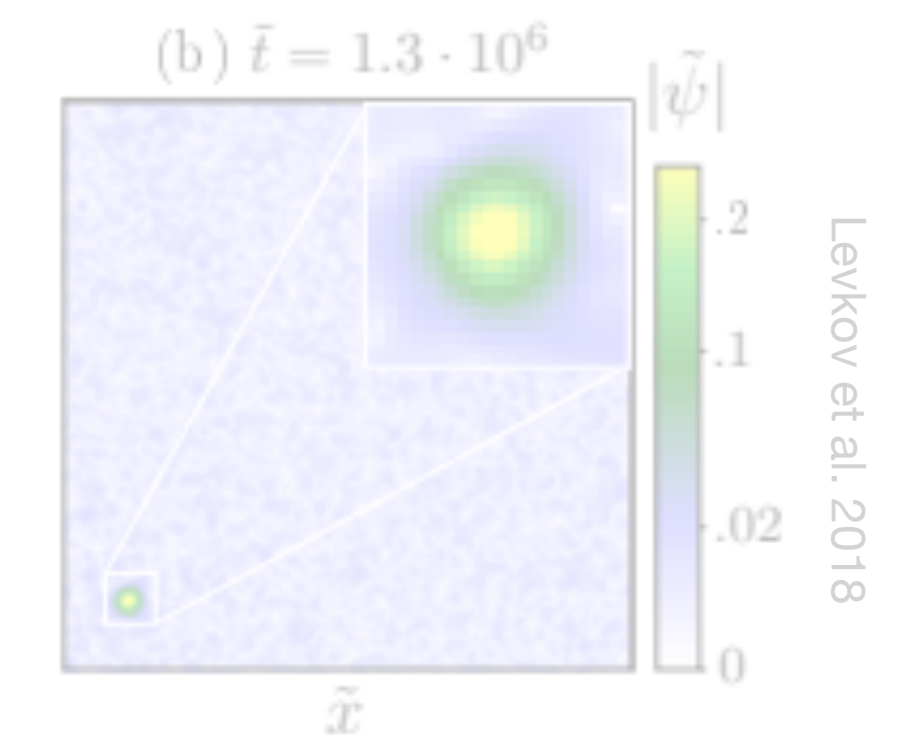


S. May et al. 2021

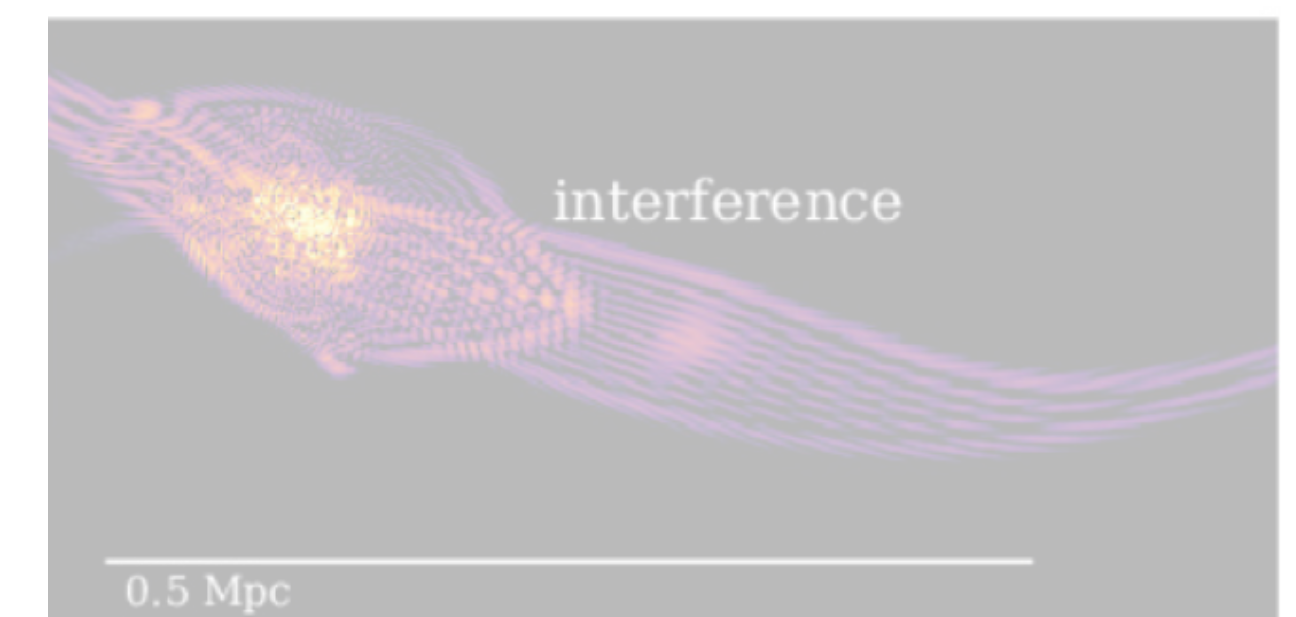
Formation of a solitonic core



Dynamical effects



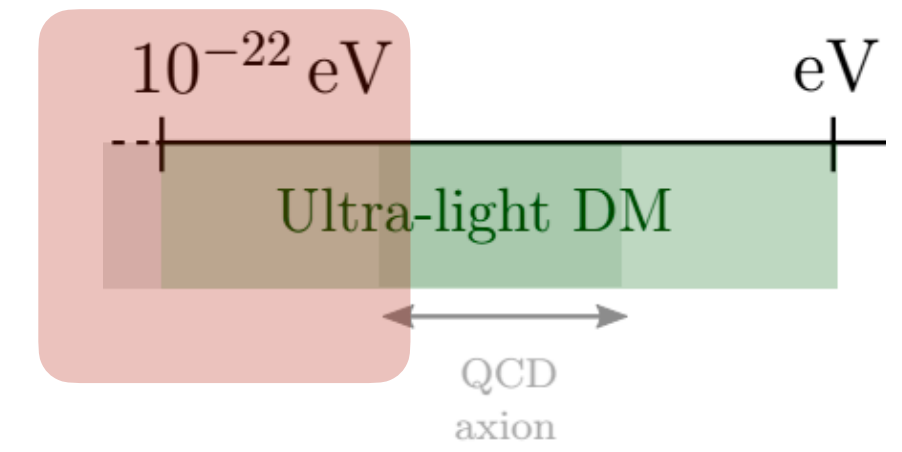
Wave interference



Mocz et al. 2017

Phenomenology

Suppression of small structures

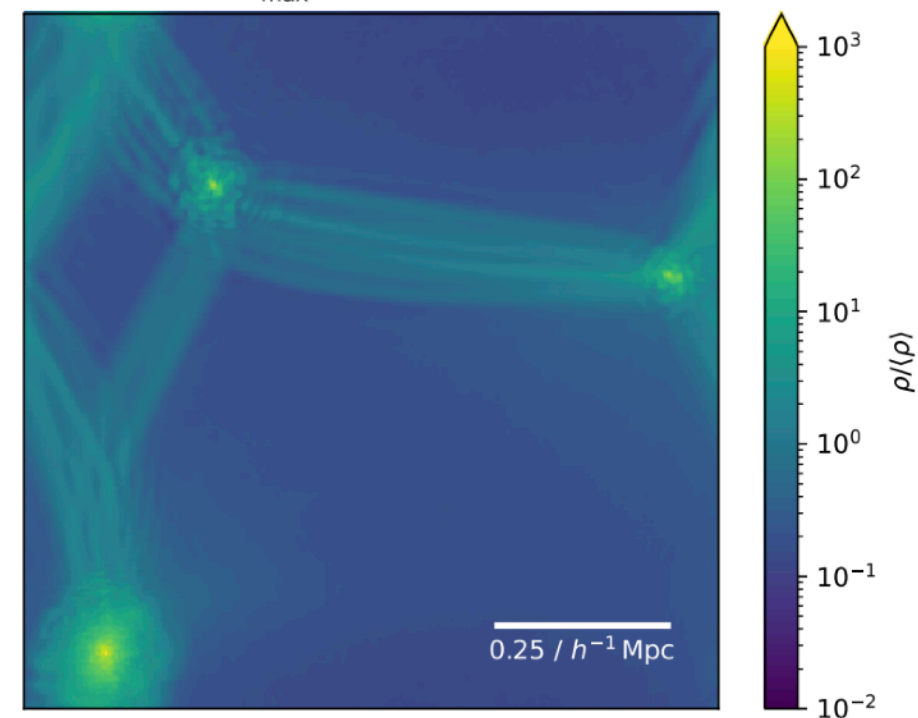


Finite Jeans length λ_J or $\lambda_{\text{attr}}, \lambda_{\text{rep}}$

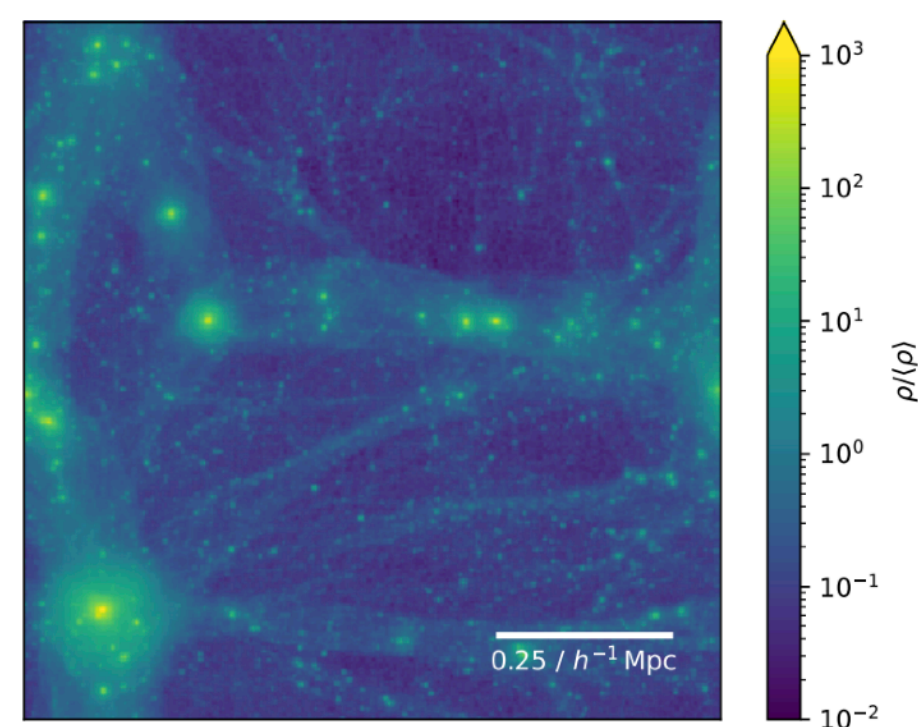


No small scale structure

FDM: 256^3 , $mc^2 = 1.75 \times 10^{-23}$ eV, $z = 0.00$
 $v_{\text{max}} = 88.1$ km/s

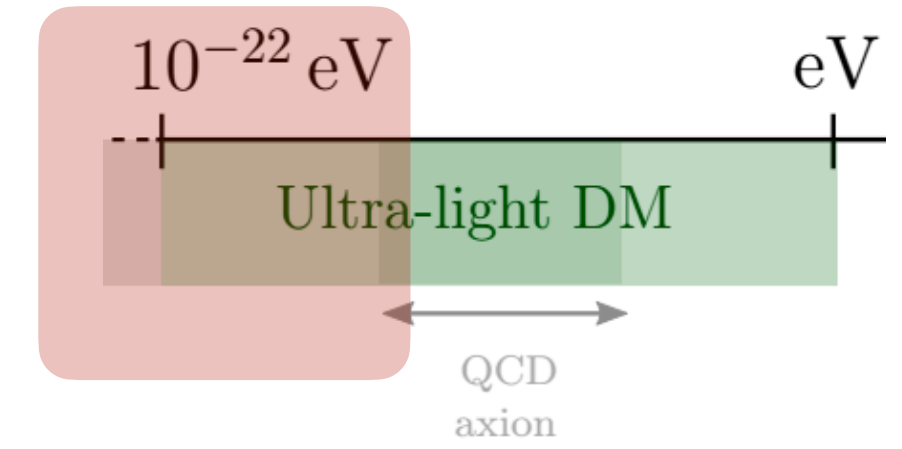


CDM: 256^3 , $z = 0.00$



Phenomenology

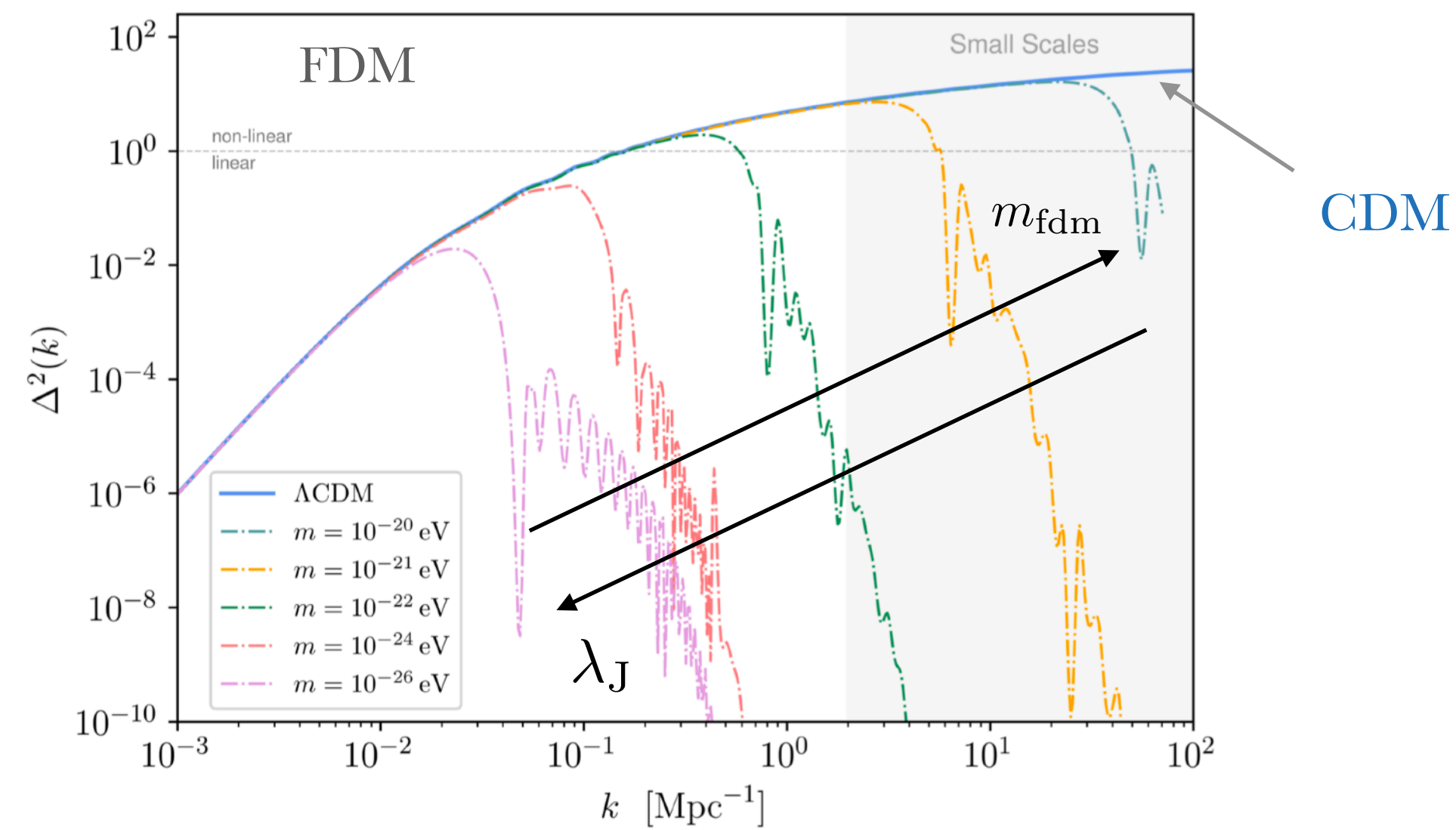
Suppression of small structures



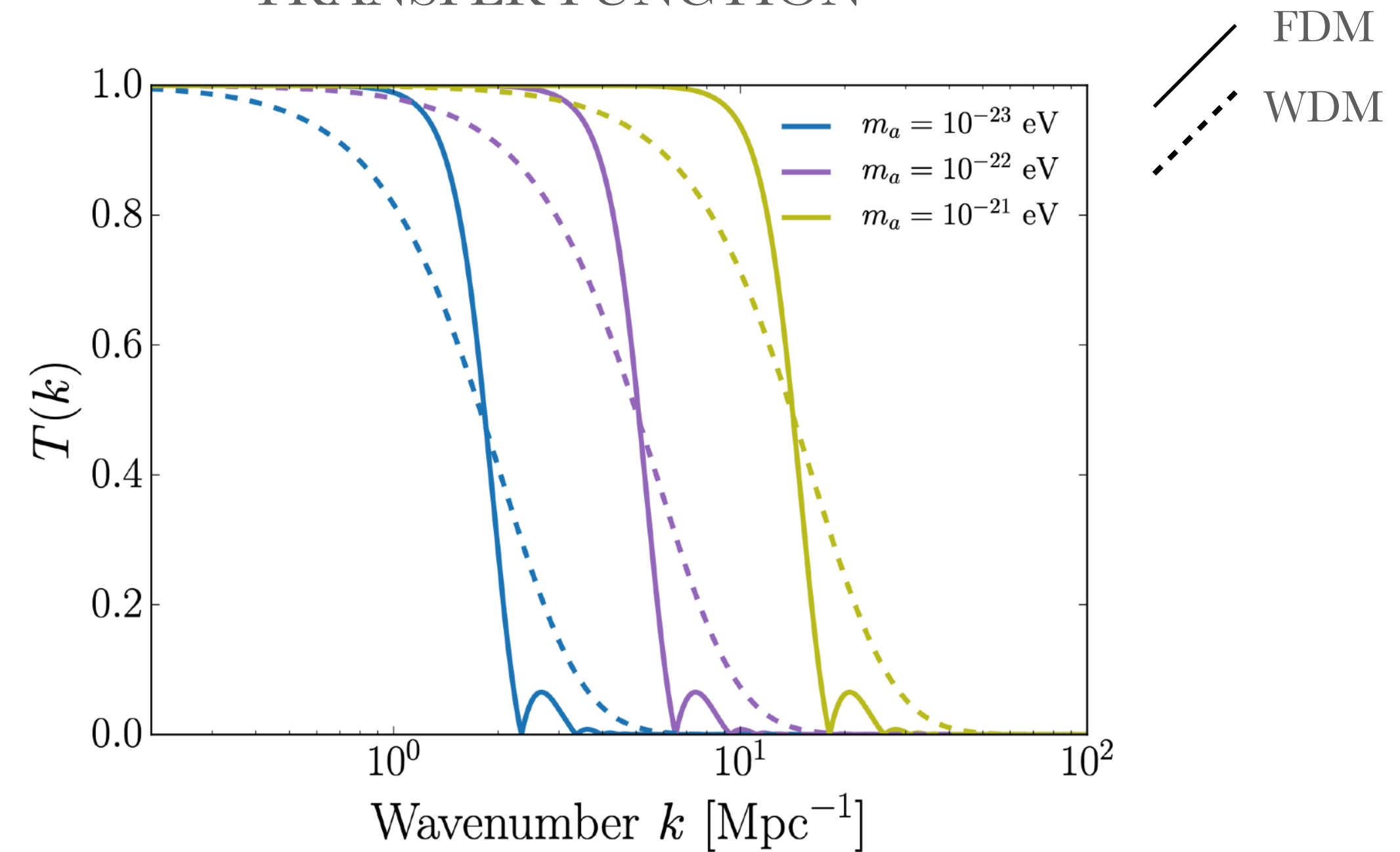
Finite Jeans length λ_J or $\lambda_{\text{attr}}, \lambda_{\text{rep}}$ \longrightarrow

Suppresses small scale structure

POWER SPECTRUM



TRANSFER FUNCTION



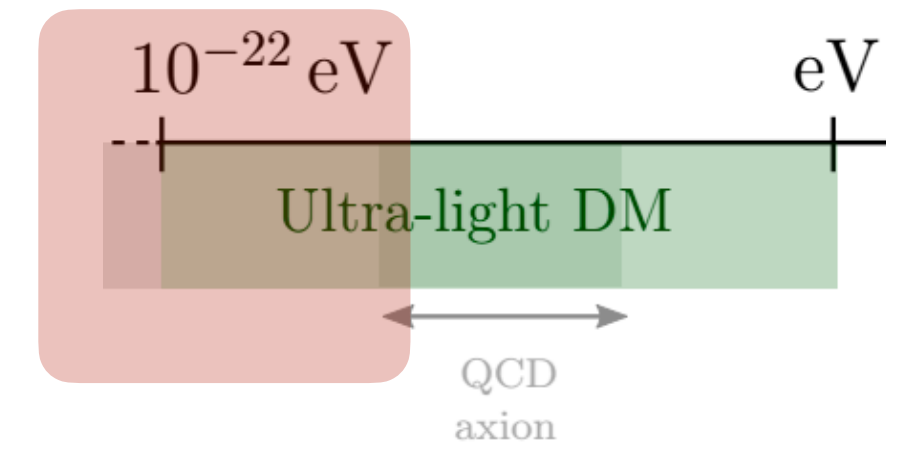
$$P_X(k, z) = T_X^2(k, z) P_{\Lambda\text{CDM}}(k)$$

$$\begin{cases} T_{\text{WDM}} = [1 + (\alpha k)^{2\mu}]^{-5/\mu} \\ T_{\text{FDM}} = \frac{\cos x_J^3(k)}{1 + x_J^8(k)} \end{cases}$$

- Degenerate with WDM

Phenomenology

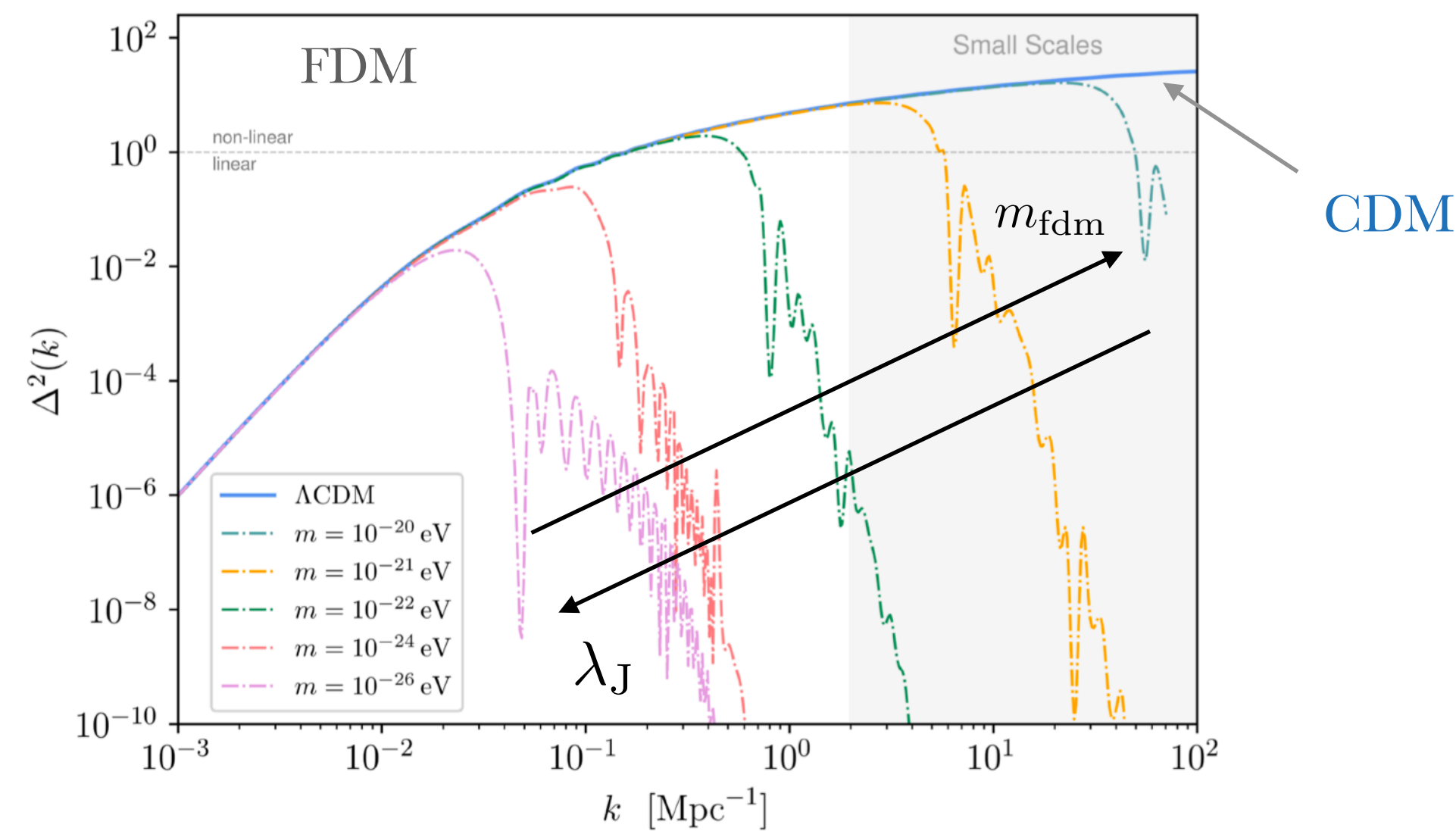
Suppression of small structures



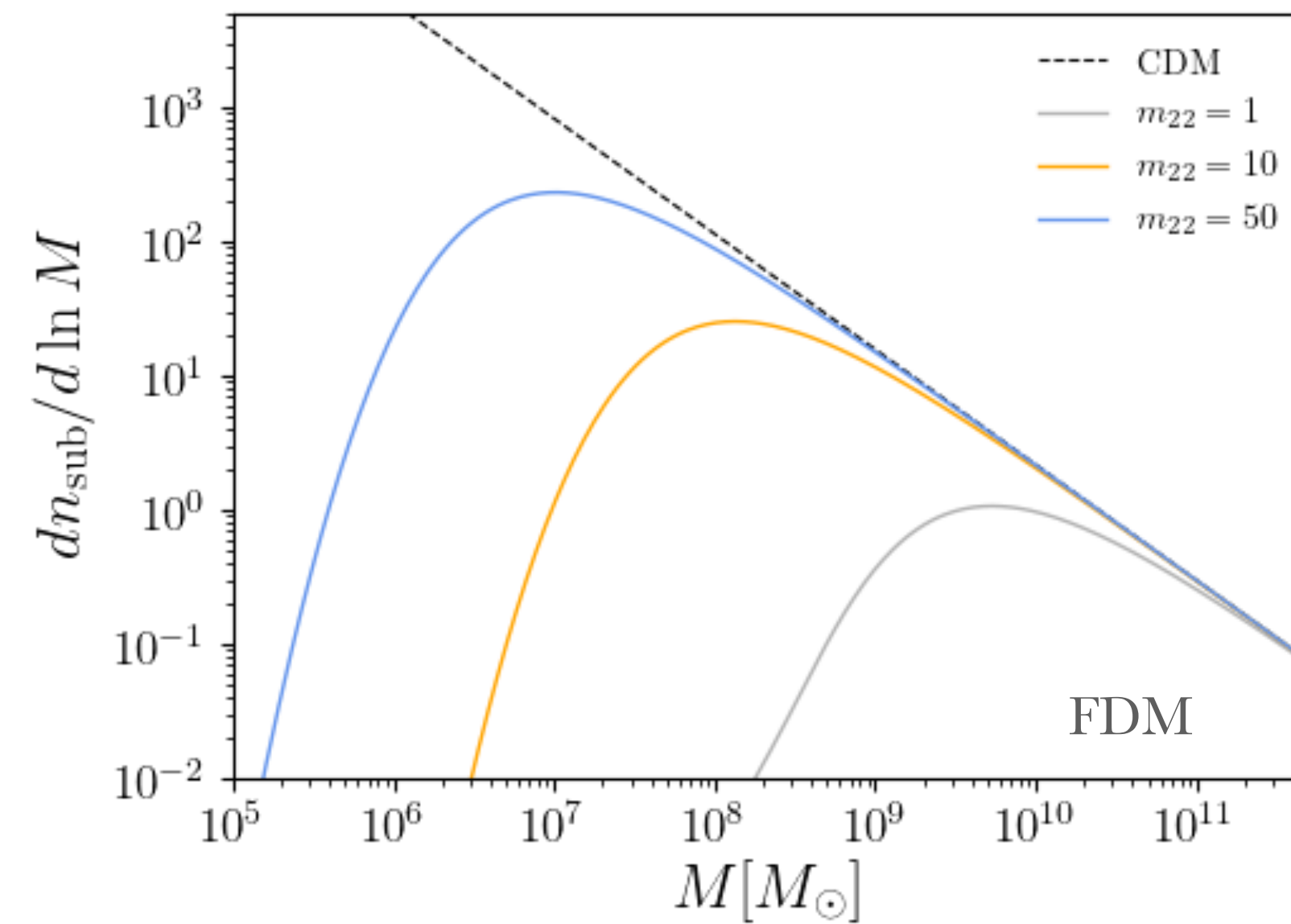
Finite Jeans length λ_J or $\lambda_{\text{attr}}, \lambda_{\text{rep}}$ \longrightarrow

Suppresses small scale structure

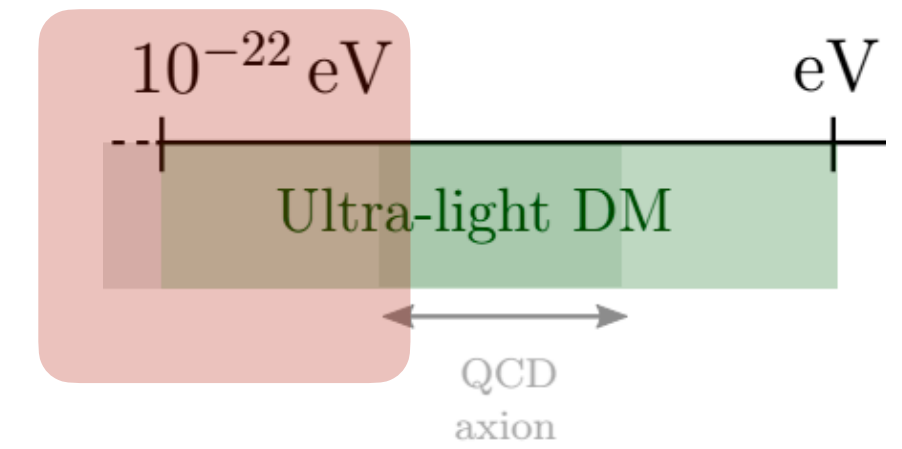
POWER SPECTRUM



(sub) HALO MASS FUNCTION

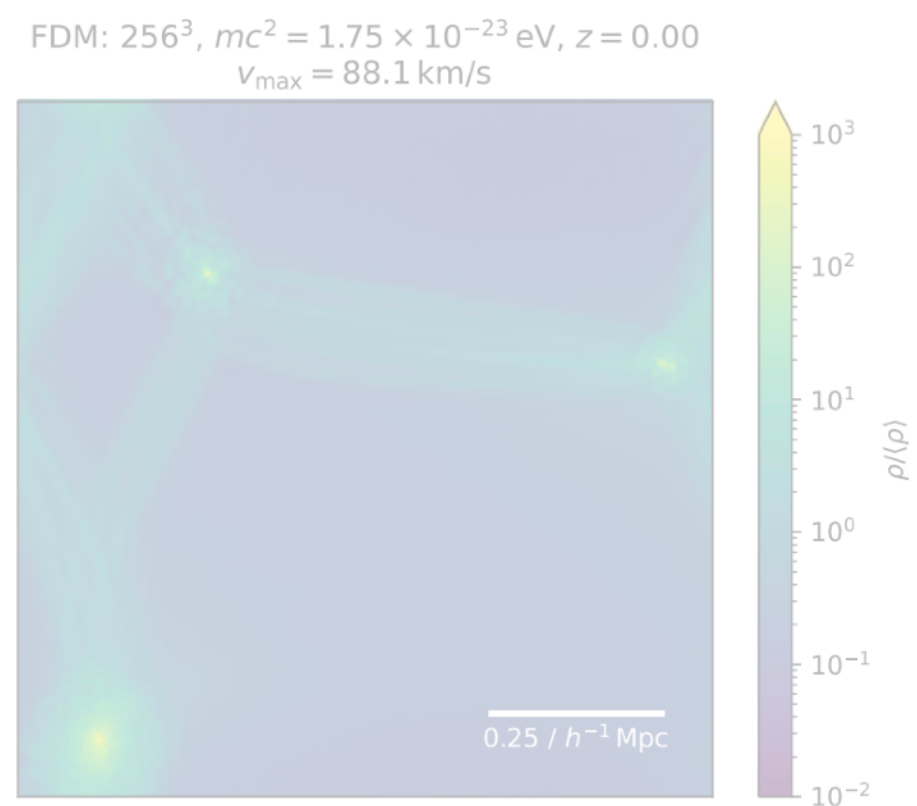


Phenomenology

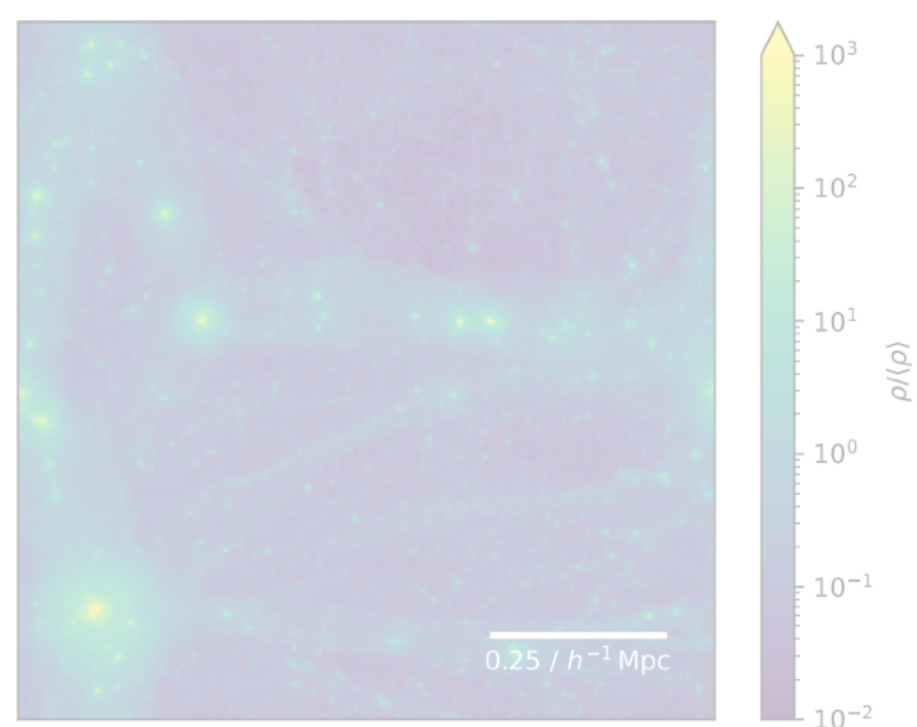


RICH PHENOMENOLOGY ON SMALL SCALES

Suppression of small structures

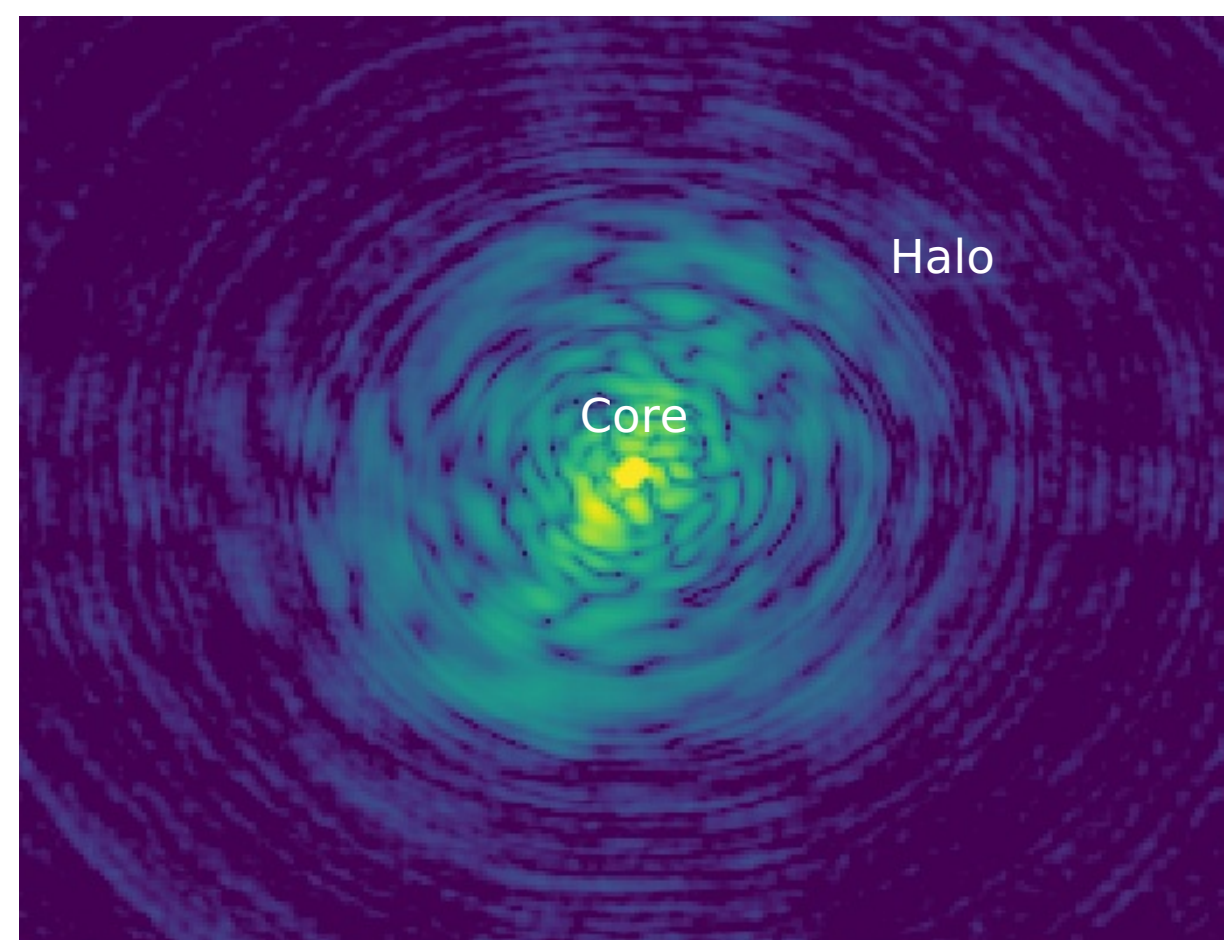


CDM: 256^3 , $z = 0.00$

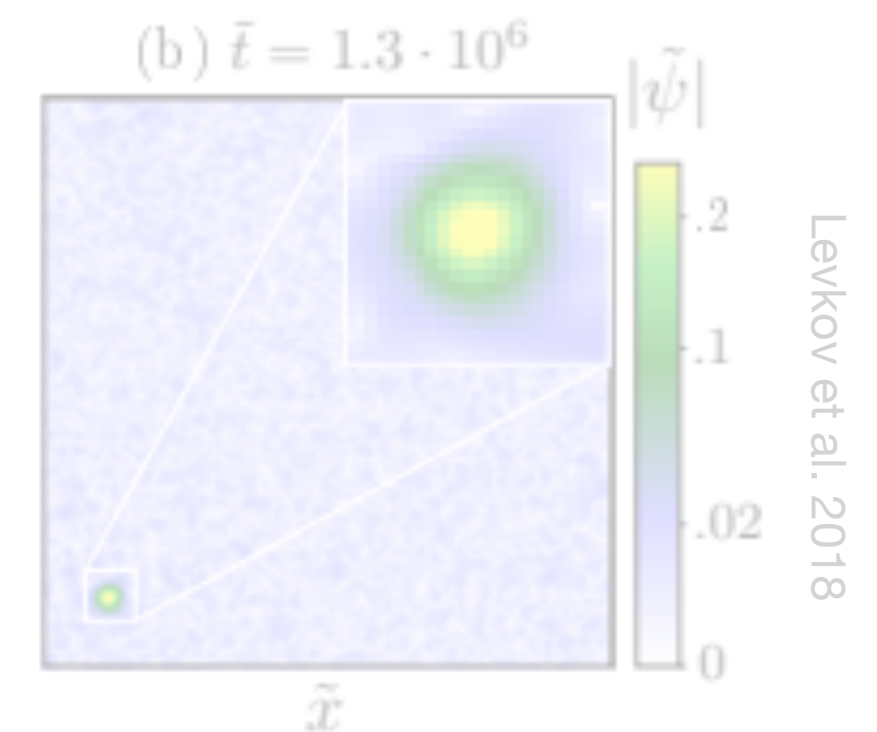


S. May et al. 2021

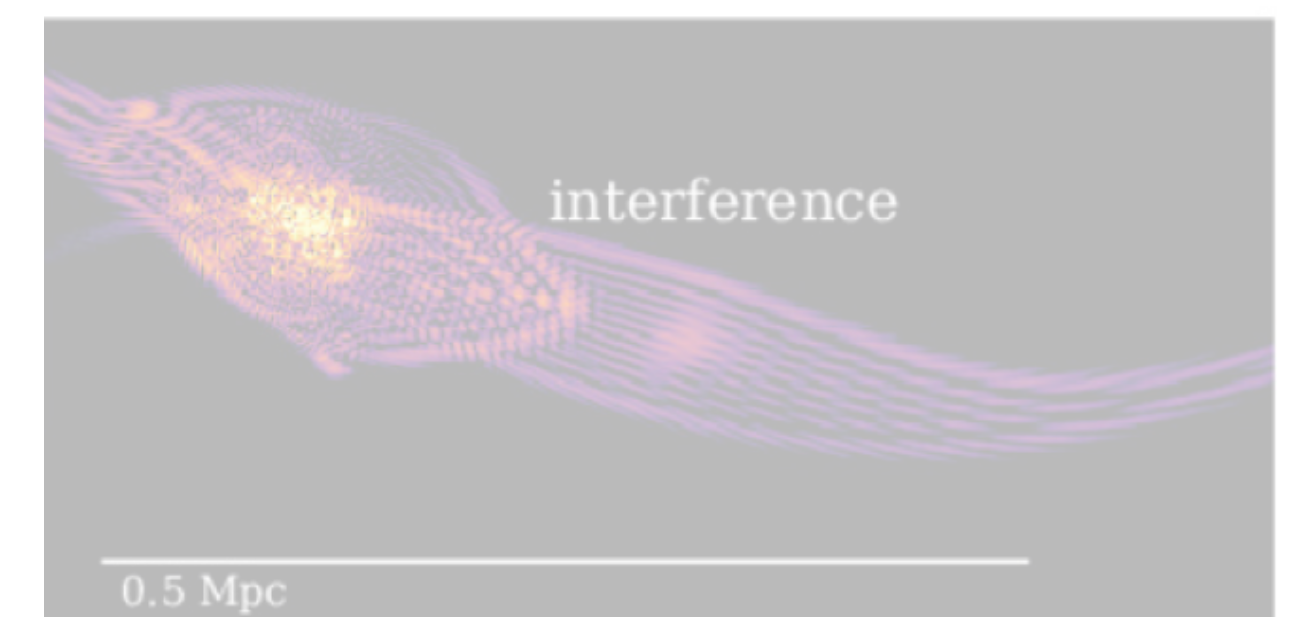
Formation of a solitonic core



Dynamical effects



Wave interference



Mocz et al. 2017

Phenomenology

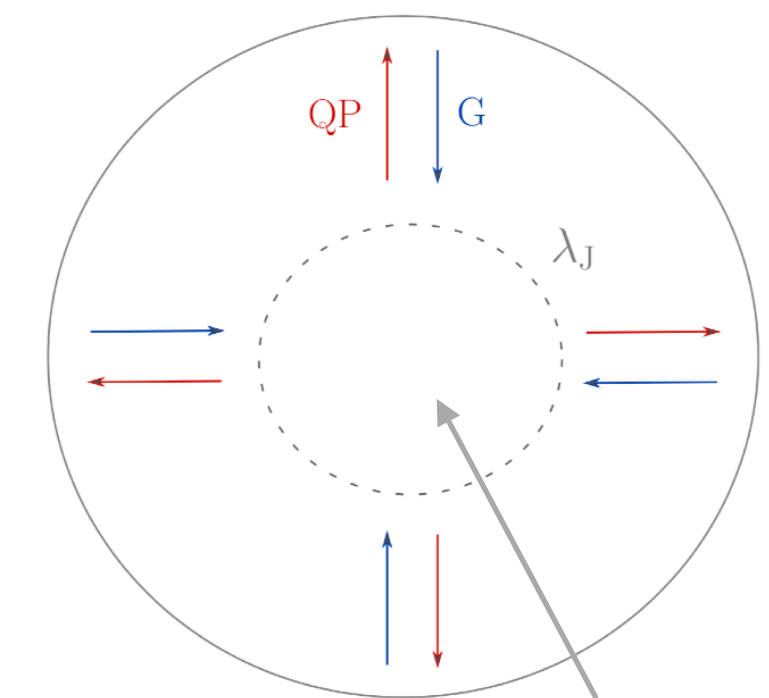
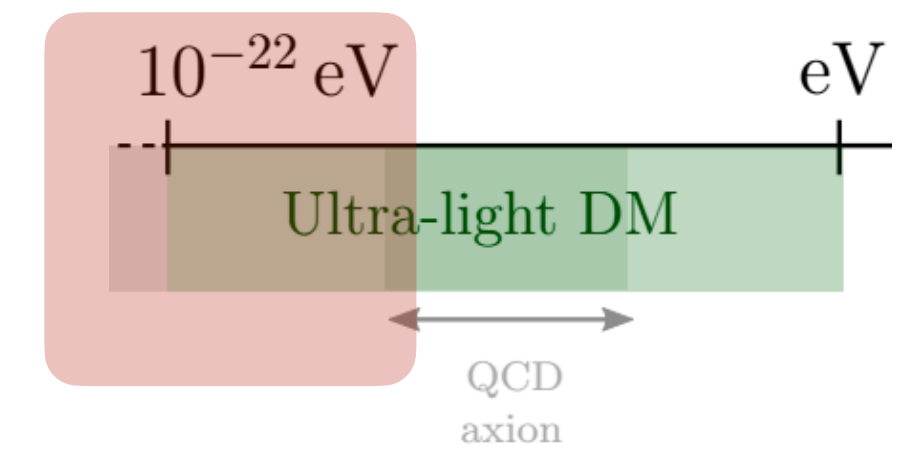
Formation of **cores**

NON-LINEAR
evolution: need
simulations

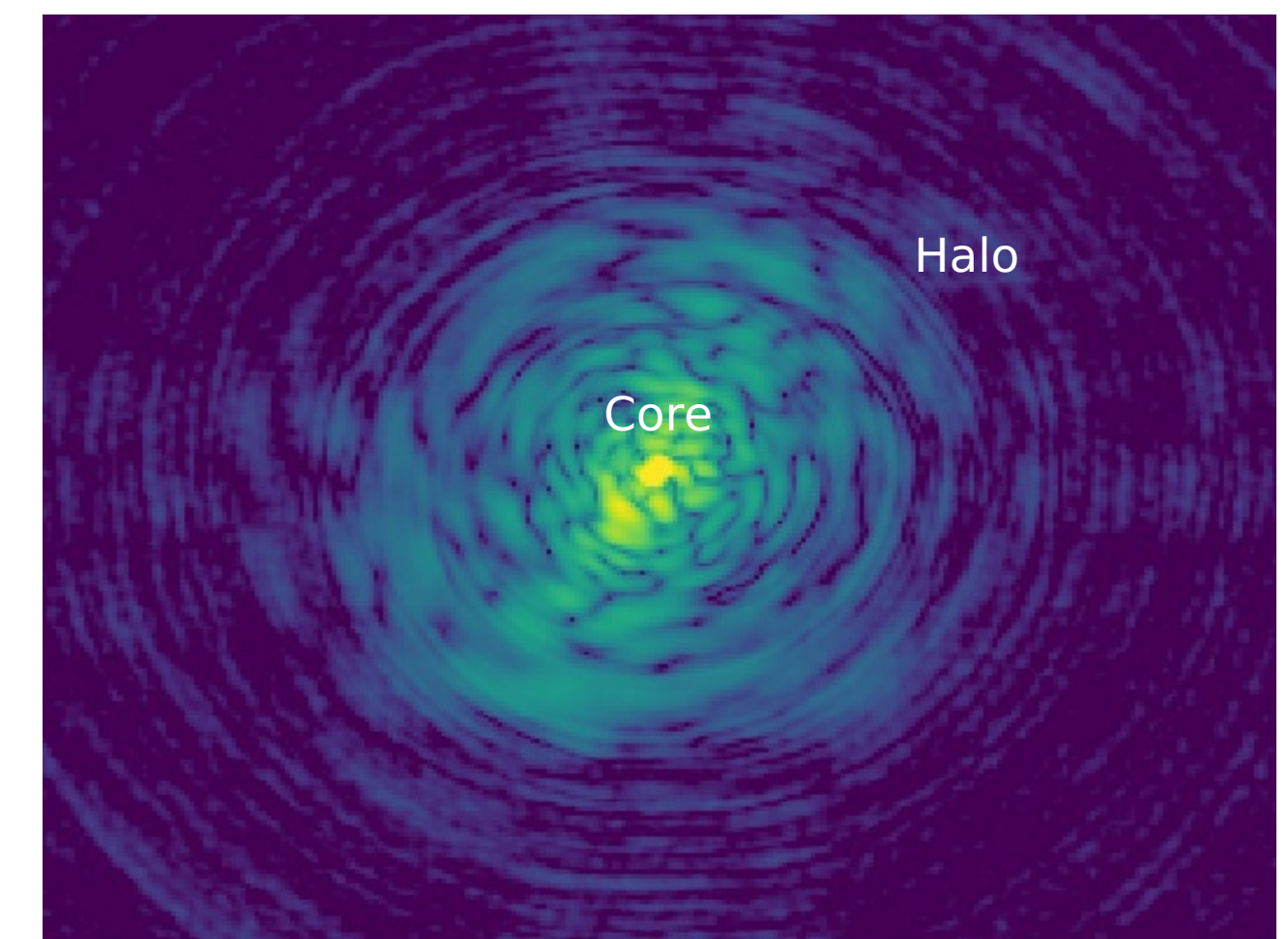
$$m = 10^{-22} \text{ eV} \quad N = 512^3 \quad L = 300 \text{ kpc}$$



Simulation by Jowett Chan

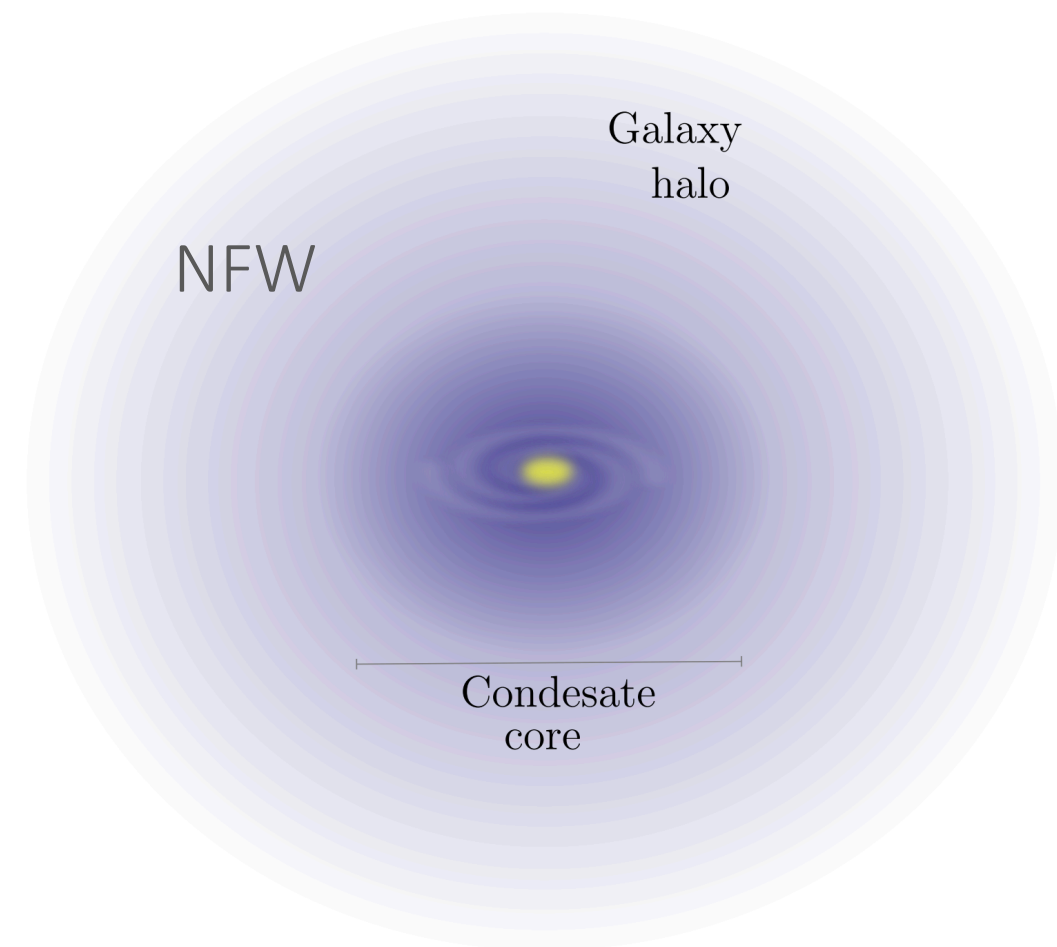


NO structure formation
Stable, oscillating solution

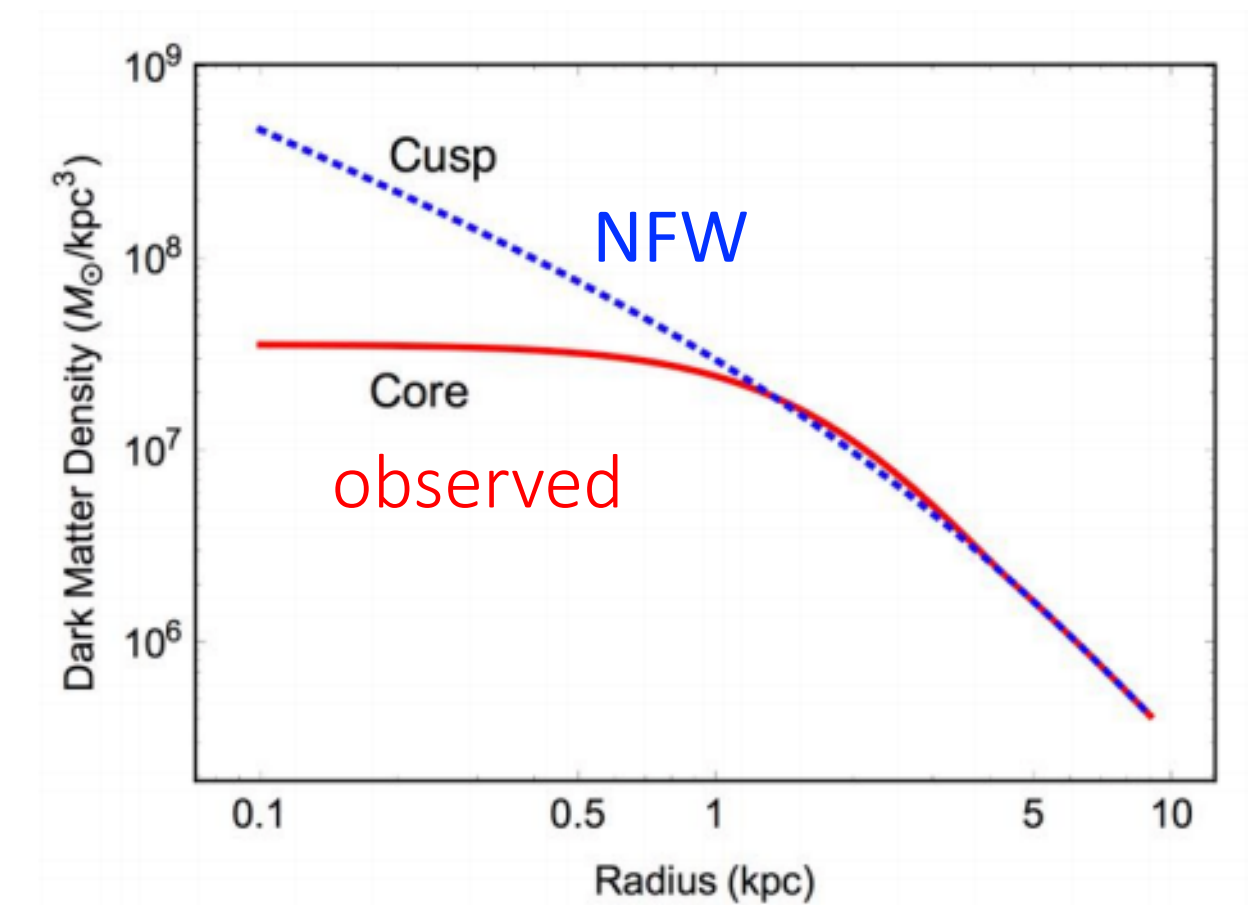
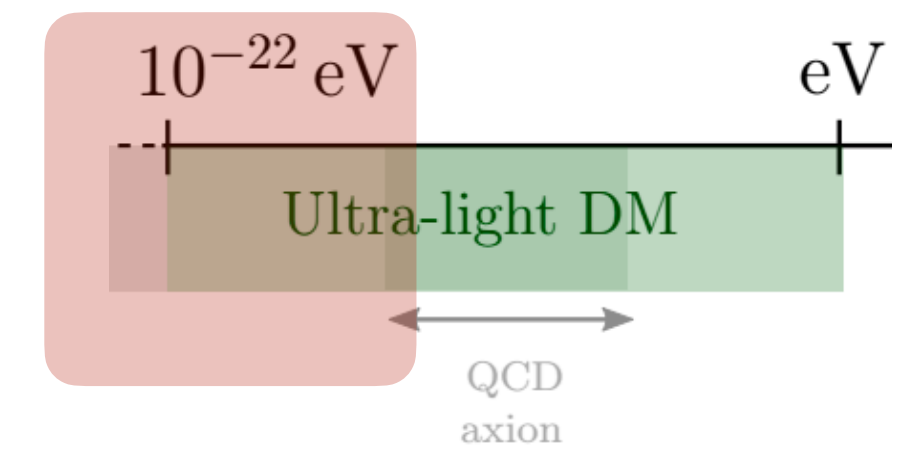


Phenomenology

Formation of **cores**



$$\rho(r) \simeq \begin{cases} \rho_c & \text{for } r \leq r_c \\ \rho_{\text{NFW}} & \text{for } r \geq r_c \end{cases}$$



FDM From simulations Schive et al. 2014, fitting function: Stable core solution

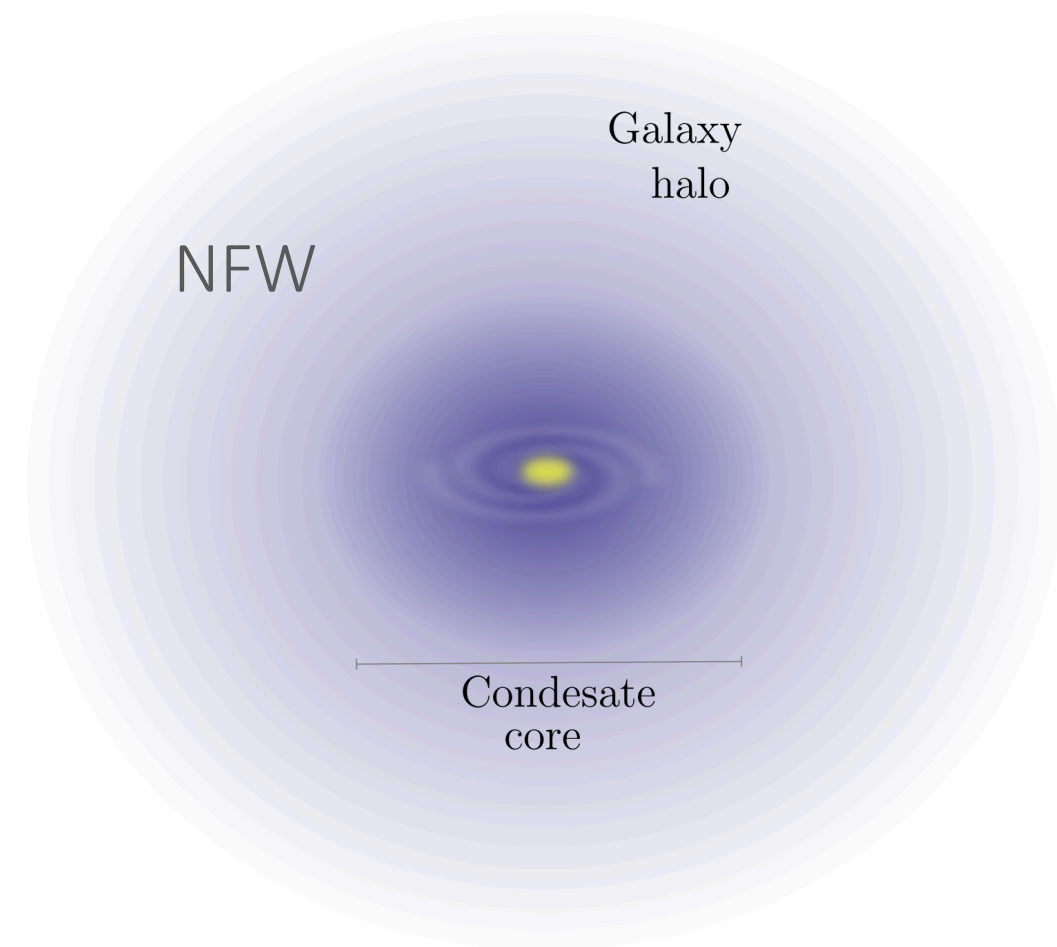
$$\rho_c \simeq \frac{1.9 \times 10^{-2}}{[1 + 0.091 (r/R_{1/2,c})^2]^8} \left(\frac{m}{10^{-22} \text{ eV}} \right)^{-2} \left(\frac{r_c}{\text{kpc}} \right)^{-4} M_{\odot} \text{ pc}^{-3},$$

$$r_c \simeq 0.16 \left(\frac{m}{10^{-22} \text{ eV}} \right)^{-1} \left(\frac{M}{10^{12} M_{\odot}} \right)^{-1/3} \text{ kpc}.$$

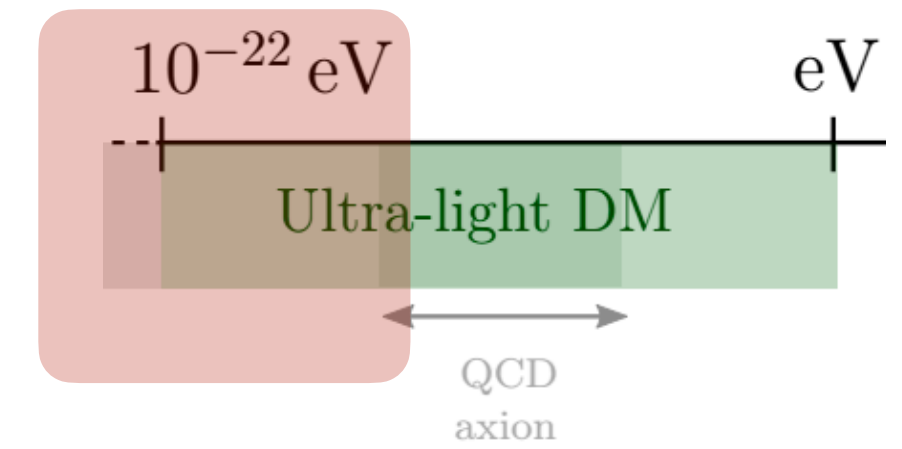
Relations used to compare with **observations**

Phenomenology

Formation of **cores**



$$\rho(r) \simeq \begin{cases} \rho_c & \text{for } r \leq r_c \\ \rho_{\text{NFW}} & \text{for } r \geq r_c \end{cases}$$

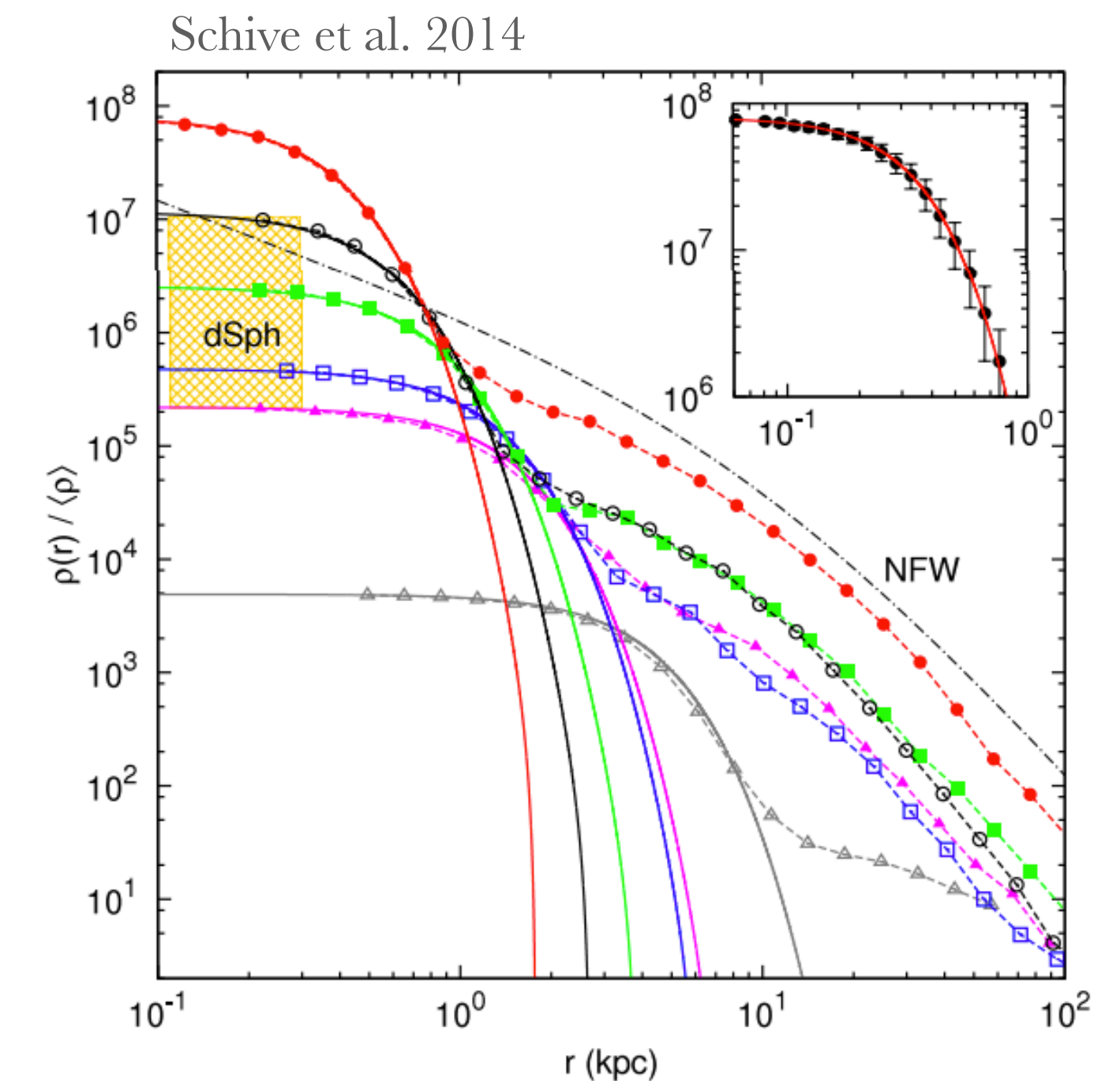


FDM

From simulations Schive et al. 2014, fitting function: Stable core solution

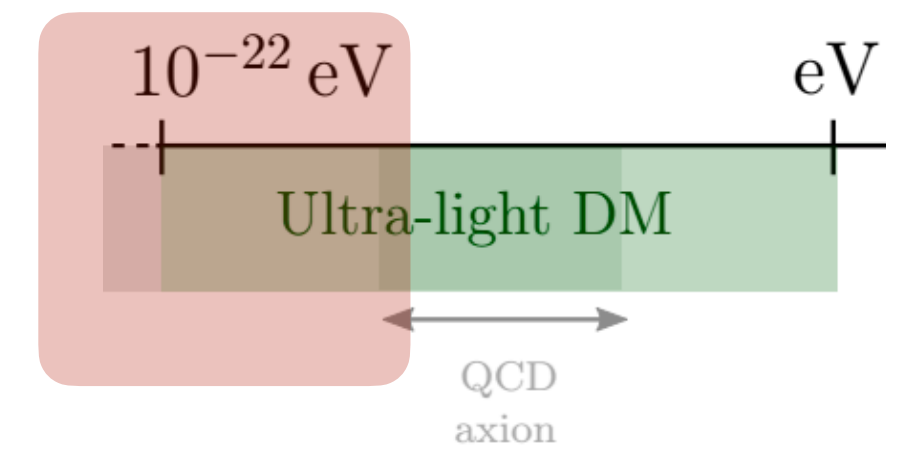
$$\rho_c \simeq \frac{1.9 \times 10^{-2}}{[1 + 0.091 (r/R_{1/2,c})^2]^8} \left(\frac{m}{10^{-22} \text{ eV}} \right)^{-2} \left(\frac{r_c}{\text{kpc}} \right)^{-4} M_\odot \text{ pc}^{-3},$$

$$r_c \simeq 0.16 \left(\frac{m}{10^{-22} \text{ eV}} \right)^{-1} \left(\frac{M}{10^{12} M_\odot} \right)^{-1/3} \text{ kpc}.$$



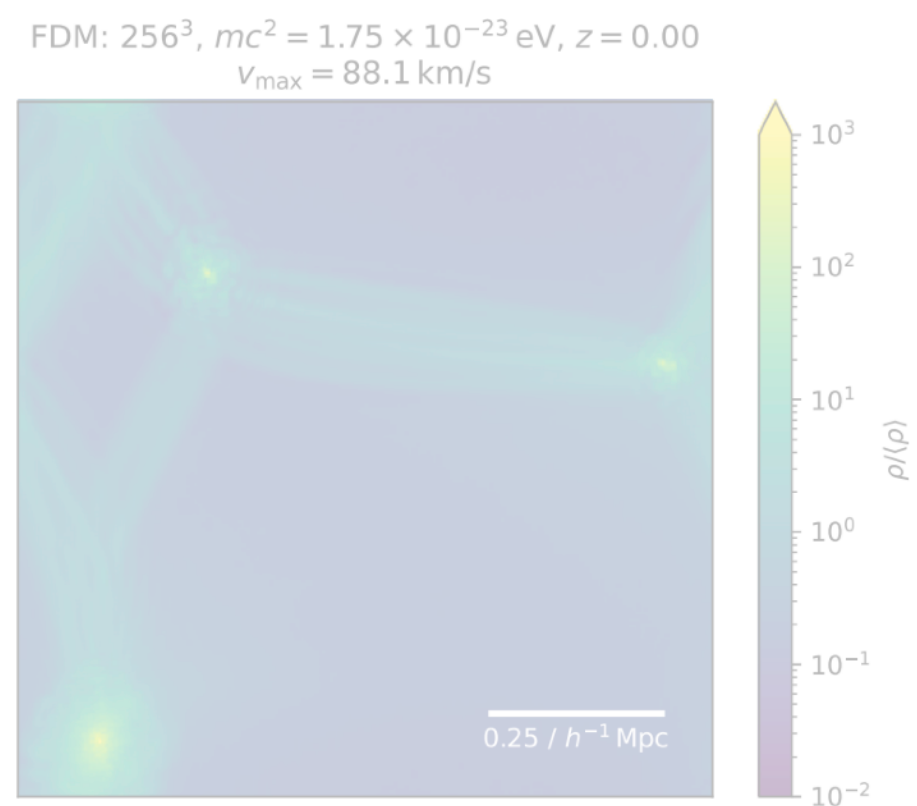
Relations used to compare with **observations**

Phenomenology

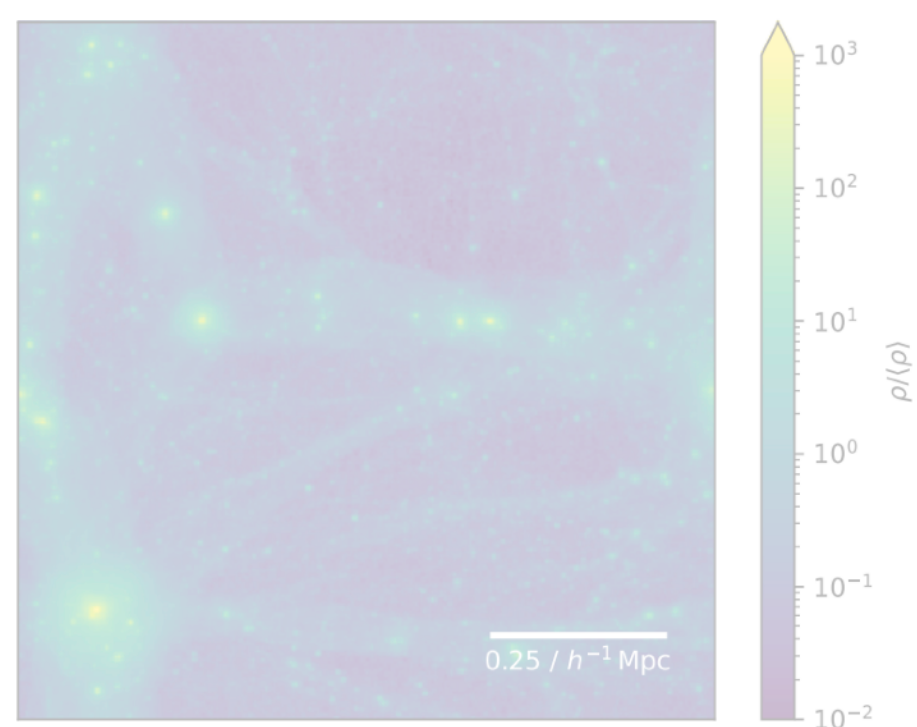


RICH PHENOMENOLOGY ON SMALL SCALES

Suppression of small structures

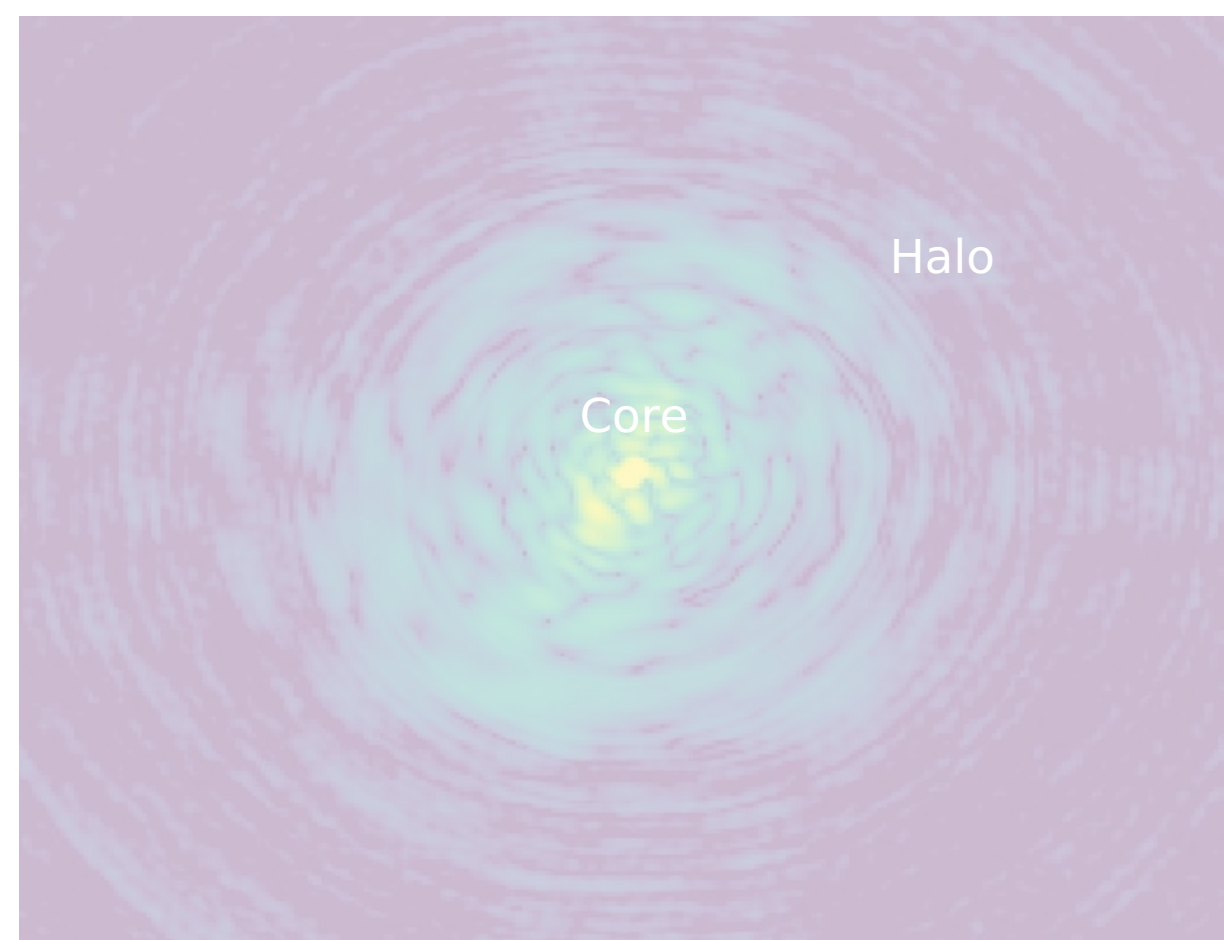


CDM: 256^3 , $z = 0.00$

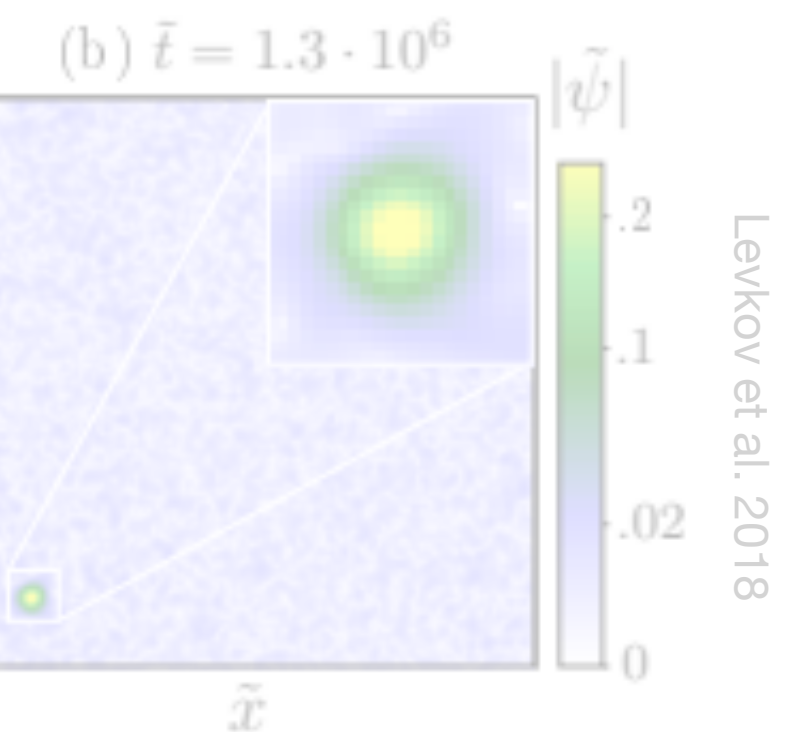


S. May et al. 2021

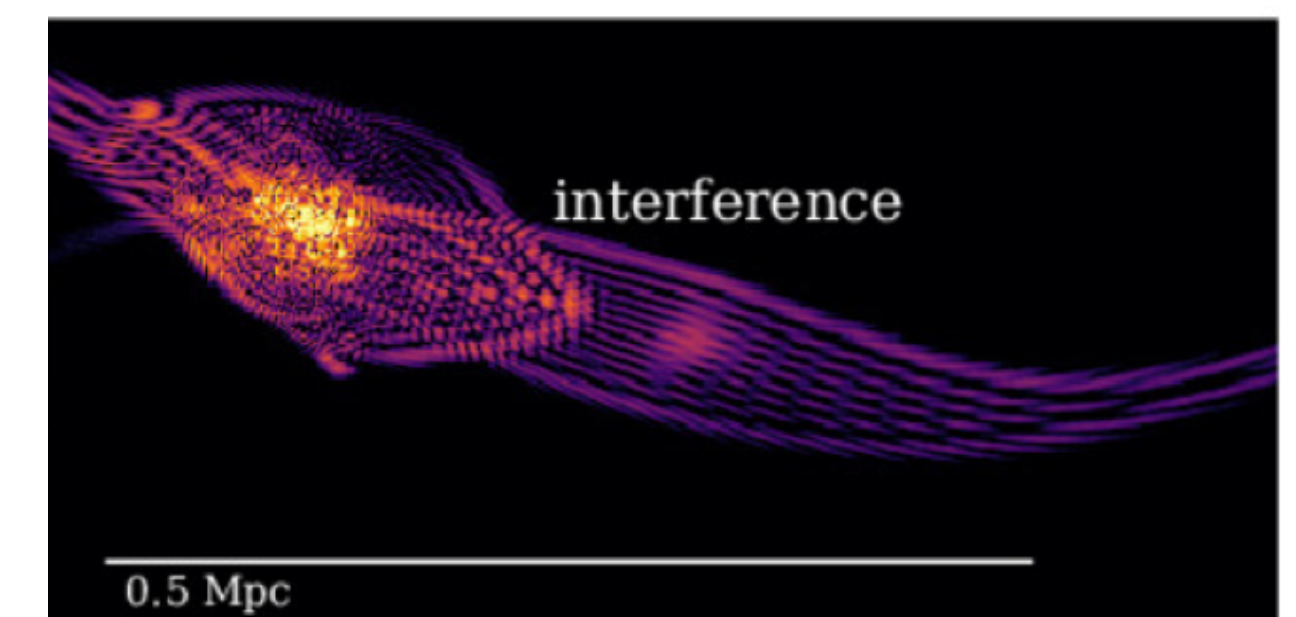
Formation of a solitonic core



Dynamical effects



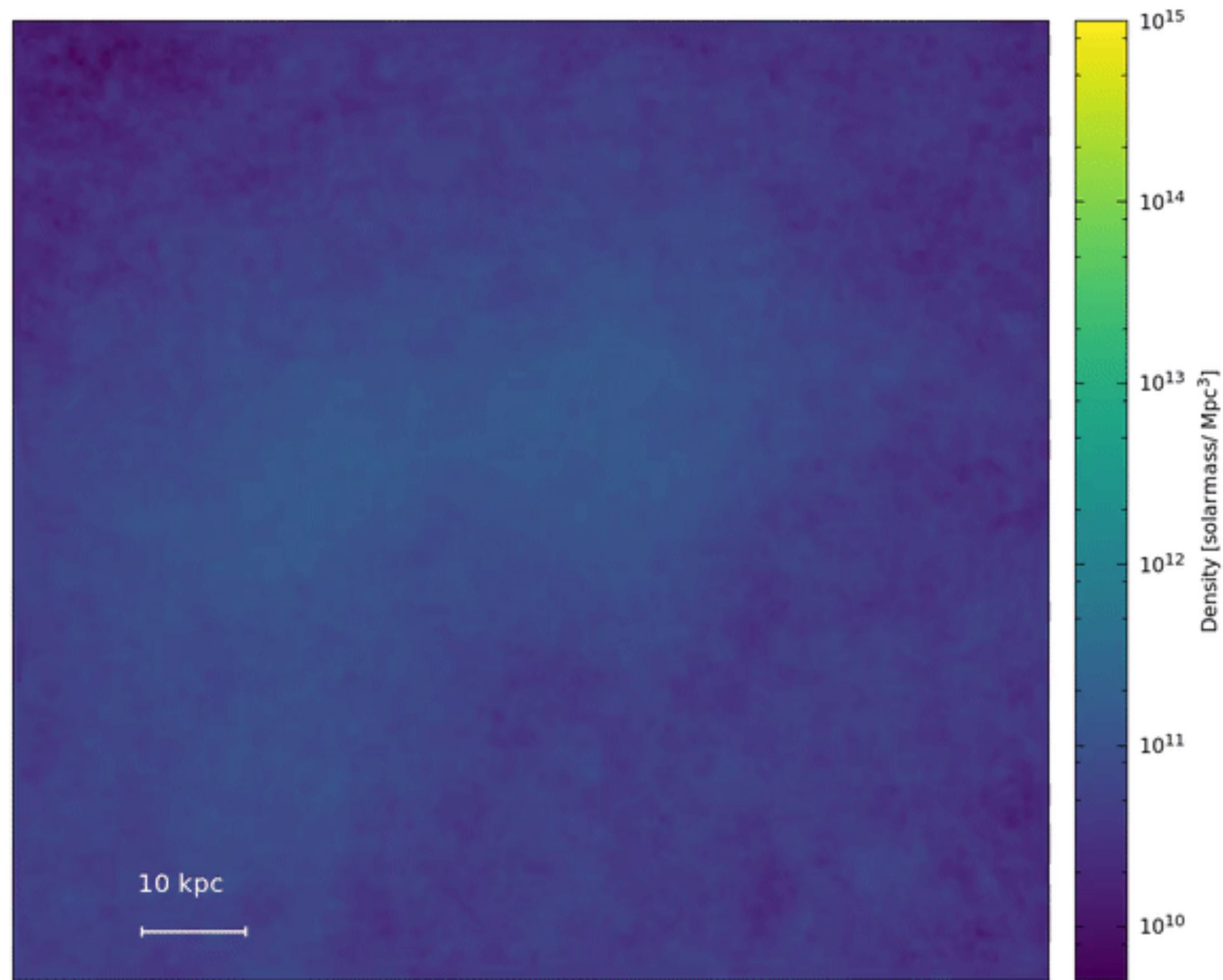
Wave interference



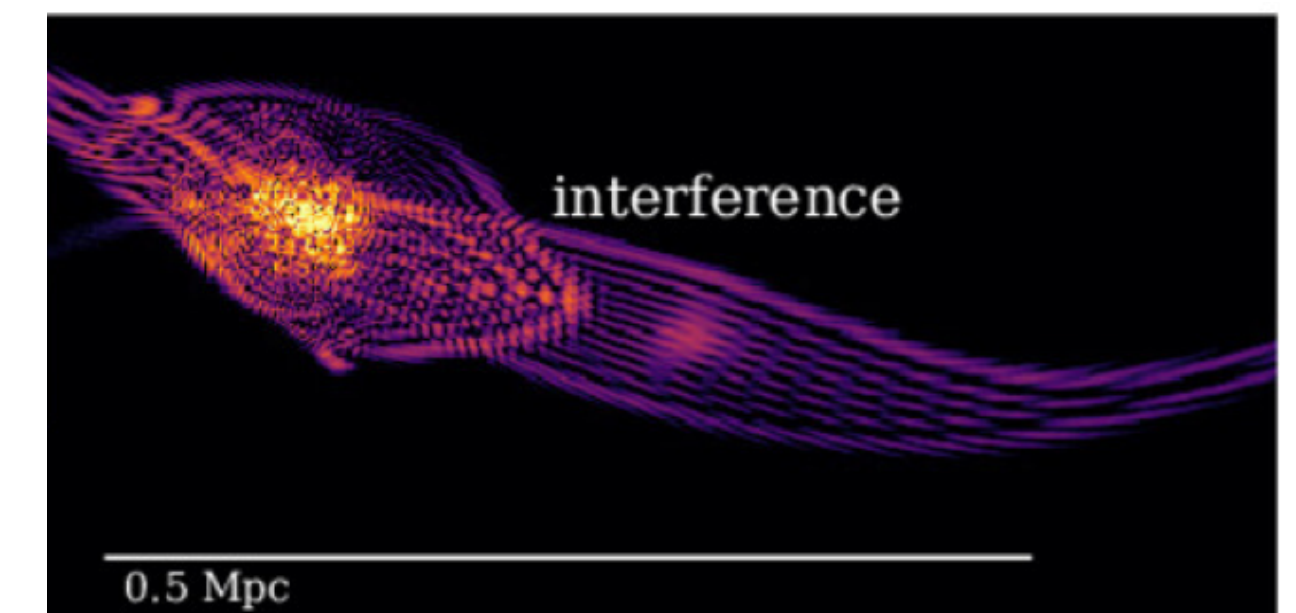
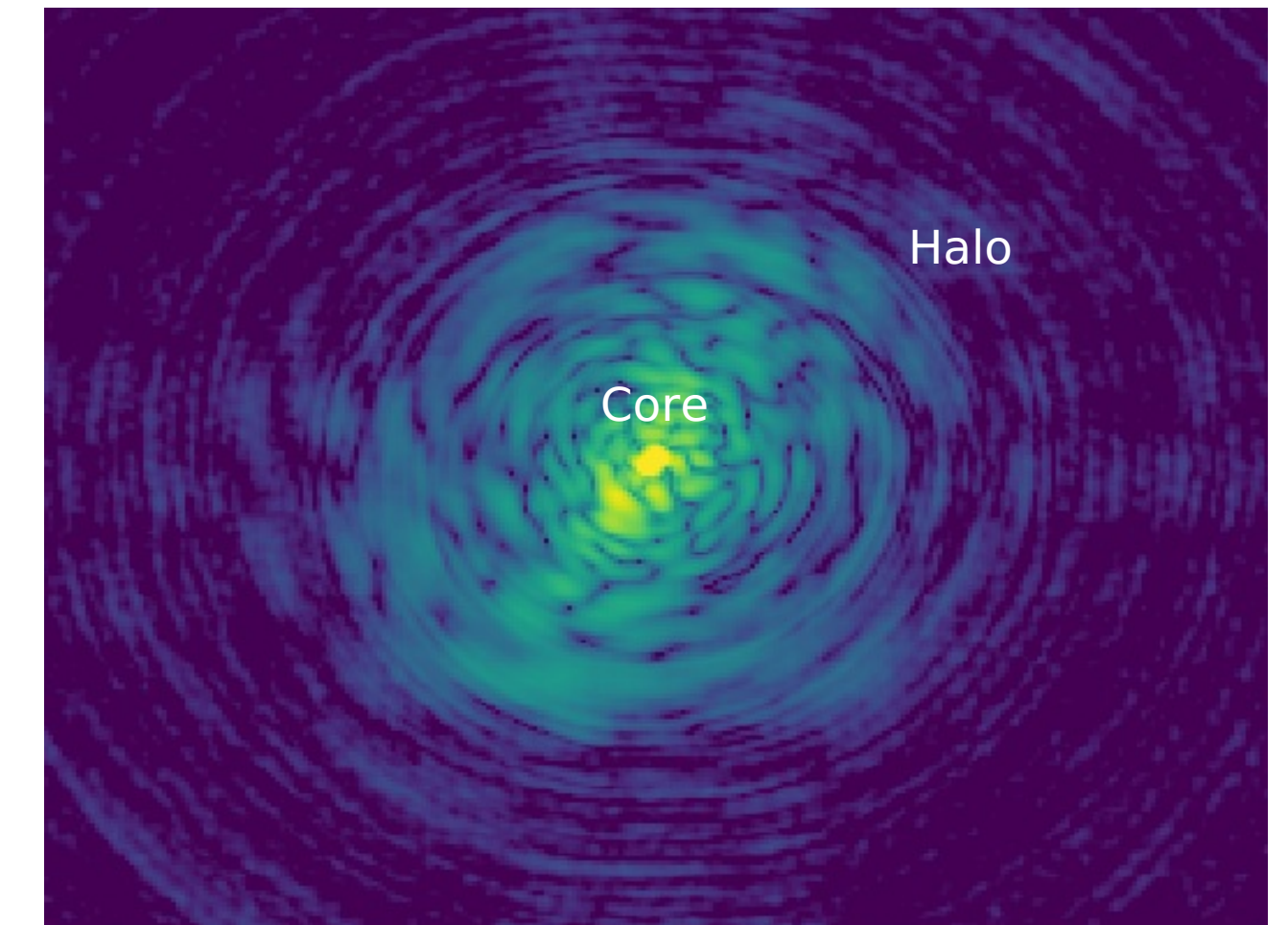
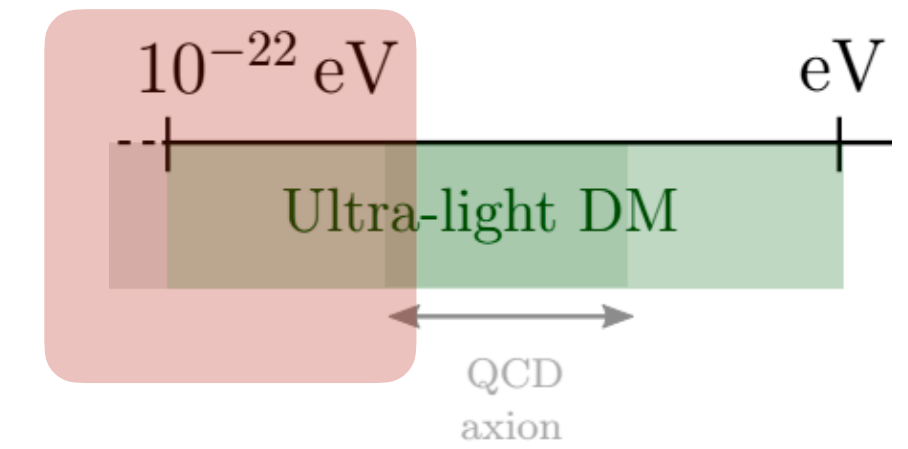
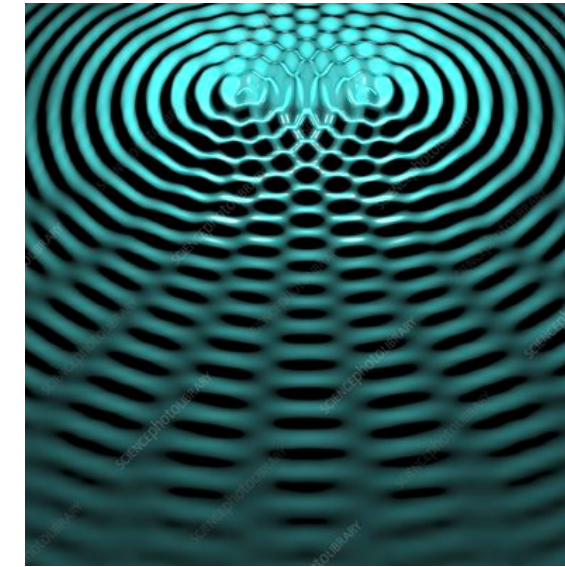
Mocz et al. 2017

Phenomenology

Wave interference: granules and vortices



Simulation by Jowett Chan



Mocz et al. 2017

Order one fluctuations in density \longrightarrow

Constructive interference: **granules**

Destructive interference

$\sim \lambda_{dB}$

Phenomenology

Vortices

Vortices are sites where the fluid velocity has a non-vanishing curl

Two ways:

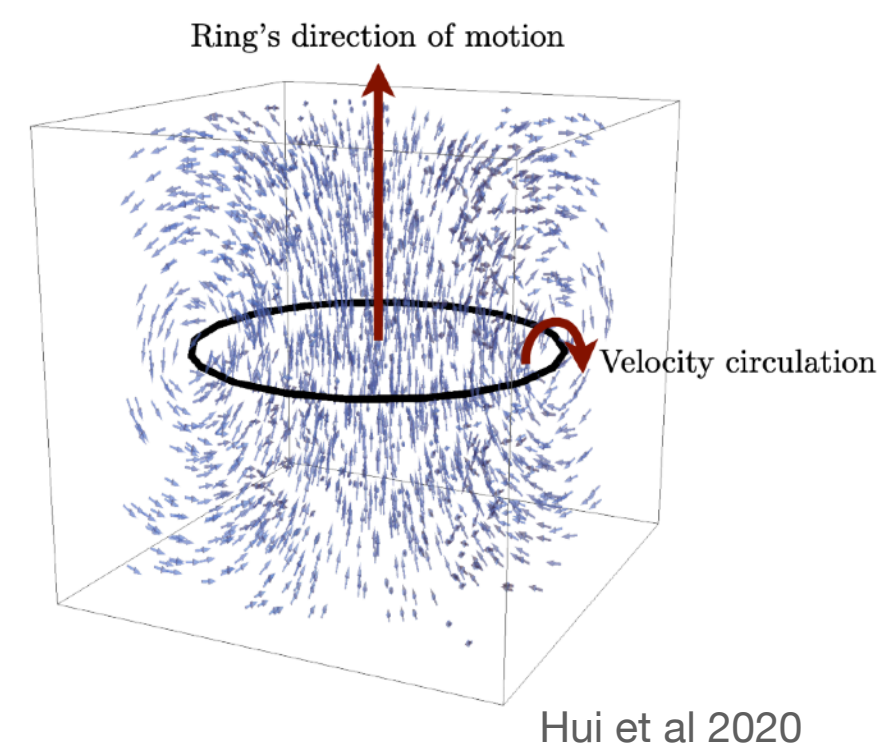
- regions where the density vanishes
- transfer of angular momentum (superfluids only)

Fuzzy DM

Interference of waves leads to **vortices** - where there is **destructive interference**

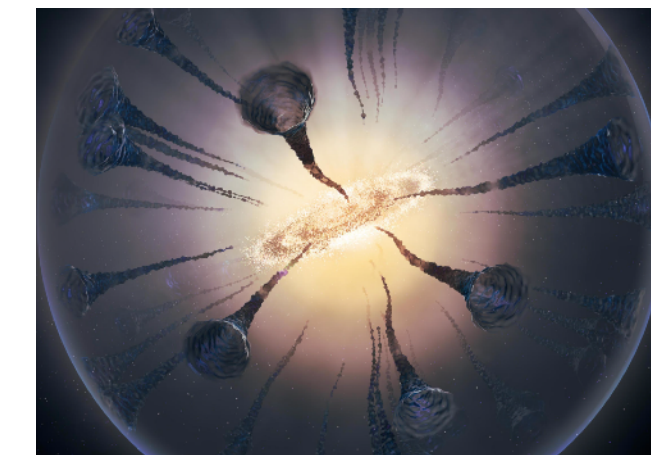
General defect in 3D

$$c = \frac{1}{m} \oint_{\partial A} d\theta = \frac{2\pi n}{m}$$



$$(\psi \equiv \sqrt{\rho/m} e^{i\theta} \text{ and } \mathbf{v} \equiv \nabla\theta/m)$$

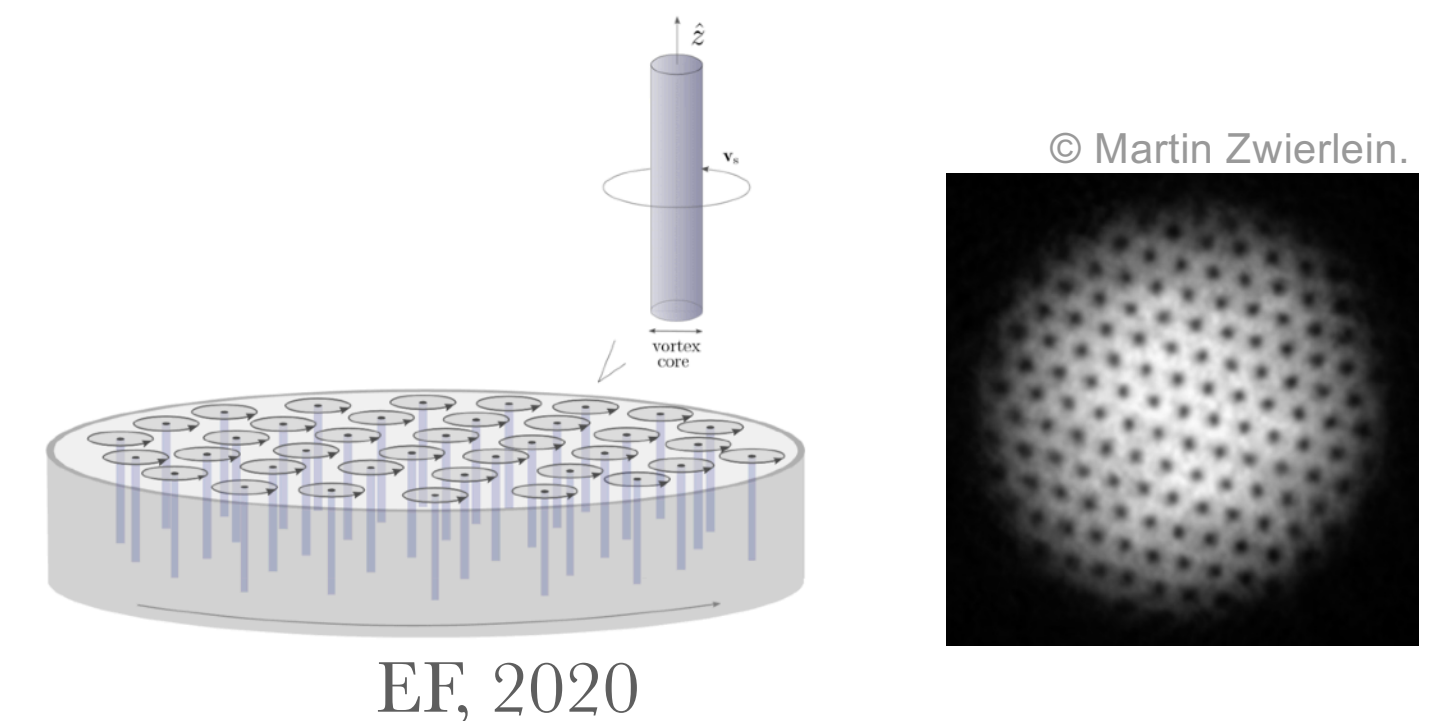
Vel. field is a gradient flow \rightarrow irrotational fluid, no vorticity



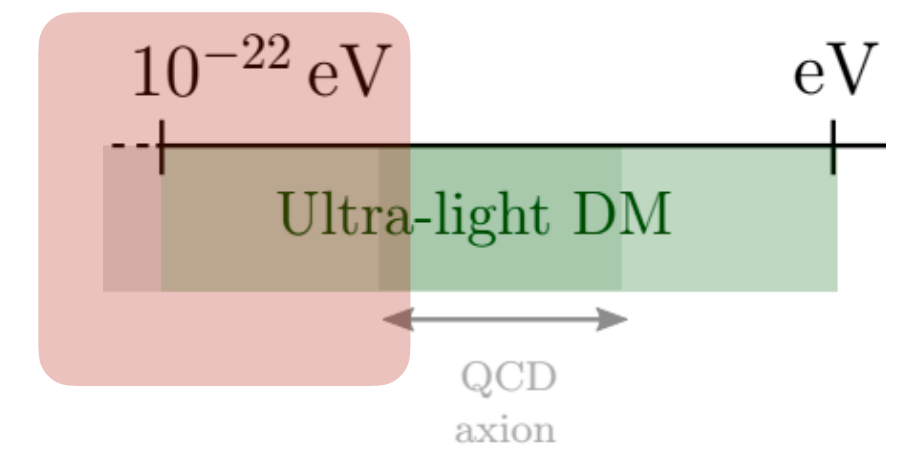
Quanta magazine

Self-interacting Fuzzy DM

Superfluid cannot rotate uniformly. If the superfluid rotates faster than the critical vel., network of vortices are formed.

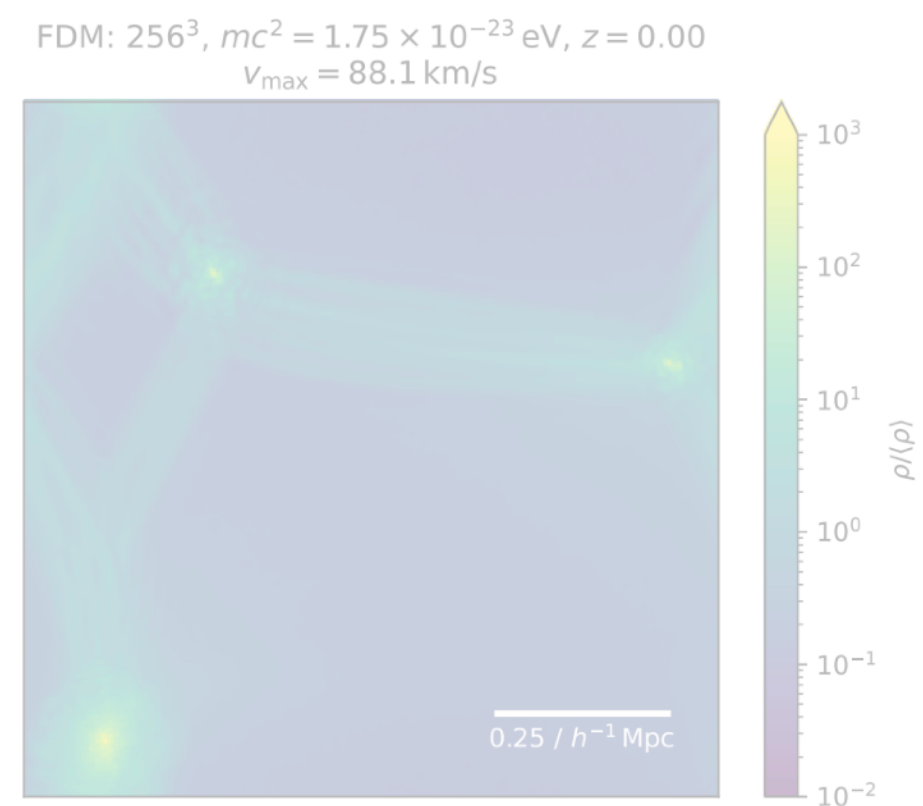


Phenomenology

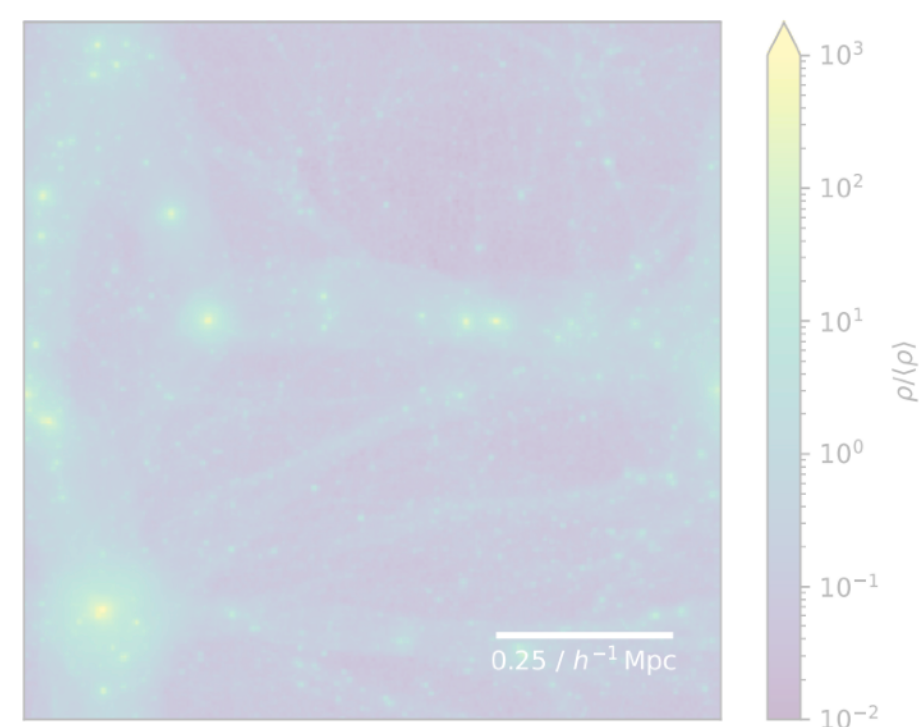


RICH PHENOMENOLOGY ON SMALL SCALES

Suppression of small structures

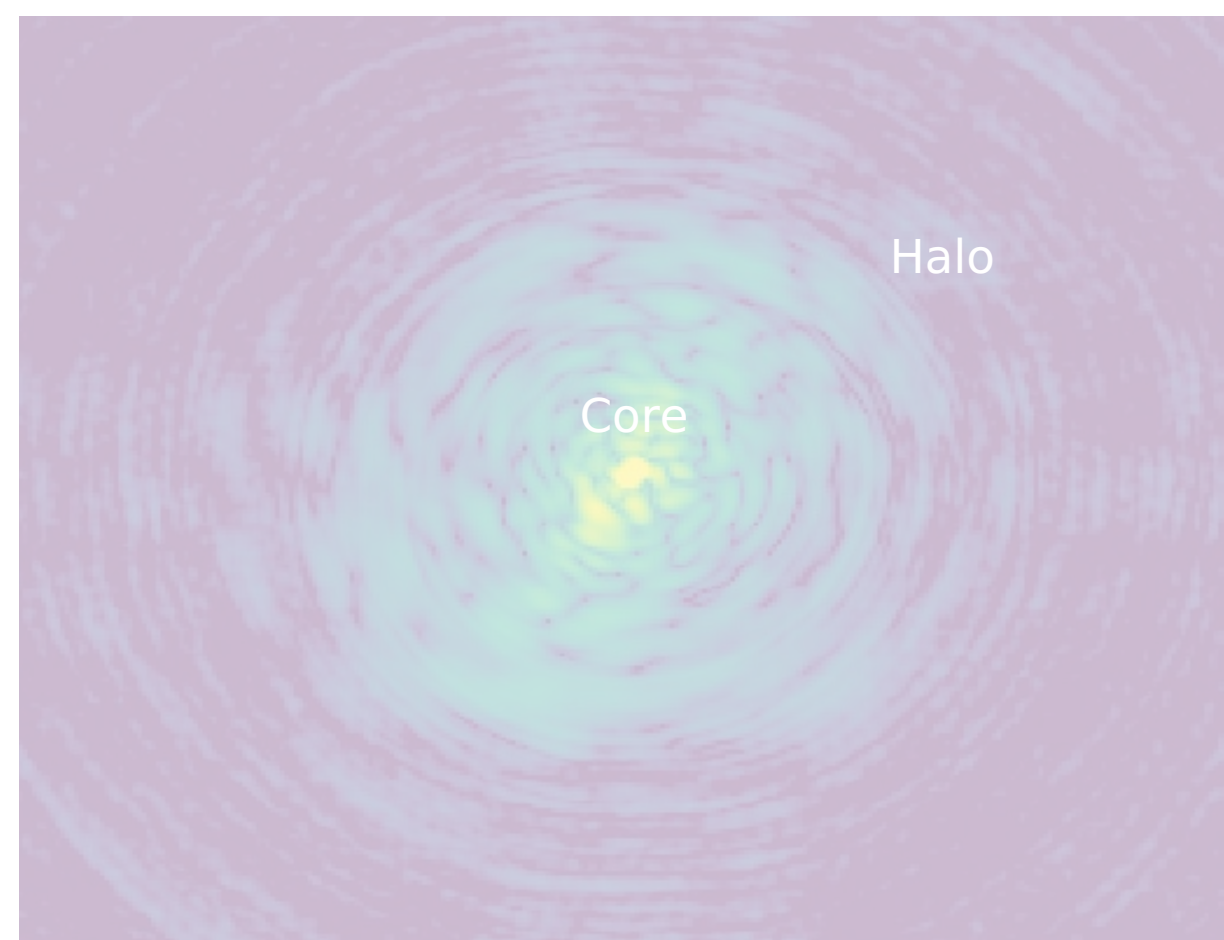


CDM: 256^3 , $z = 0.00$

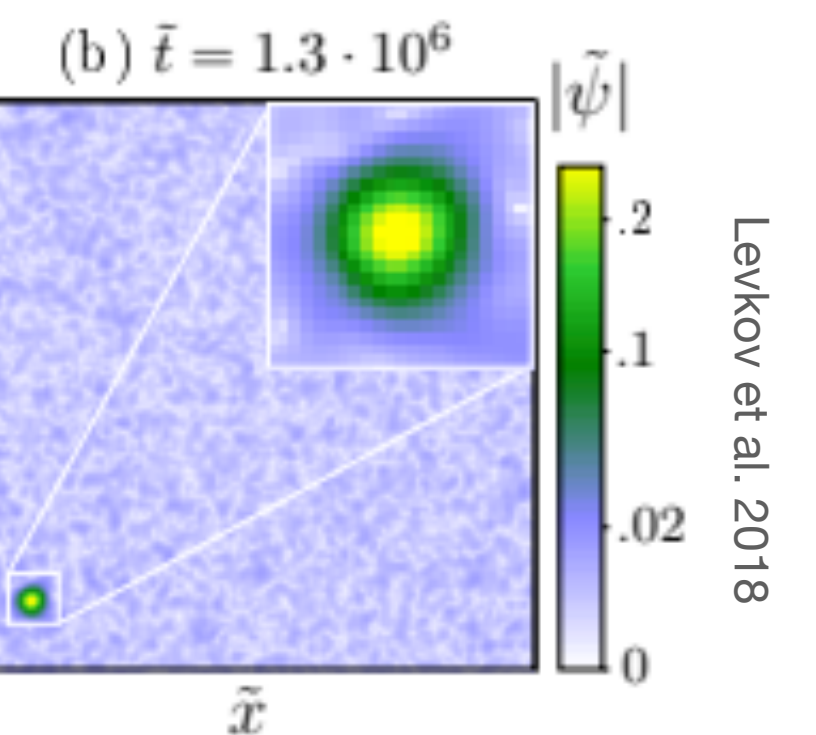


S. May et al. 2021

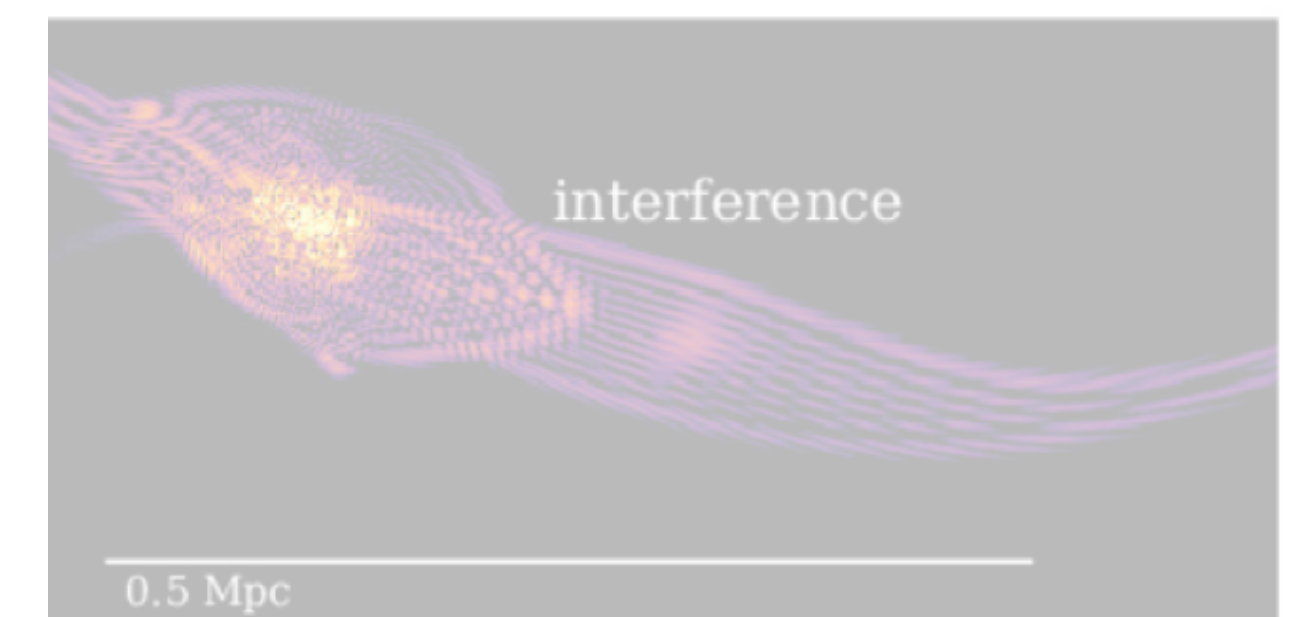
Formation of a solitonic core



Dynamical effects



Wave interference

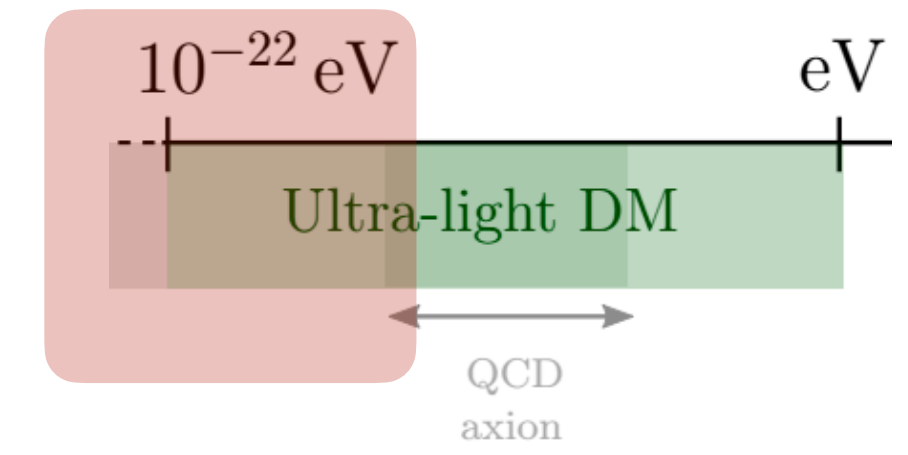


Mocz et al. 2017

Phenomenology

Dynamical effects

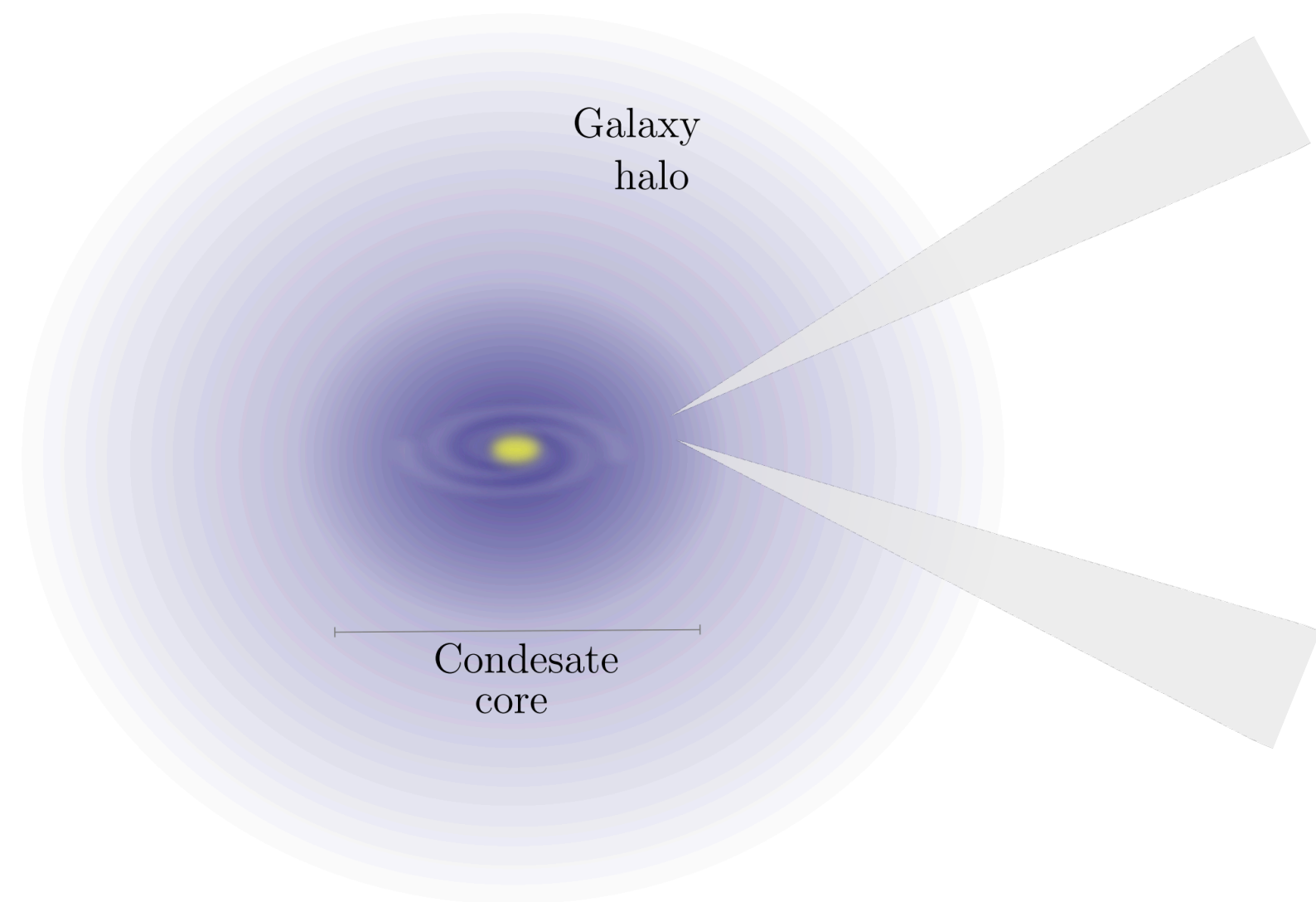
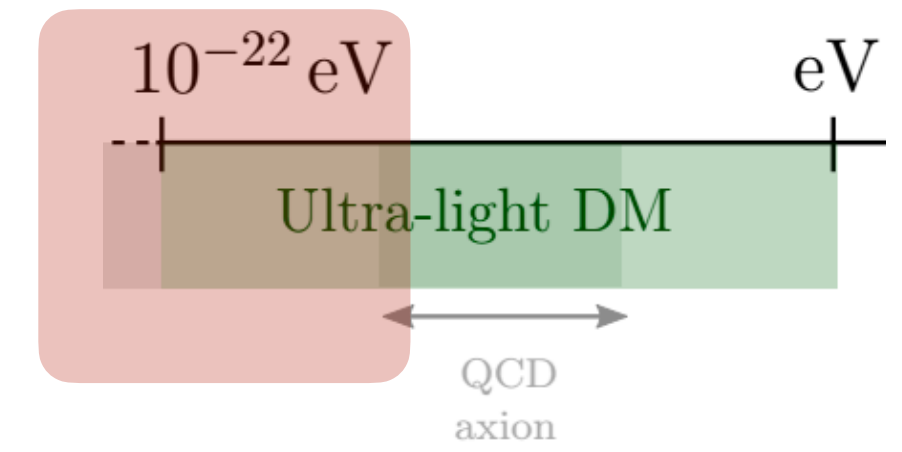
Relaxation, oscillation, friction, and heating



Phenomenology

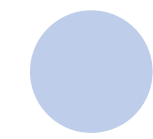
Dynamical effects

Relaxation, oscillation, friction, and heating



Heating

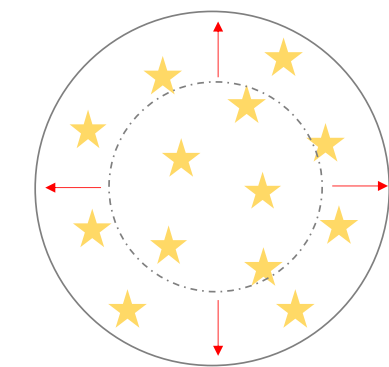
FDM granule



m_{eff}

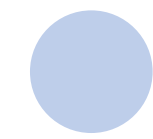


System (star)
gains energy



Friction

FDM granule



m_{eff}



Globular cluster

System (GC or BH)
loses energy

Phenomenology

Dynamical effects

Relaxation, oscillation, friction, and heating

—————> Condensation

Formation of a BEC / superfluid

- **Thermalization** (and **condensation**) *seem* to happen inside the galaxy!
Formation of a **soliton** (ground state) or **Bose star** in the interior of galaxies

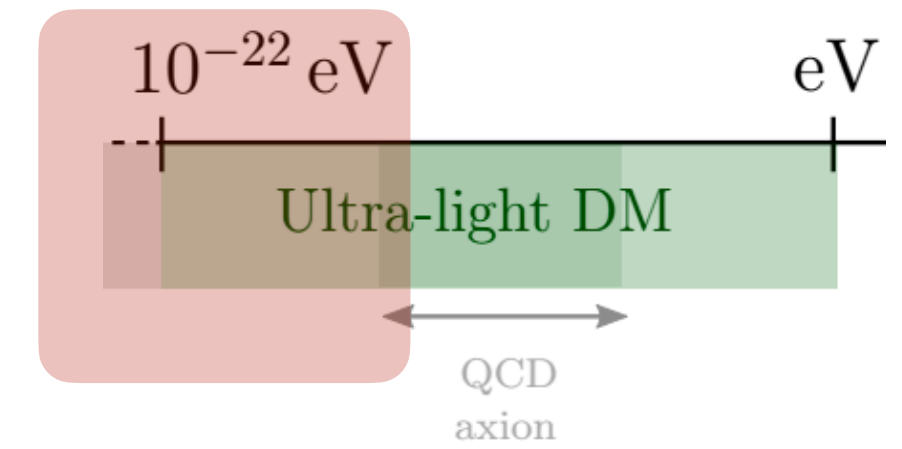
- Formation of a condensate and a core occur from **gravitational interaction**.

Condensation/relaxation time: $\tau_{\text{gr}} \gg \tau_{\text{int}}$

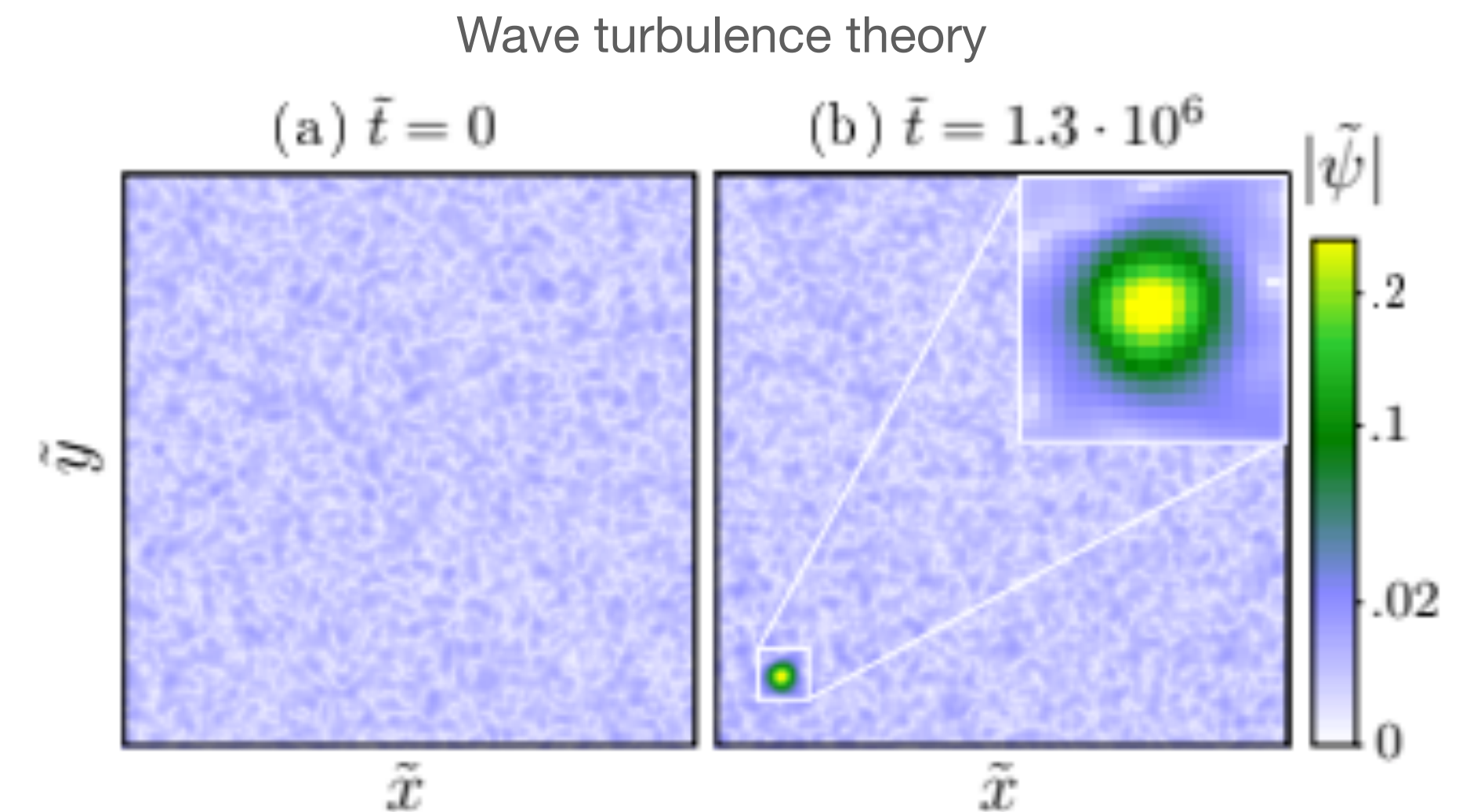
$$\tau_{\text{gr}} \sim 10^6 \text{ yr} \left(\frac{m}{10^{-22} \text{ eV}} \right)^3 \left(\frac{v}{30 \text{ km/s}} \right)^6 \left(\frac{\rho}{0.1 M_{\odot}/\text{pc}^3} \right)^{-2}$$

$$\tau_{\text{int}} = \frac{1}{\sqrt{8}|g|n}$$

Smaller than the age of the universe!



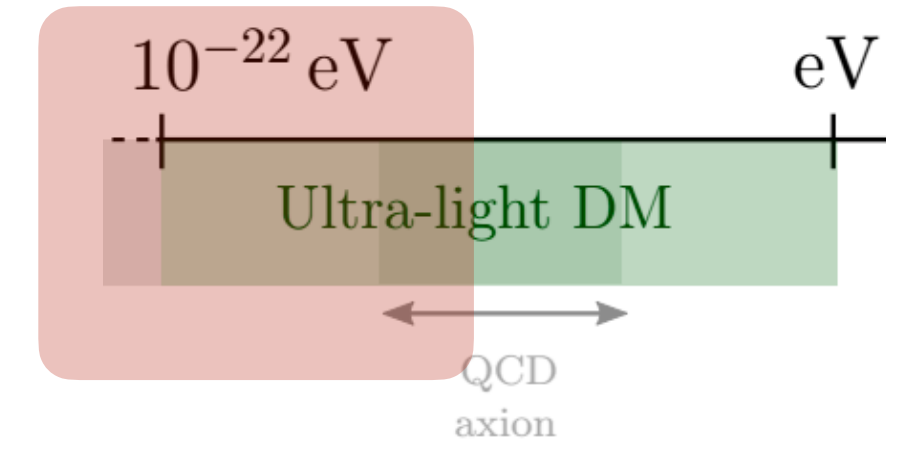
A. Guth M. Hertzberg, C. Prescod-Weinstein (2014)



Open question!

Levkov et al. 2018, Kirpatrick et al. 2020

Observational implications and constraints

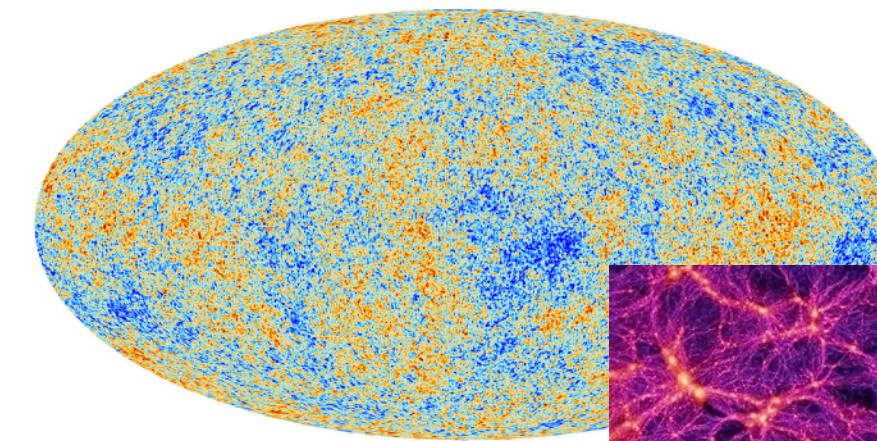


Galaxies

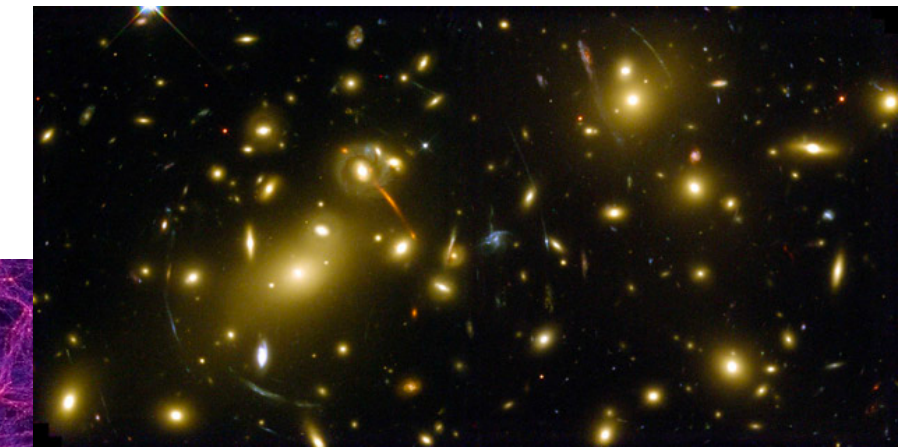


NASA and ESA

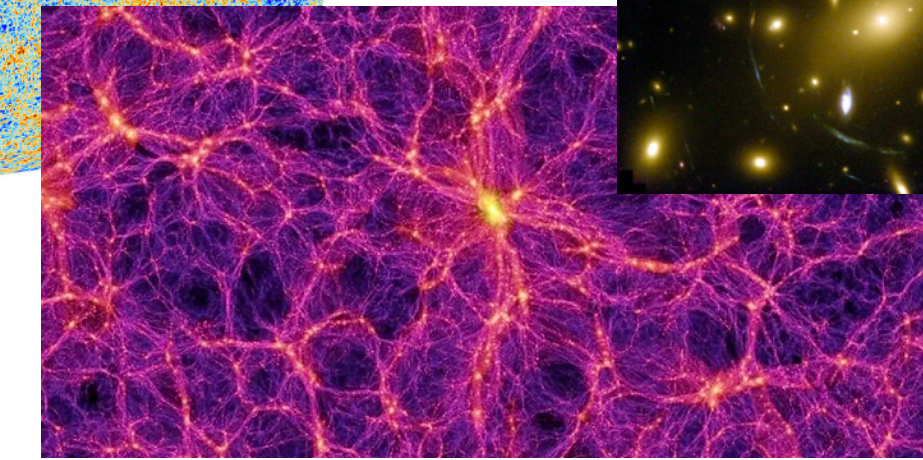
CMB+LSS



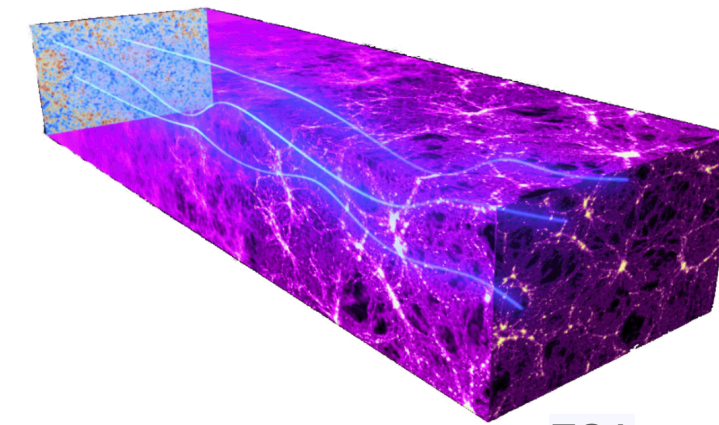
ESA and the Planck Collaboration



NASA and ESA

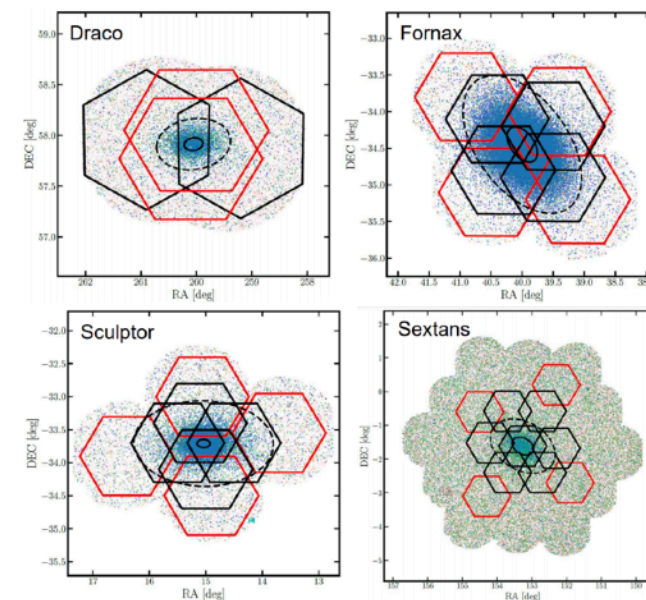


Springel & others / Virgo Consortium

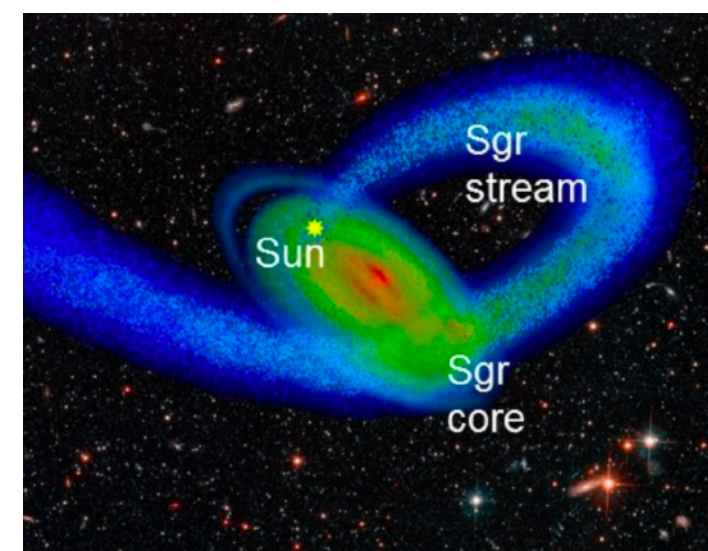


ESA

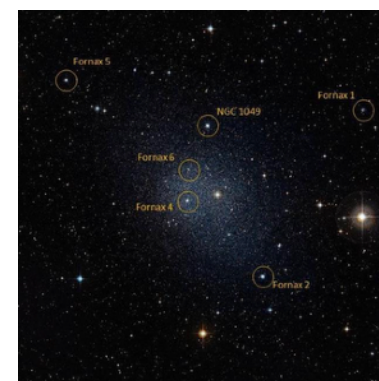
Dwarfs



Stellar stream



Globular clusters

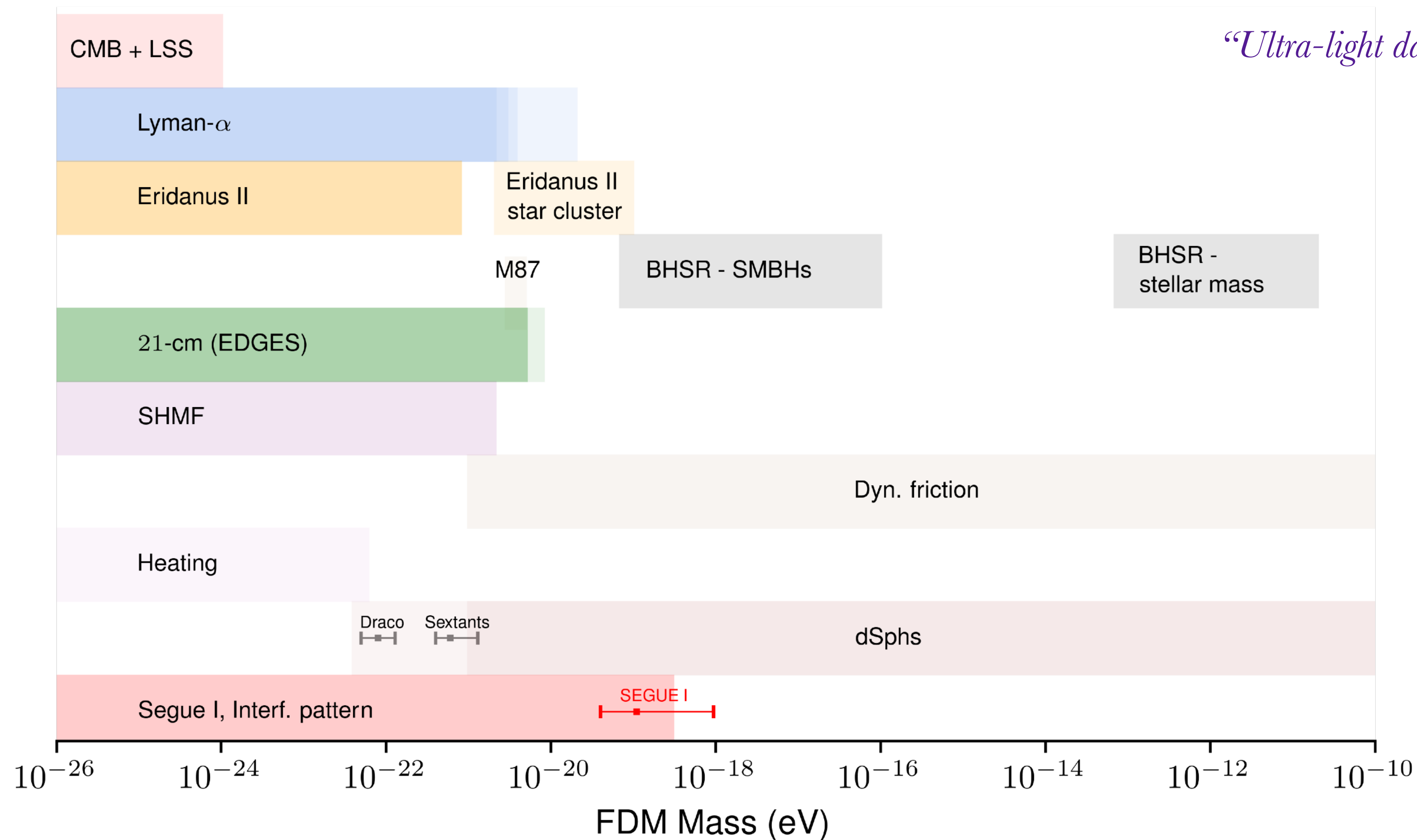
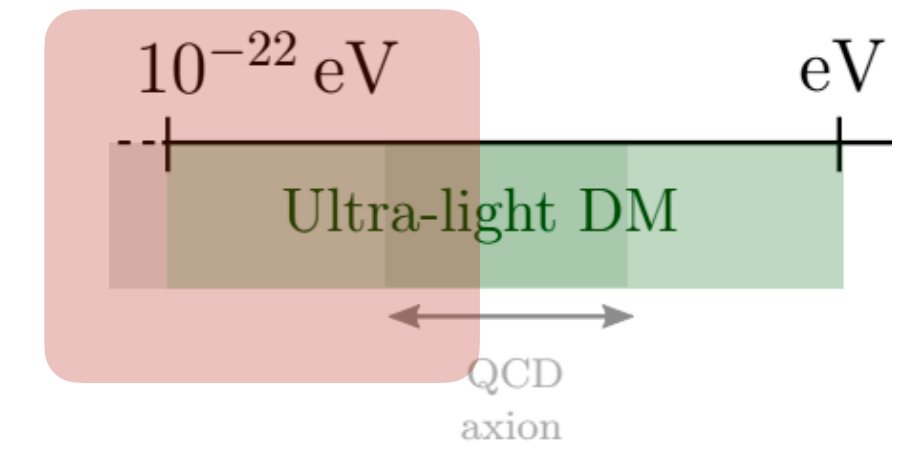


Clusters



Observational implications and constraints

Fuzzy Dark Matter - bounds on the mass

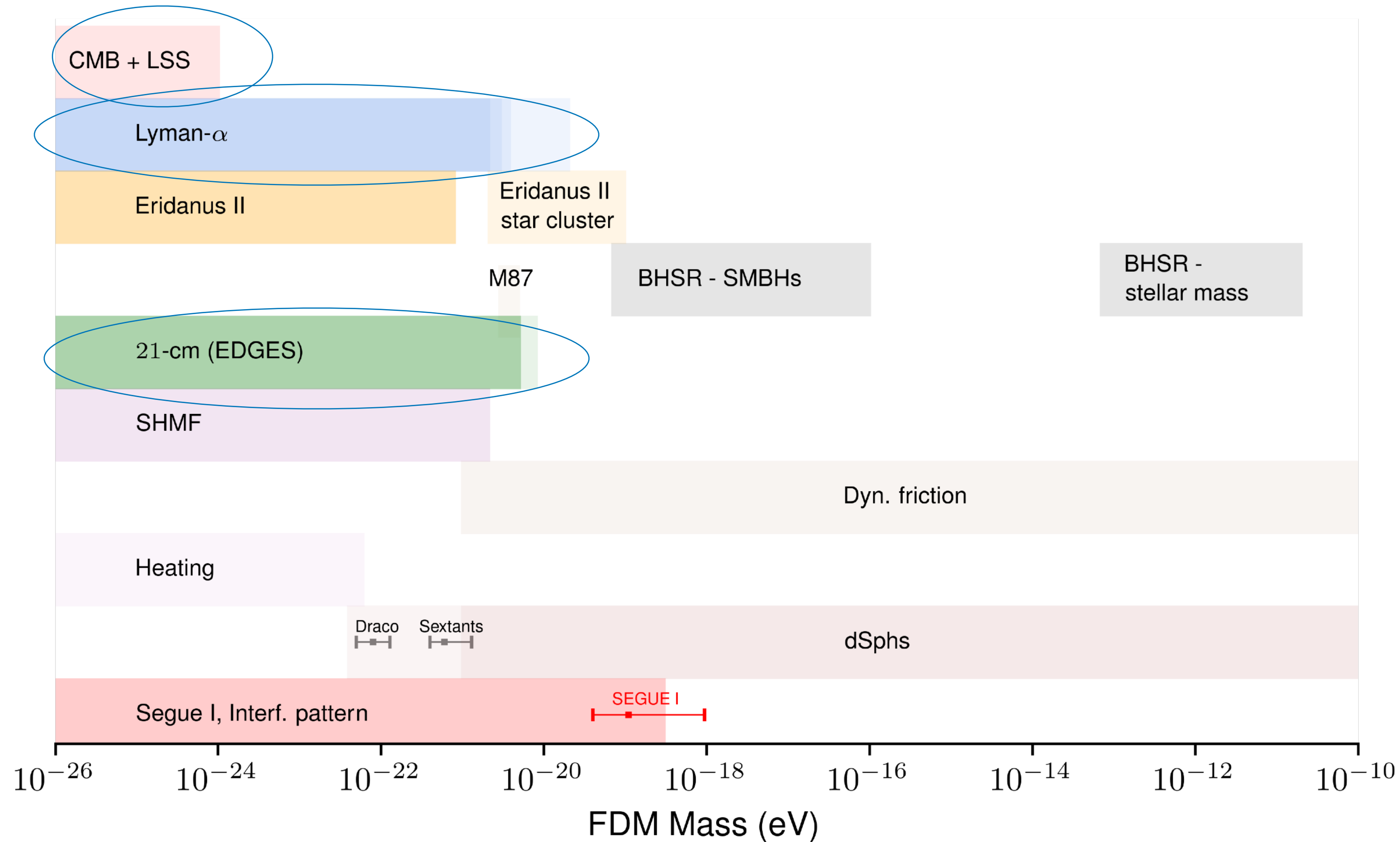
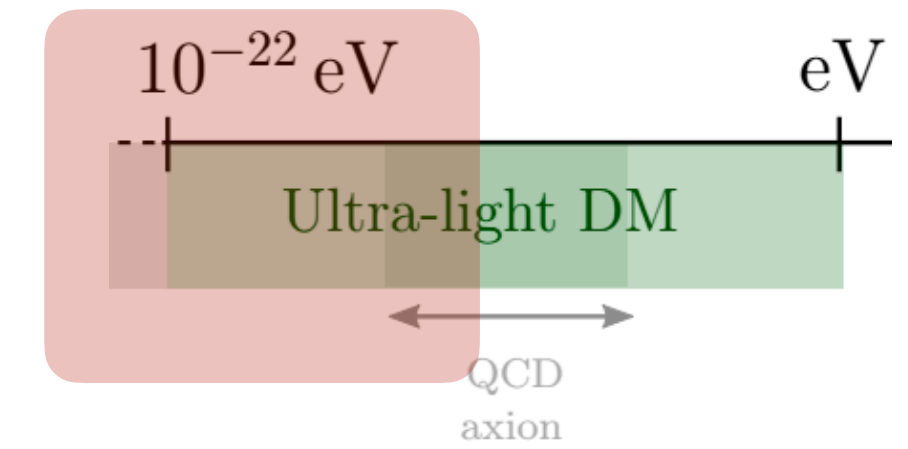


“Ultra-light dark matter”, E.F., 2020. The Astronomy and Astrophysics Review.

Bounds consider FDM is *all* DM

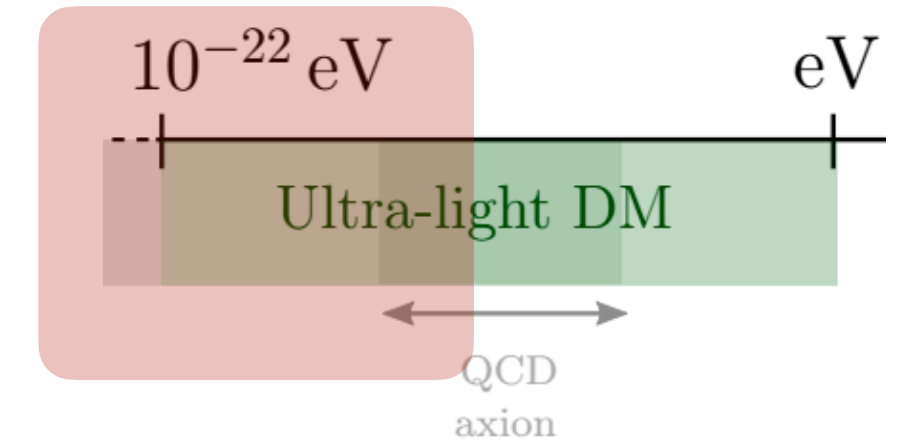
Observational implications and constraints

Fuzzy Dark Matter - bounds on the mass



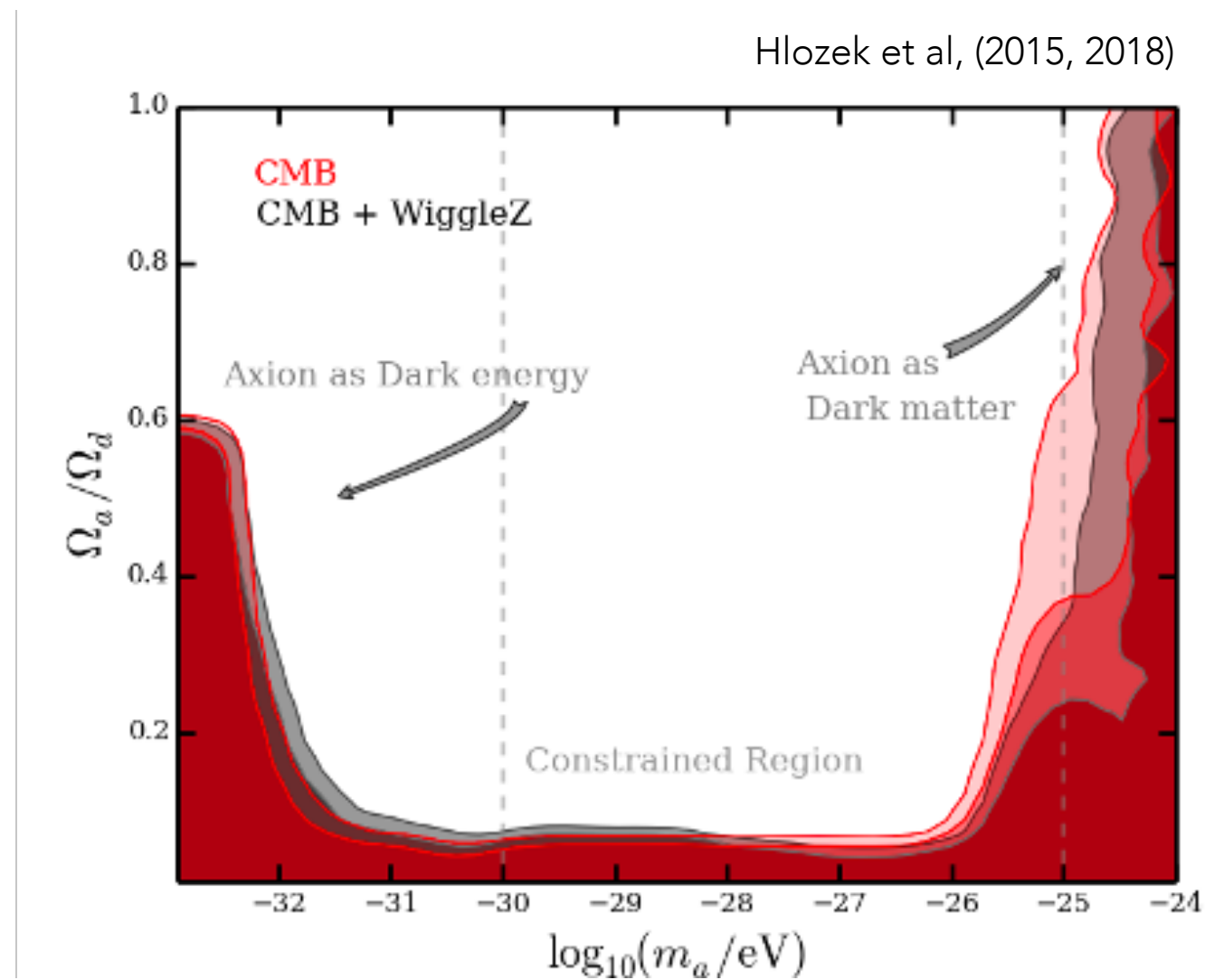
Observational implications and constraints

Fuzzy Dark Matter - bounds on the mass



Suppression of small structures

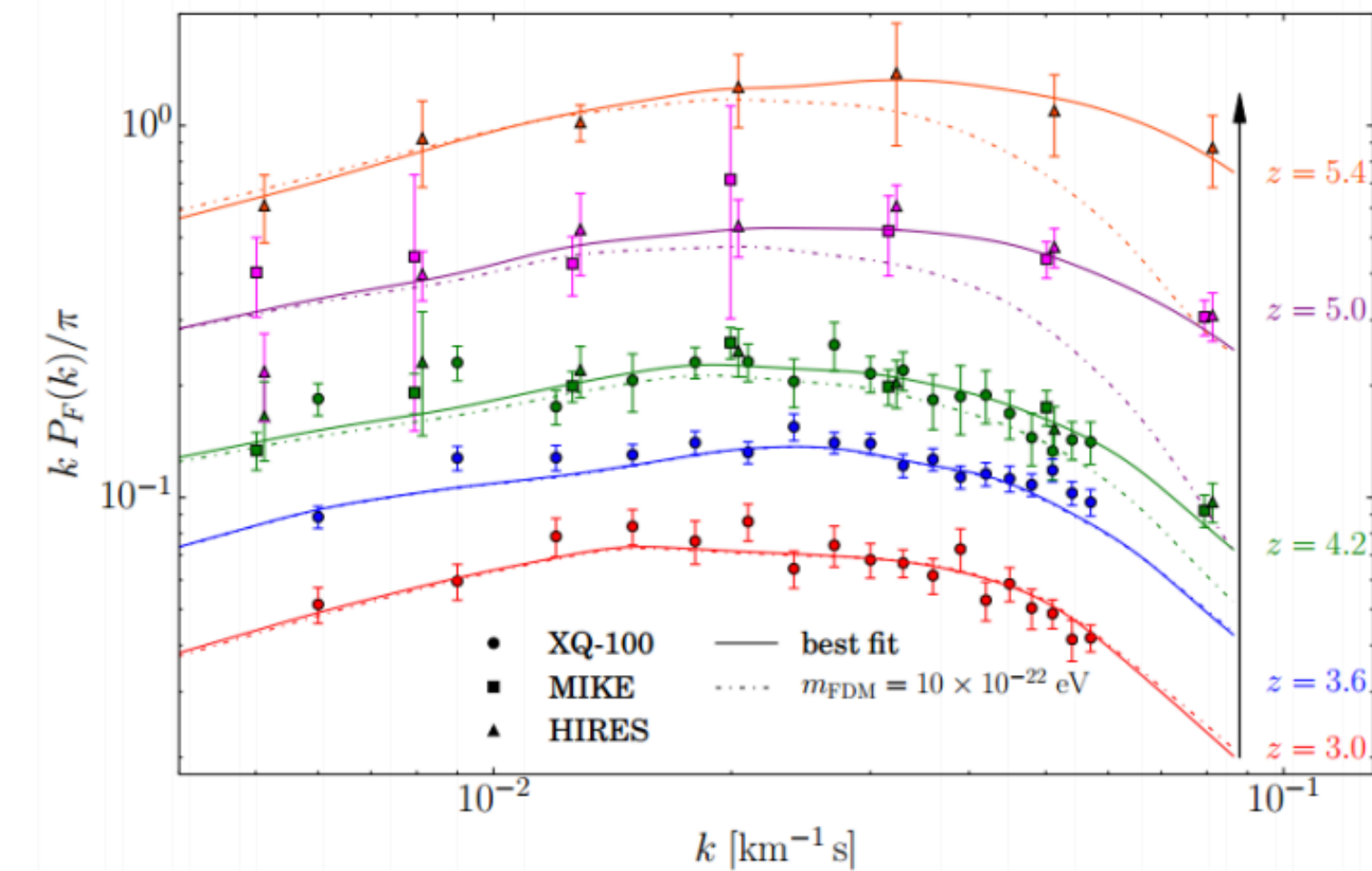
CMB/LSS



$$m \gtrsim 10^{-24} \text{ eV}$$

Lyman alpha

Armengaud et al. (2017); Iršič et al. (2017);
Rogers et al. (2020)

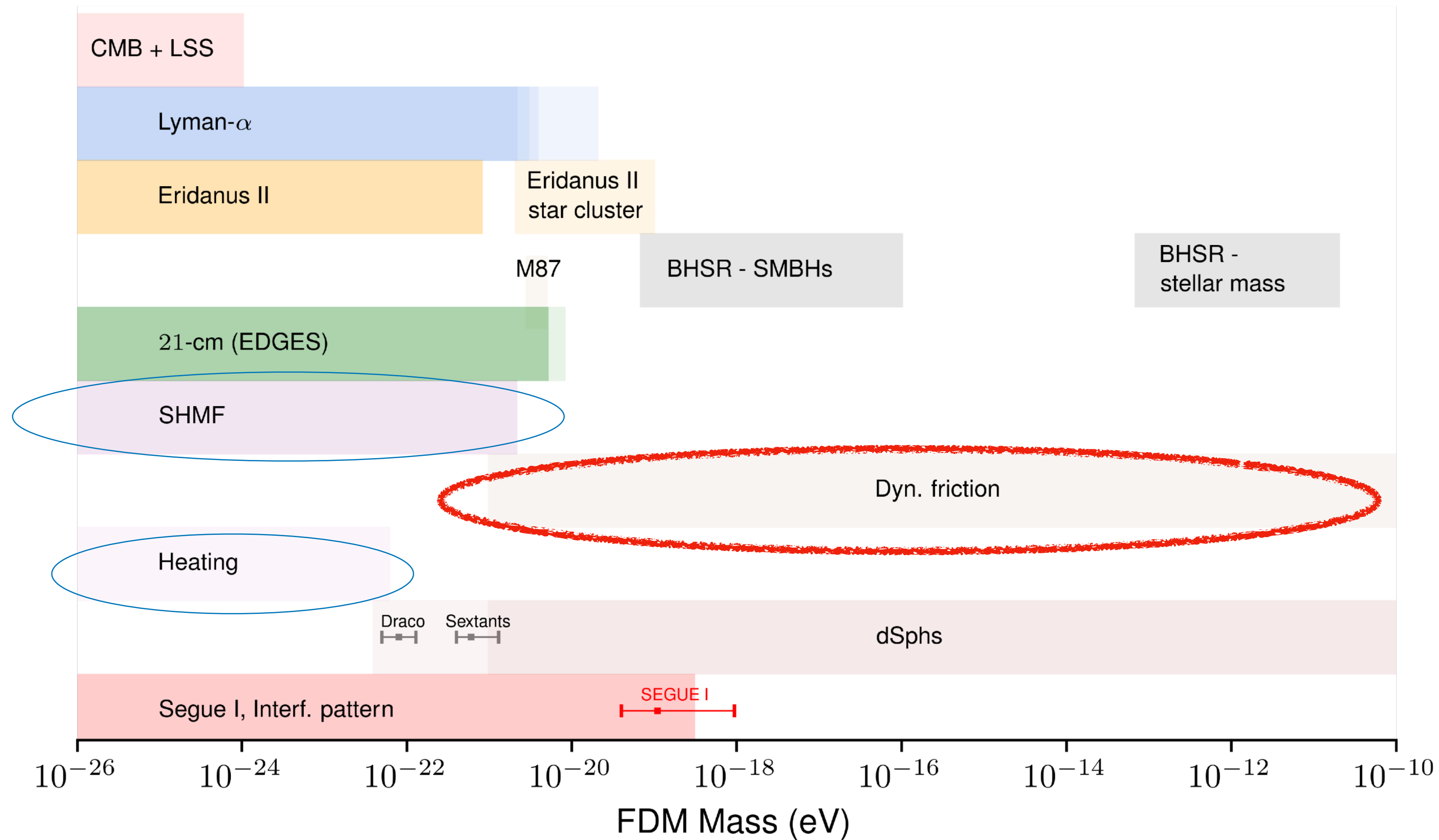


$$m \gtrsim 2 \times 10^{-20} \text{ eV}$$

so enough Mpc-scale power in Ly- α forest at $z = 5$.

Observational implications and constraints

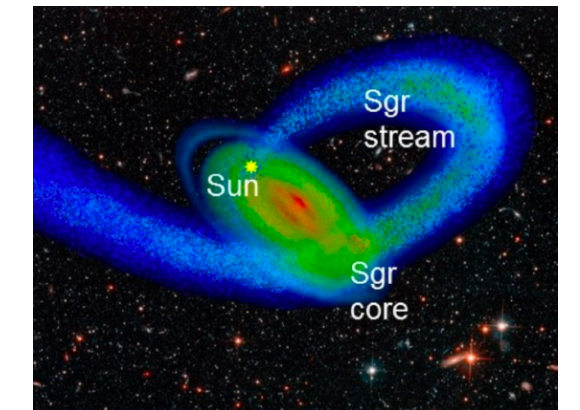
Fuzzy Dark Matter - bounds on the mass



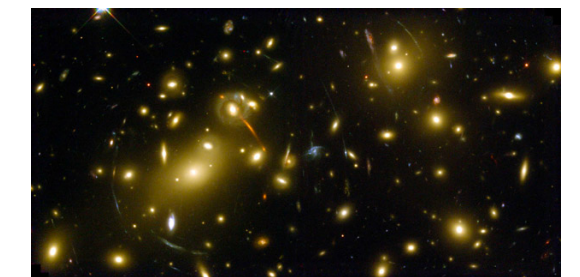
Suppression of small structures

Stellar streams

Schutz 2020: bound in the FDM SHMF using stellar streams and grav. lensing



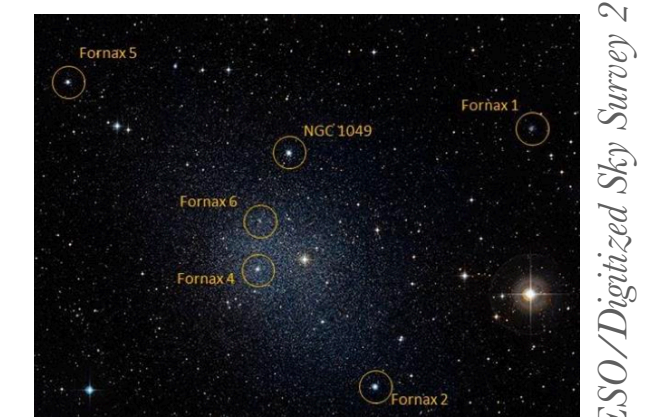
Grav. lensing



Dynamical effects

Globular clusters

$$m < 10^{-21} \text{ eV}$$



Lancaster et al. 2020

Heating of the MW disk

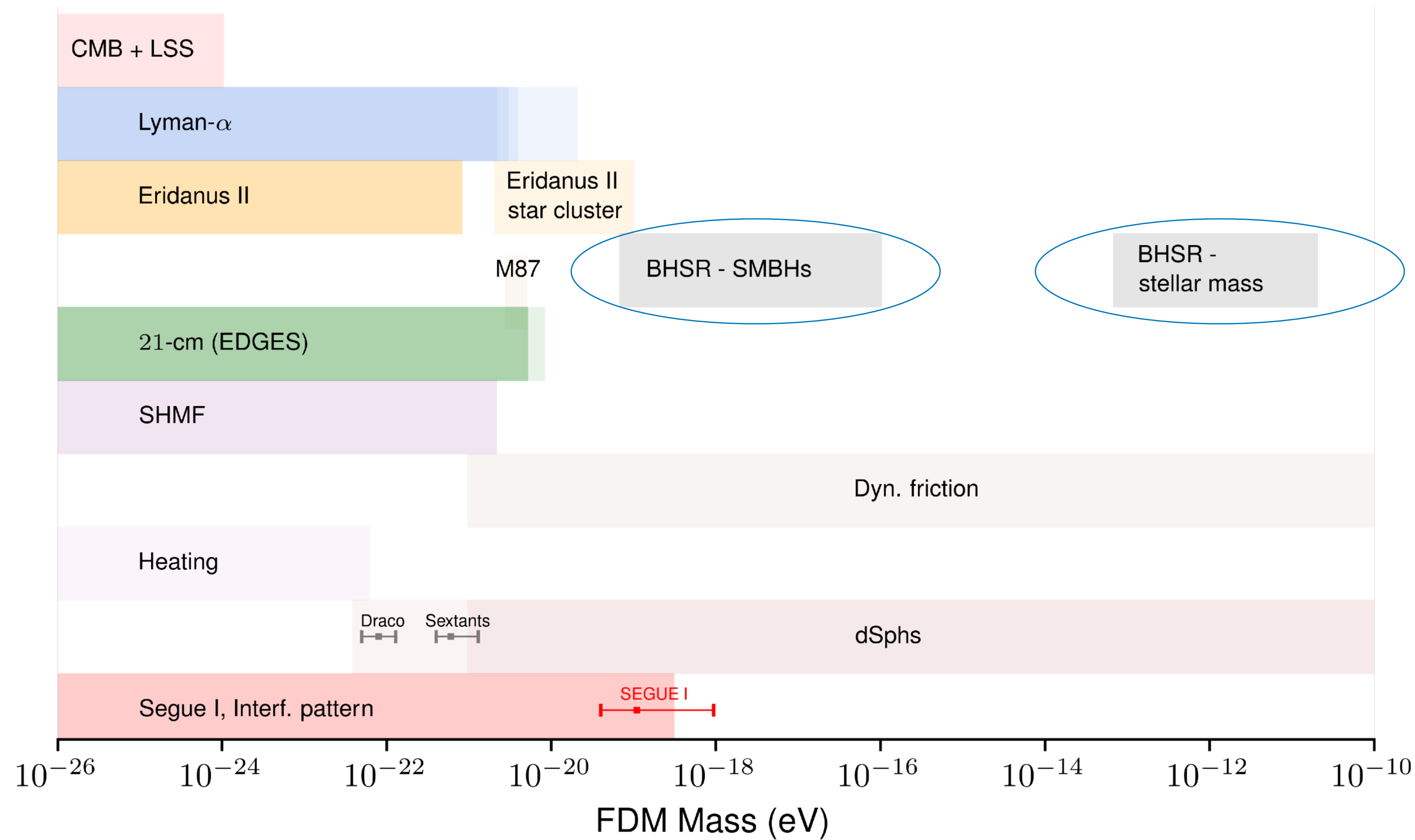
Church et al. 2019

$$m > 0.6 \times 10^{-22} \text{ eV}$$

ESO/Digitized Sky Survey 2

Observational implications and constraints

Fuzzy Dark Matter - bounds on the mass



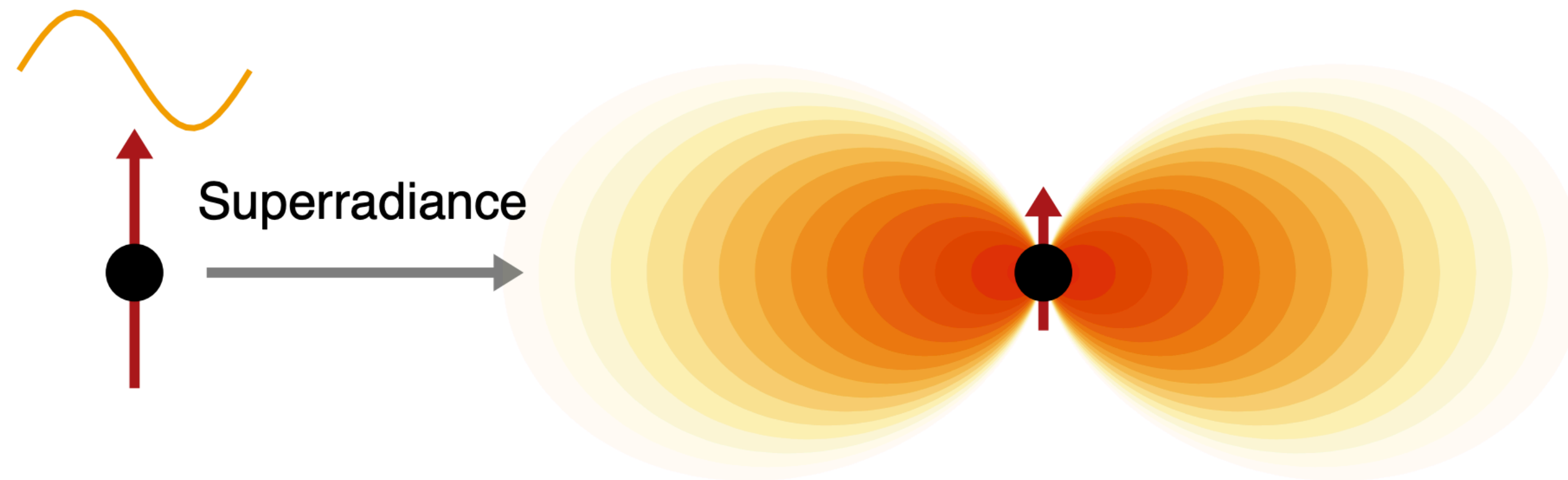
Black Hole Superradiance

Black Hole Superradiance

Zeldovich (1972) Starobinsky (1973) Arvanitaki et al. [0905.4720]

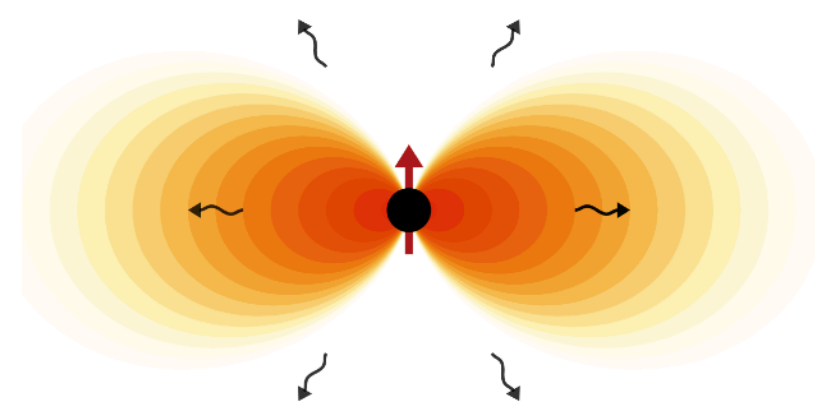
A cloud of **ultra-light bosons** (and vector fields) can be created around **rotating black holes** - if the particle Compton wavelength is of the order of the size of the BH

Structure like a “gravitational atom”

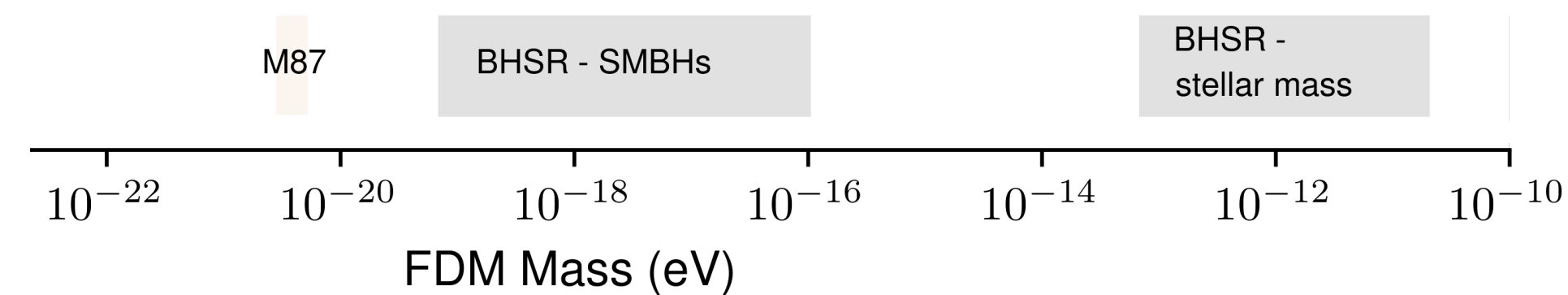


H. Chia et al, 2018

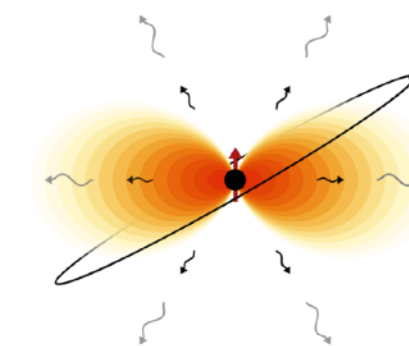
Emits gravitational waves



H. Chia et al, 2018



Dynamics can be altered by the presence of a companion - binary

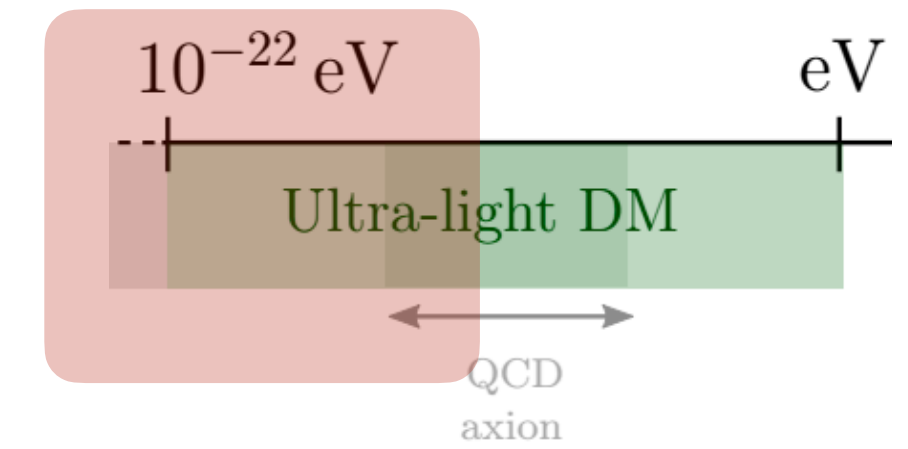
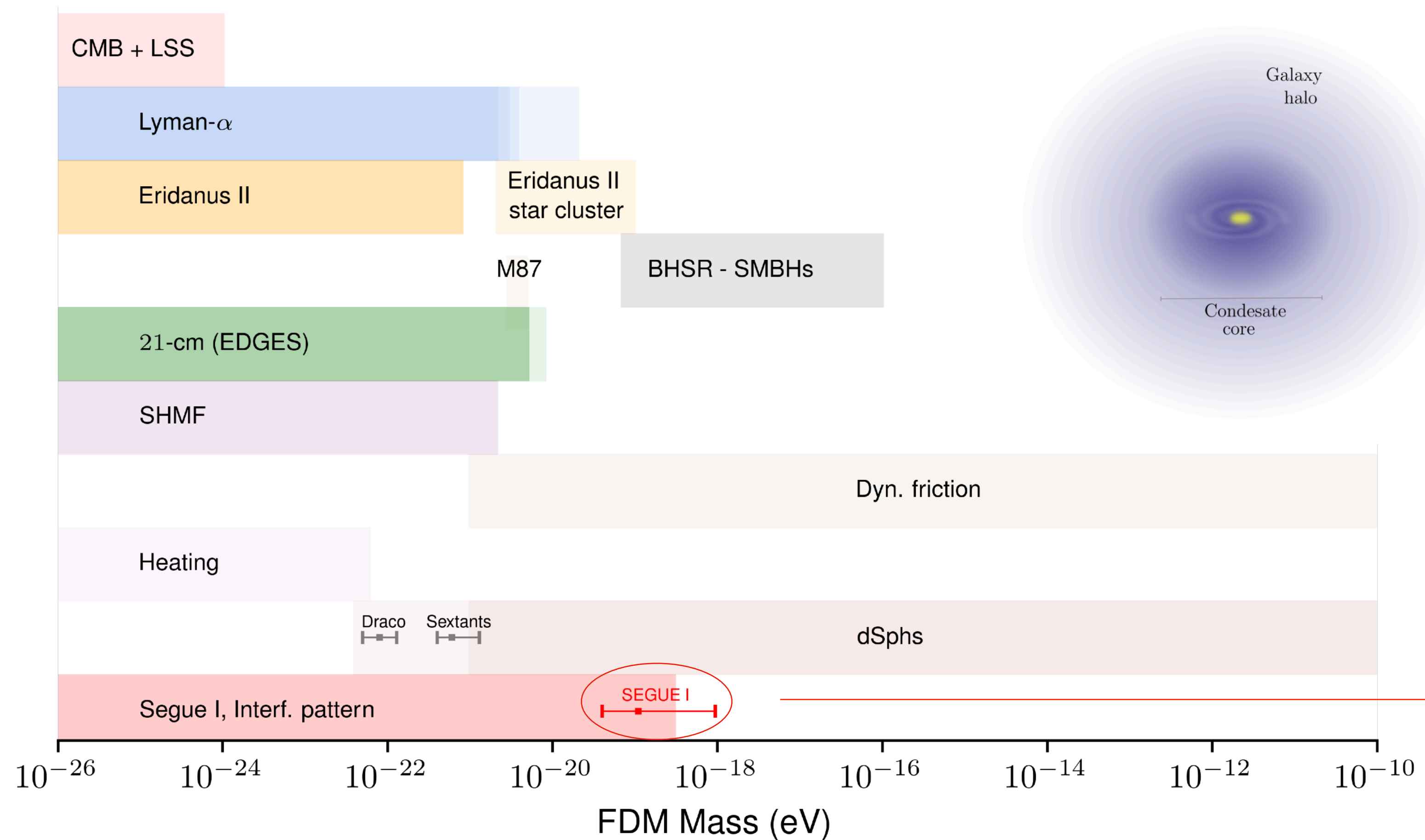


H. Chia et al, 2018

Observational implications and constraints

Fuzzy Dark Matter - bounds on the mass

Presence of a core



DWARFS

Ultra faint dwarfs

FDM SIMULATIONS

$$\rho(r) = \begin{cases} \rho_{\text{soliton}} \simeq \frac{\rho_c}{[1 + 0.091(r/r_c)^2]^8}, & r < r_c \\ \rho_{\text{NFW}} = \frac{\rho_s}{(r/r_s)(1 + r/r_s)^2}, & r > r_c \end{cases}$$

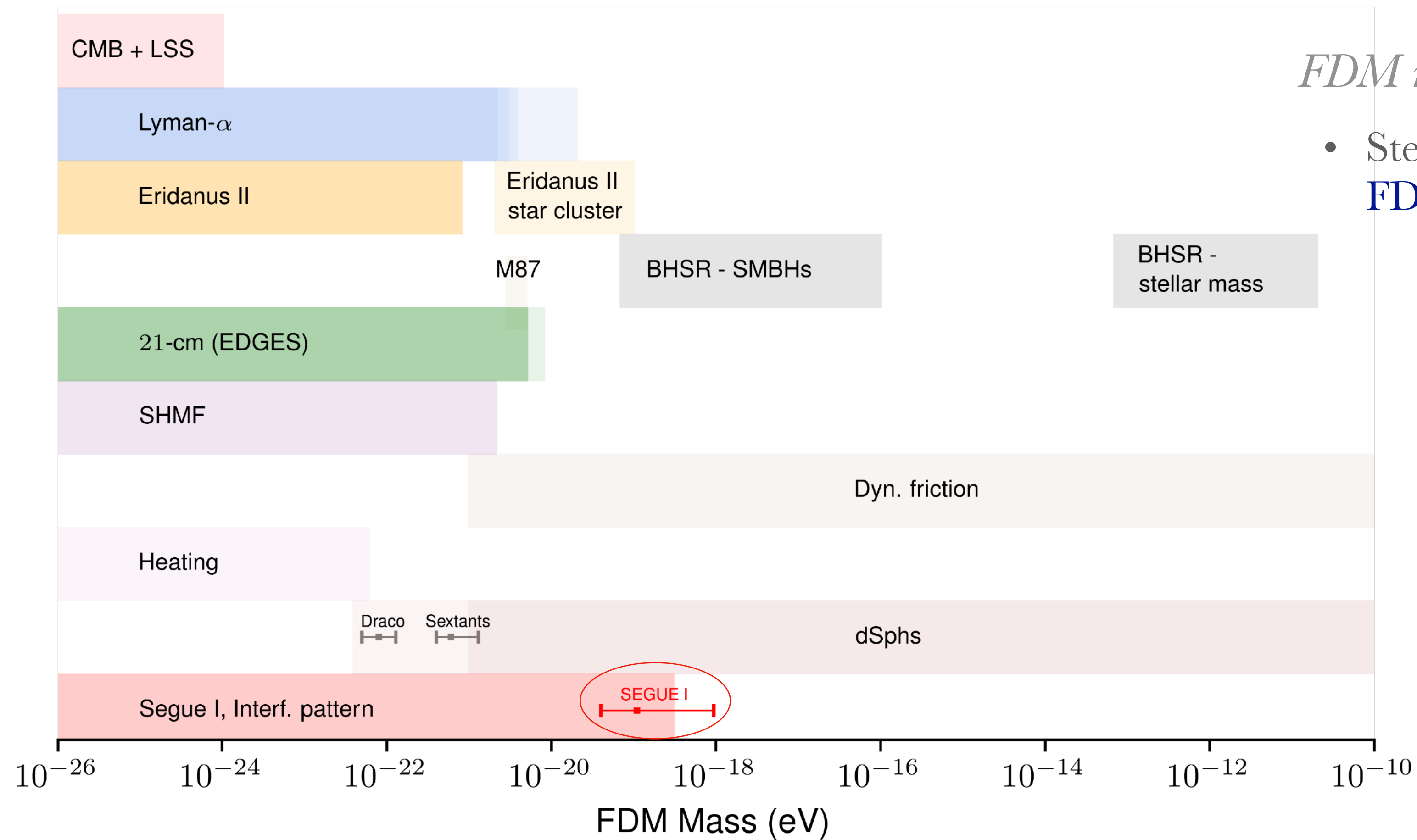
“Narrowing the mass range of Fuzzy Dark Matter with Ultra-faint Dwarfs”, J. Chan, E.F., K. Hayashi, 2021.

Ultra-light Dark Matter

Fuzzy Dark Matter - bounds on the mass

Ultra faint dwarfs

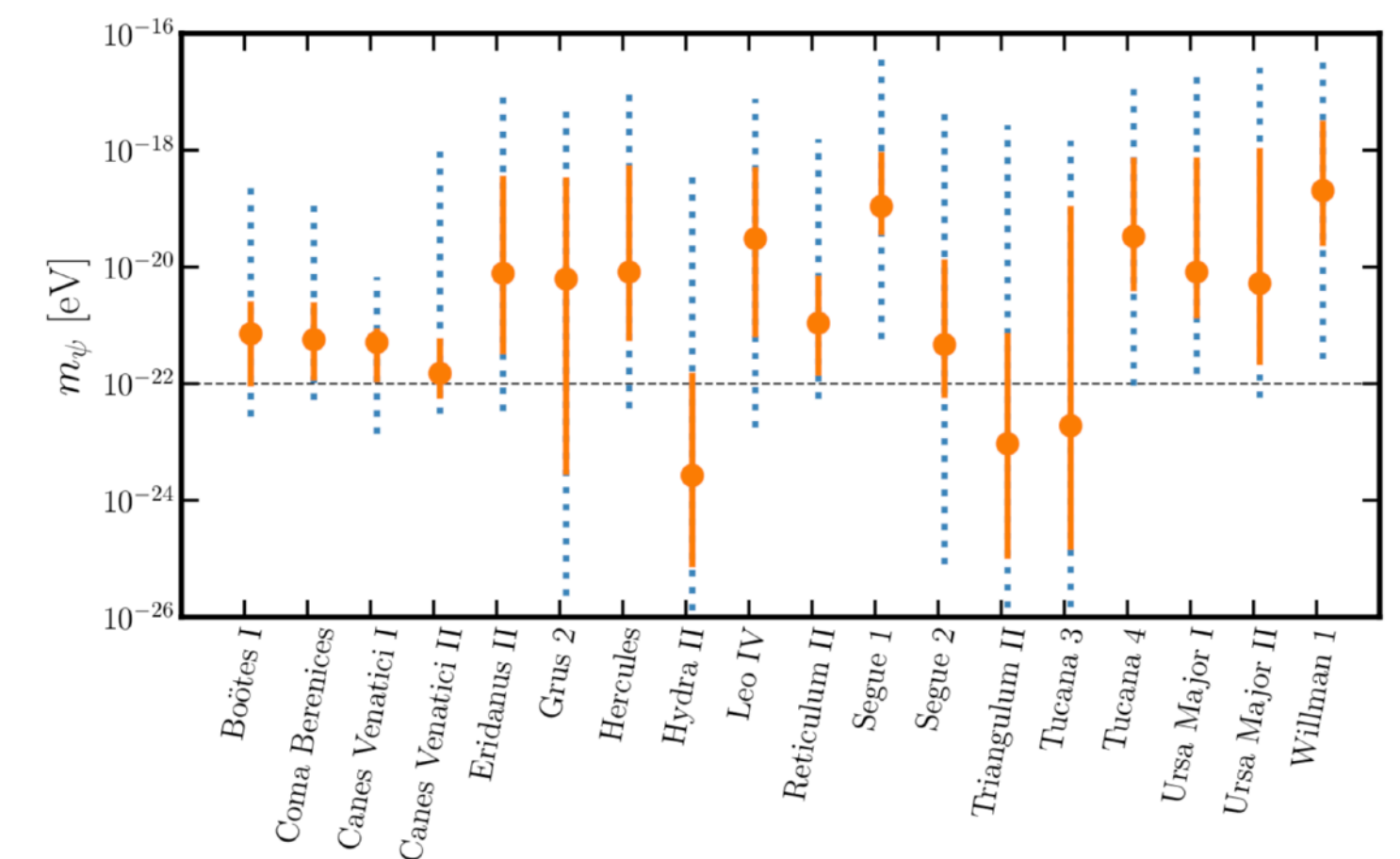
Hayashi, E.F, Chan, 2021.



FDM mass from Ultra-faint dwarfs

- Stellar kinematic data from 18 UFDs to fit the FDM profile from simulations

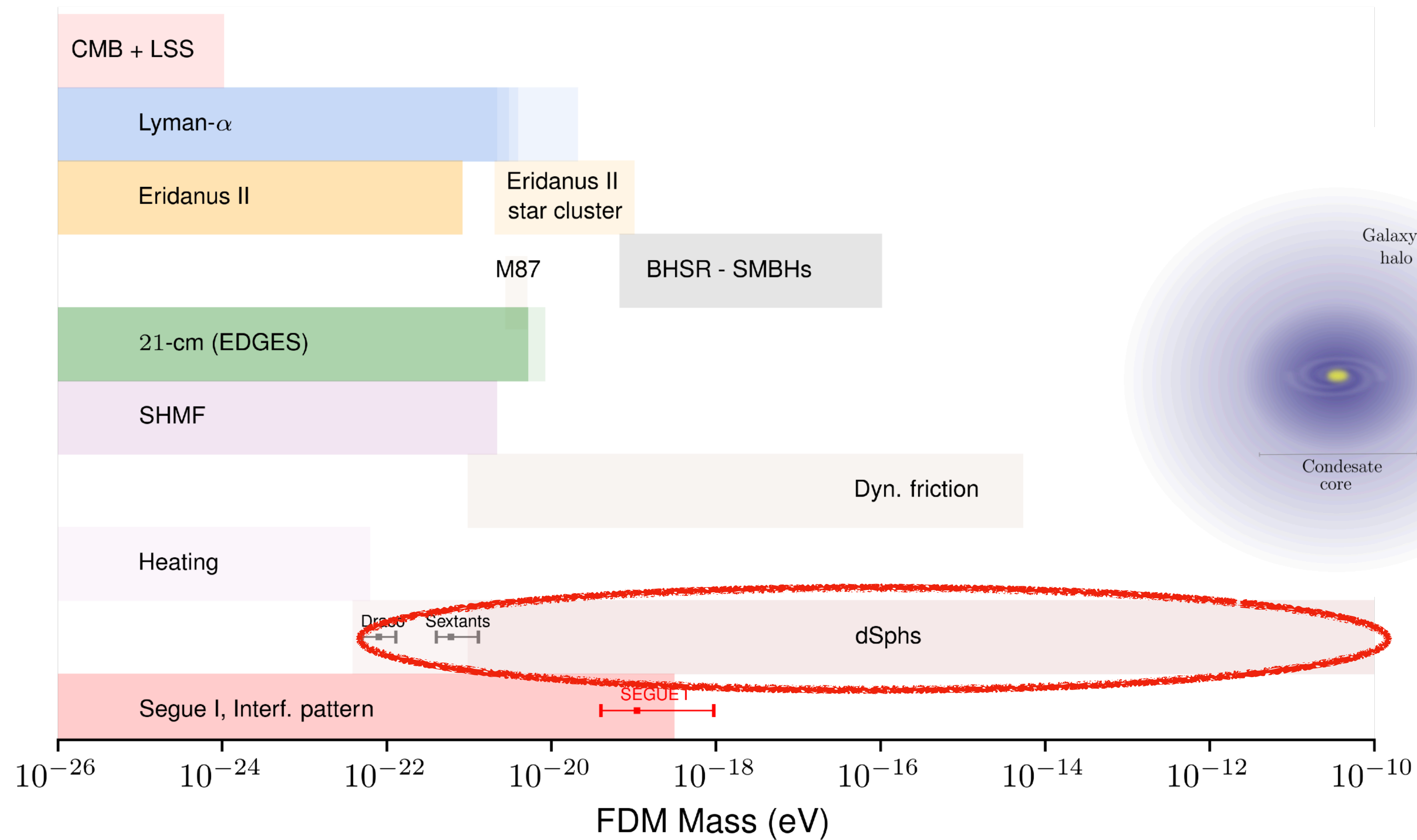
$$m_{\text{FDM}}^{(\text{Seg1})} = 1.1_{-0.7}^{+8.3} \times 10^{-19} \text{ eV}$$



Preference for higher mass

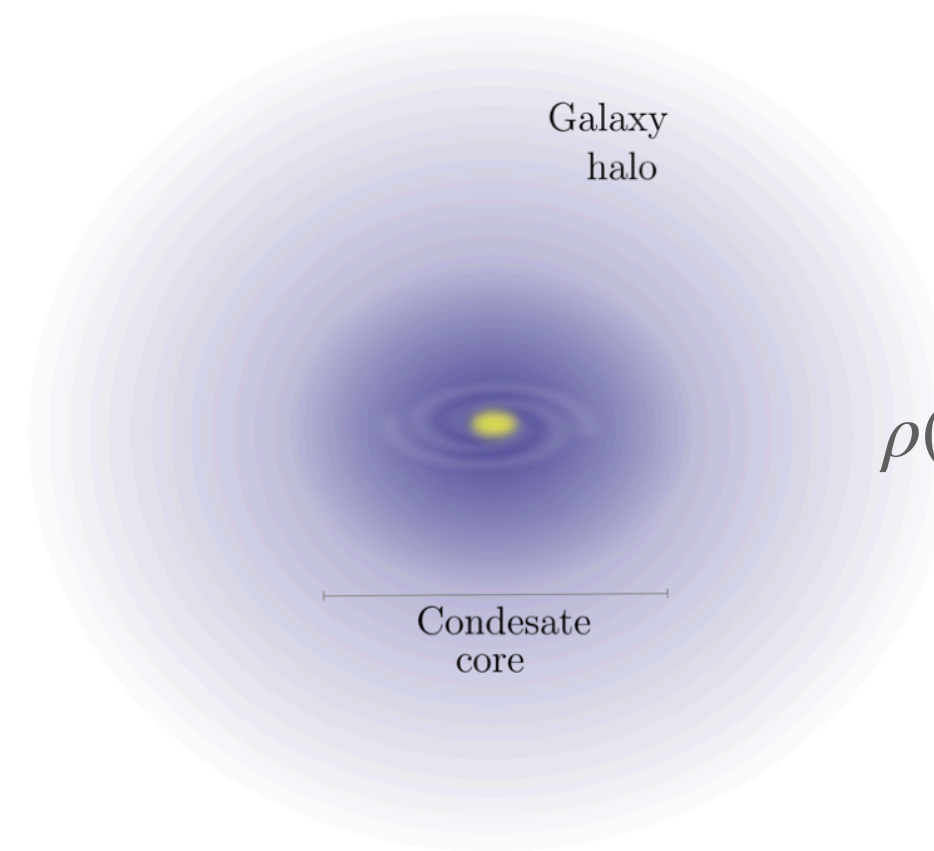
Observational implications and constraints

Fuzzy Dark Matter - bounds on the mass



DWARFS

Dwarf Spheroidals (dSphs)



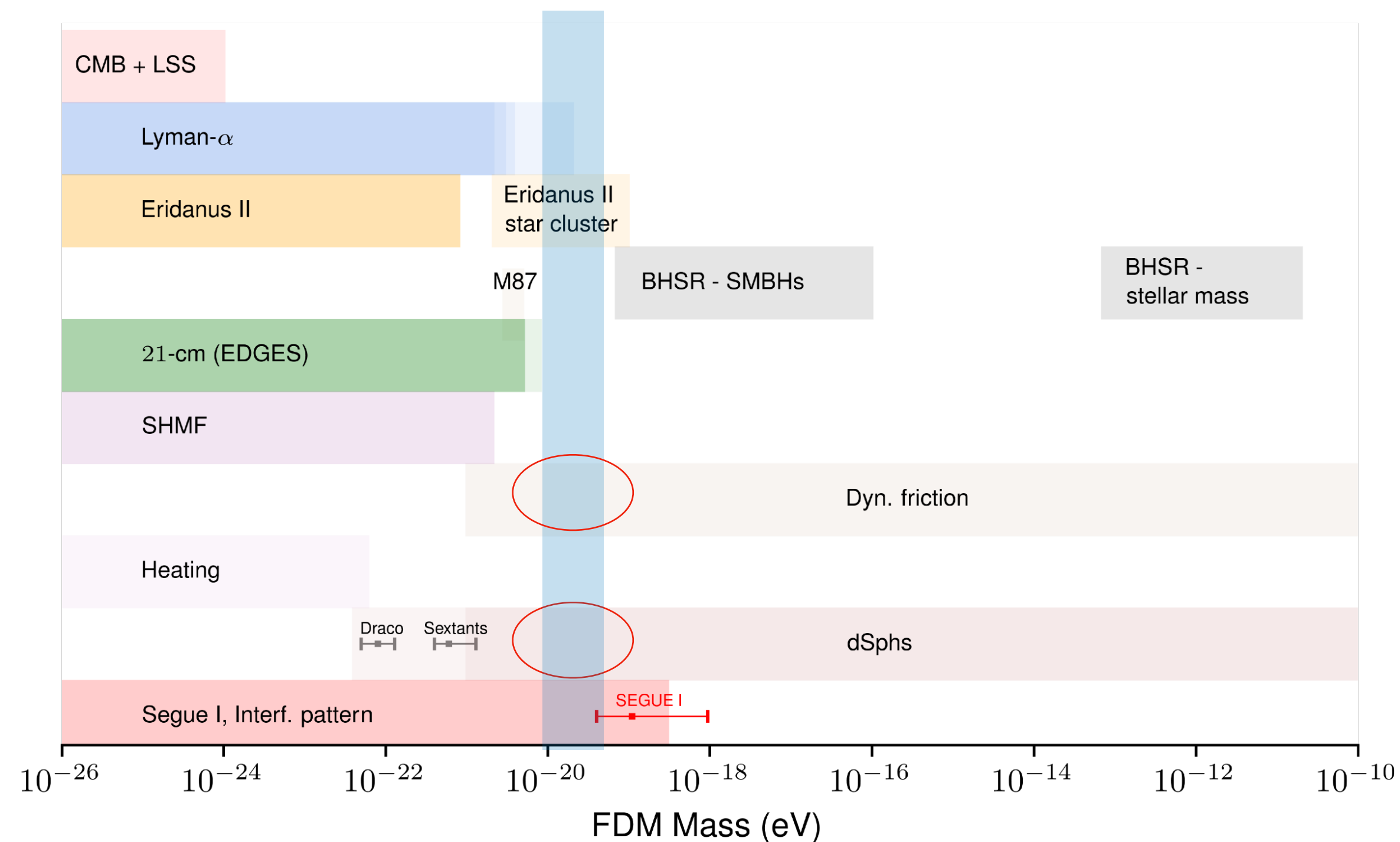
FDM SIMULATIONS

$$\rho(r) = \begin{cases} \rho_{\text{soliton}} \approx \frac{\rho_c}{[1 + 0.091(r/r_c)^2]^8}, & r < r_c \\ \rho_{\text{NFW}} = \frac{\rho_s}{(r/r_s)(1 + r/r_s)^2}, & r > r_c \end{cases}$$

Fornax - Sculptor

$$m < 0.8 \times 10^{-22} \text{ eV}$$

Constraints on the mass



$$m_{\text{FDM}}^{(\text{Seg1})} = 1.1^{+8.3}_{-0.7} \times 10^{-19} \text{ eV}$$

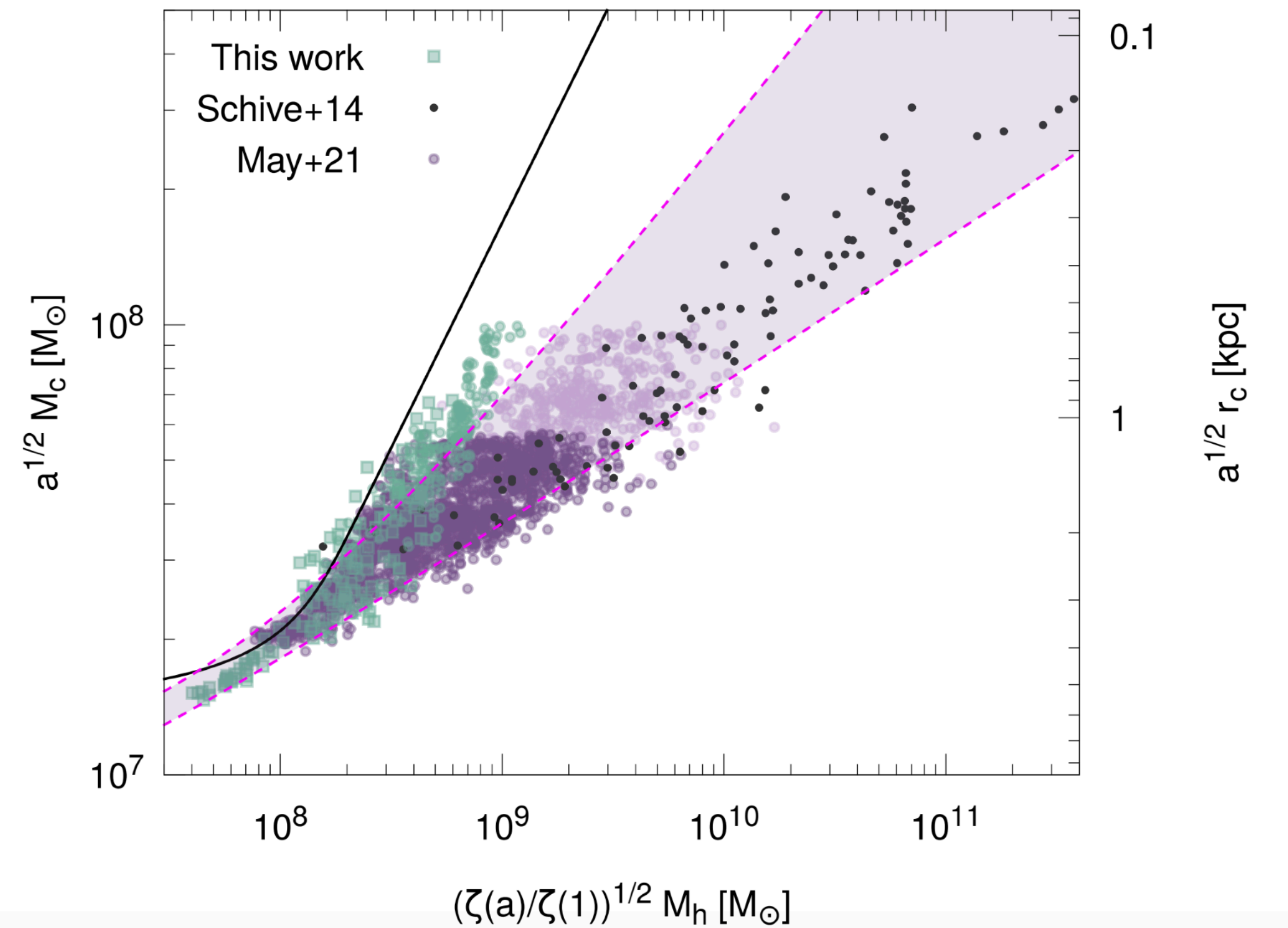
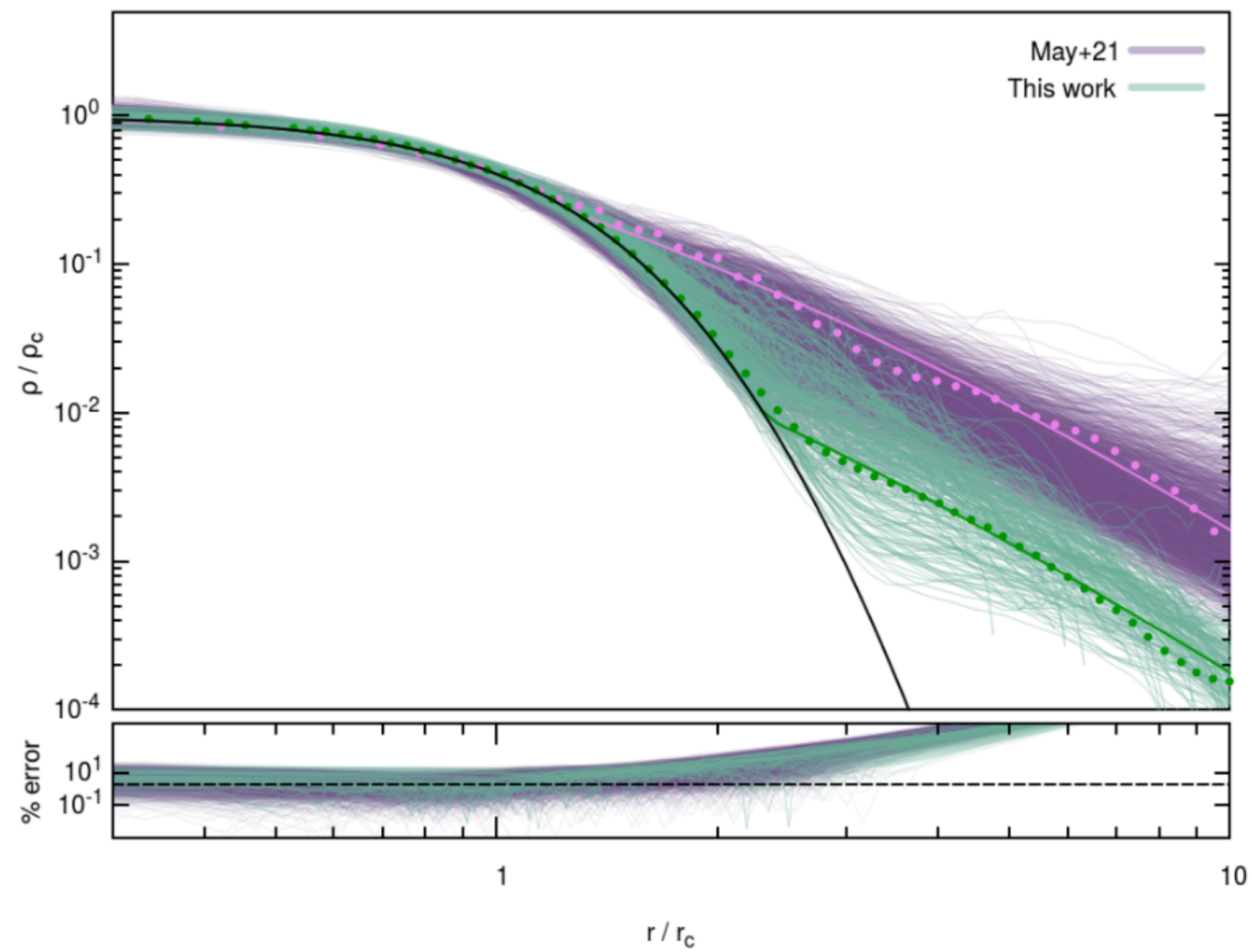
Incompatibility between all bounds and the dSphs
(Fornax and Sculptor) bounds

Possible reasons for this *incompatibility*:

- *Influence of baryons*: baryonic processes can change the density structure of their halo - we are not probing the intrinsic DM profile.
- *Universality of the core profile*: FDM soliton profile might be too simplistic, could change for different systems (might also depend on baryons)
- *Core-mass relation*: might need to be better understood. \neq relation in \neq simulations
- *Challenge for the FDM model*

FDM - Core-halo mass relation

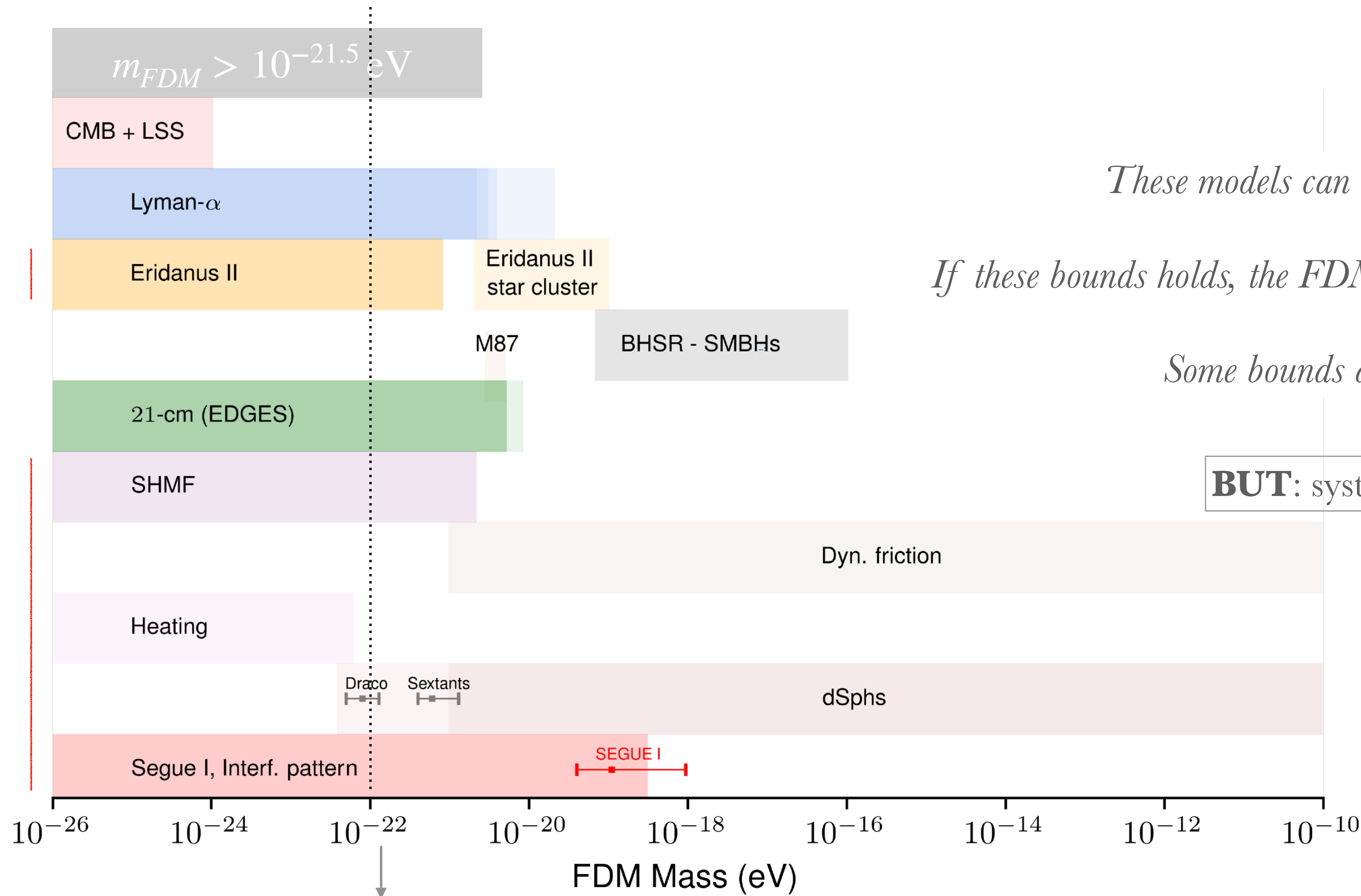
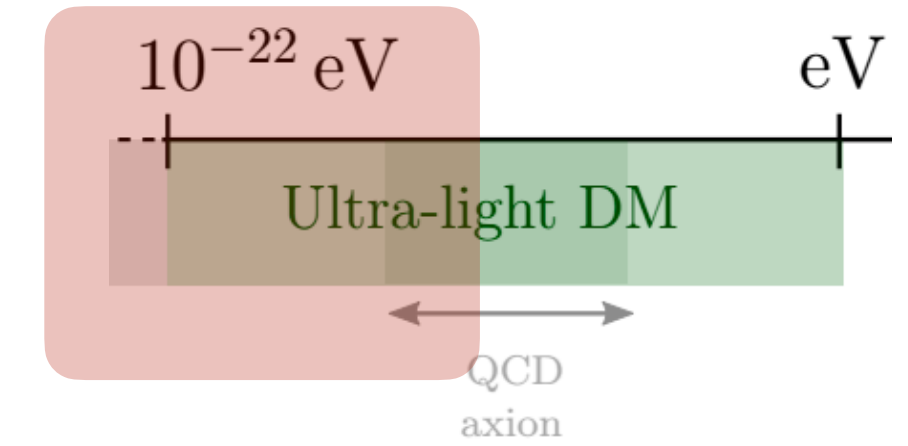
J. Chan, EF, S. May, K. Hayashi, M. Chiba 2021



Steeper slope \longrightarrow Smaller core \longrightarrow Smaller mass

Current status

Fuzzy Dark Matter - bounds on the mass



These models can be highly constrained

If these bounds holds, the FDM mass range is narrowing down

Some bounds are incompatible!

BUT: systematic effects!!

Need:

- Observations
- Improve sims
- New observables
- New probes

Sweet spot for solving small scale problems

Current status

Bounds on the mass and other parameters

Self interacting FDM

m

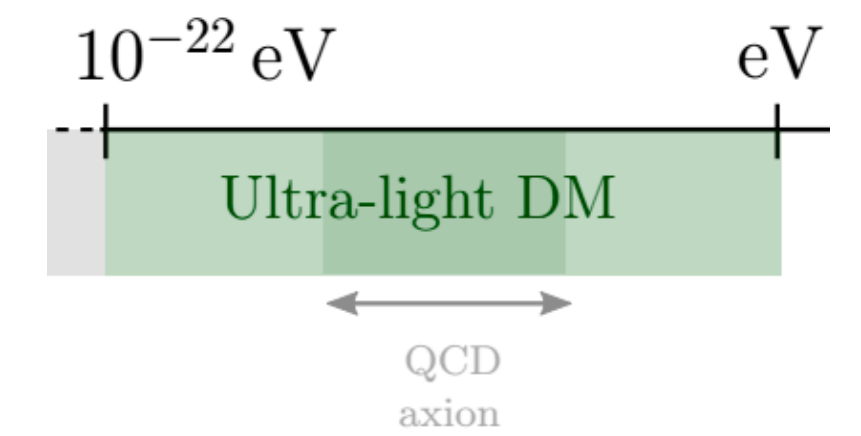
g

DM Superfluid

$$\mathcal{L} = P(X)$$

* Check: Lasha Berezhiani et al (2020)

Still highly unconstrained



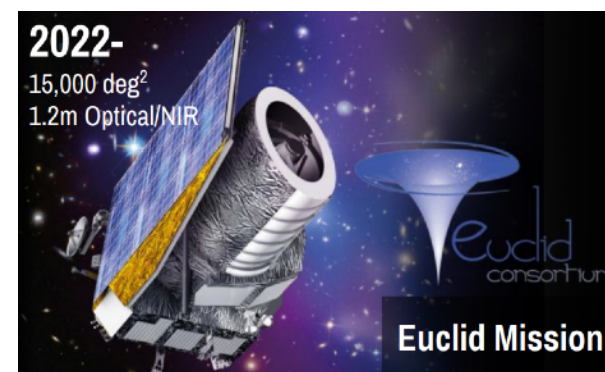
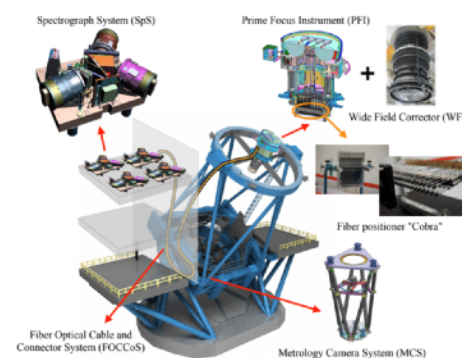
FUTURE

Observations

Photometric and spectroscopic surveys

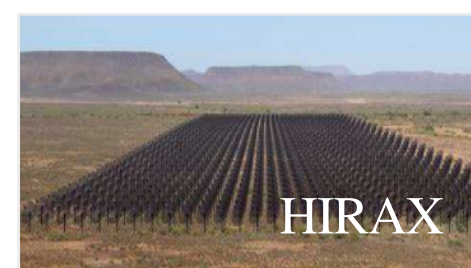


Prime Focus Spectrograph (PFS)



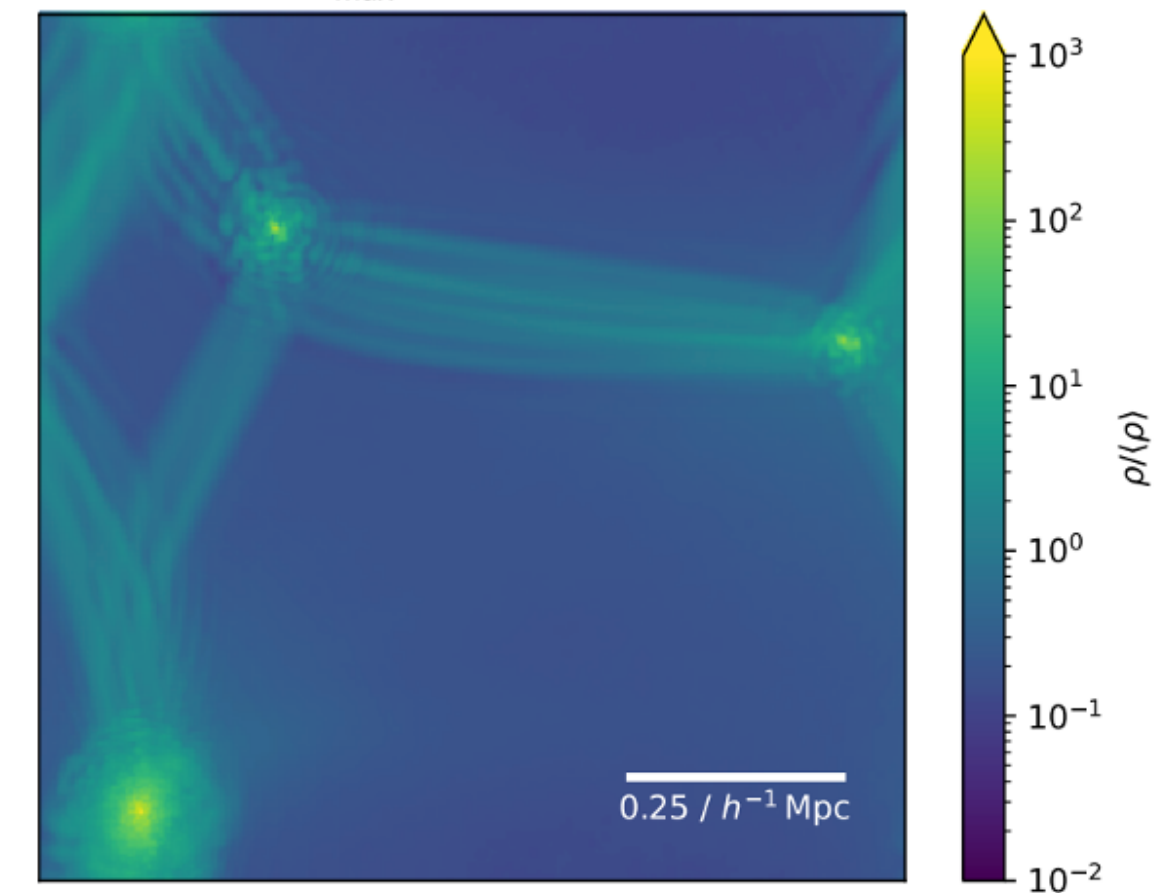
CMB

21cm



Simulations

FDM: 256^3 , $mc^2 = 1.75 \times 10^{-23}$ eV, $z = 0.00$
 $v_{\max} = 88.1$ km/s



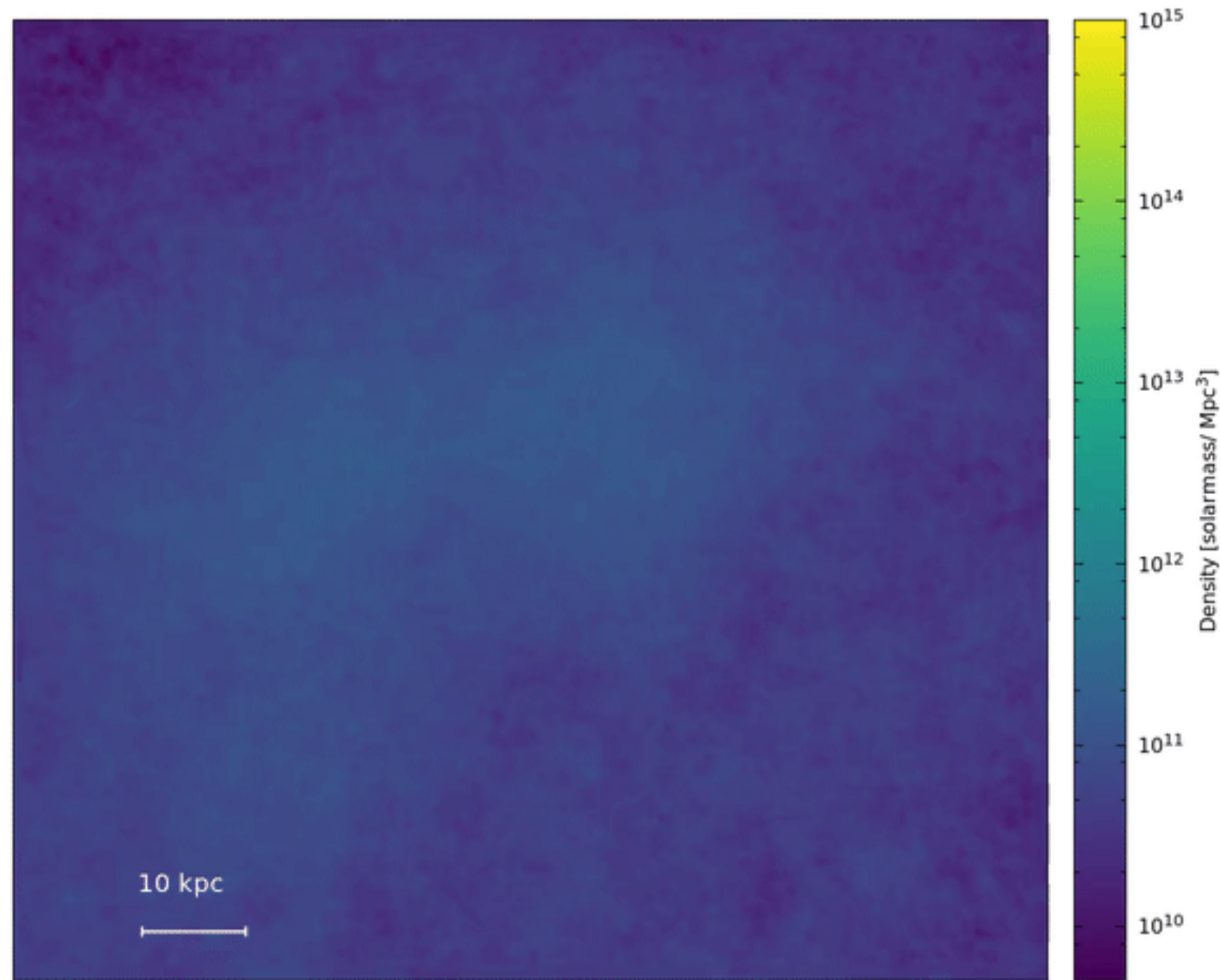
New observables

Ex.: - interference pattern
- vortices

New probes

New observables/new probes

Interference pattern



Simulation by Jowett Chan

$\mathcal{O}(1)$ fluctuations in density \rightarrow

Constructive interference: granules

Destructive interference $\sim \lambda_{dB}$

ONGOING

- Characterizing the interference patterns using full simulations

- Strong lensing

Devon Powel, Simona Vegetti, Simon White, John McKean

- Stellar streams

Sten Delos and Fabian Schmidt

Previous studies:

Strong lensing:

J. Chan, H. Schive, S.g. Wong, T. Chiueh, T. Broadhurst, 2020

A. Laroche, Daniel Gilman, X. Li, J. Bovy, X. Du, 2022

Stellar streams:

Neal Dalal, Jo Bovy Lam Hui, Xinyu Li, 2020

Sub-galactic power spectrum:

Hezaveh et al. (2016)

Sub-galactic power spectrum

Kawai, Oguri (2021)

Dwarfs

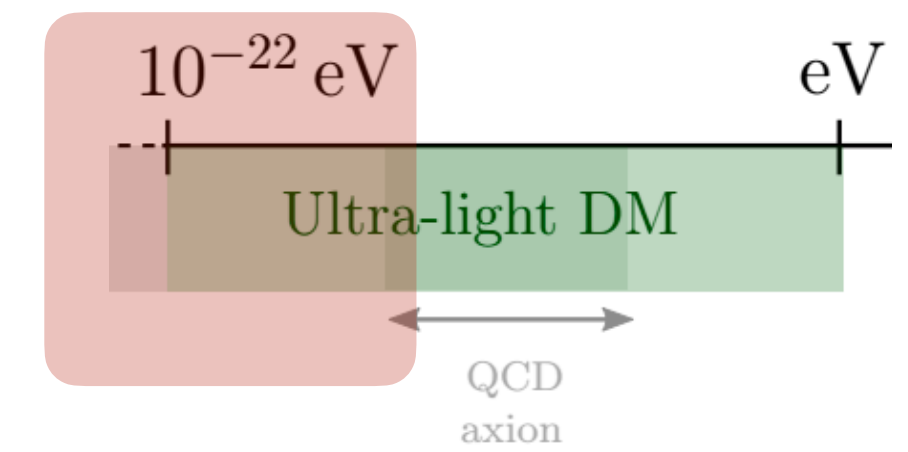
N. Dalal, A. Kravtsov, 2022

PROBES:

- Strong lensing

- Stellar streams

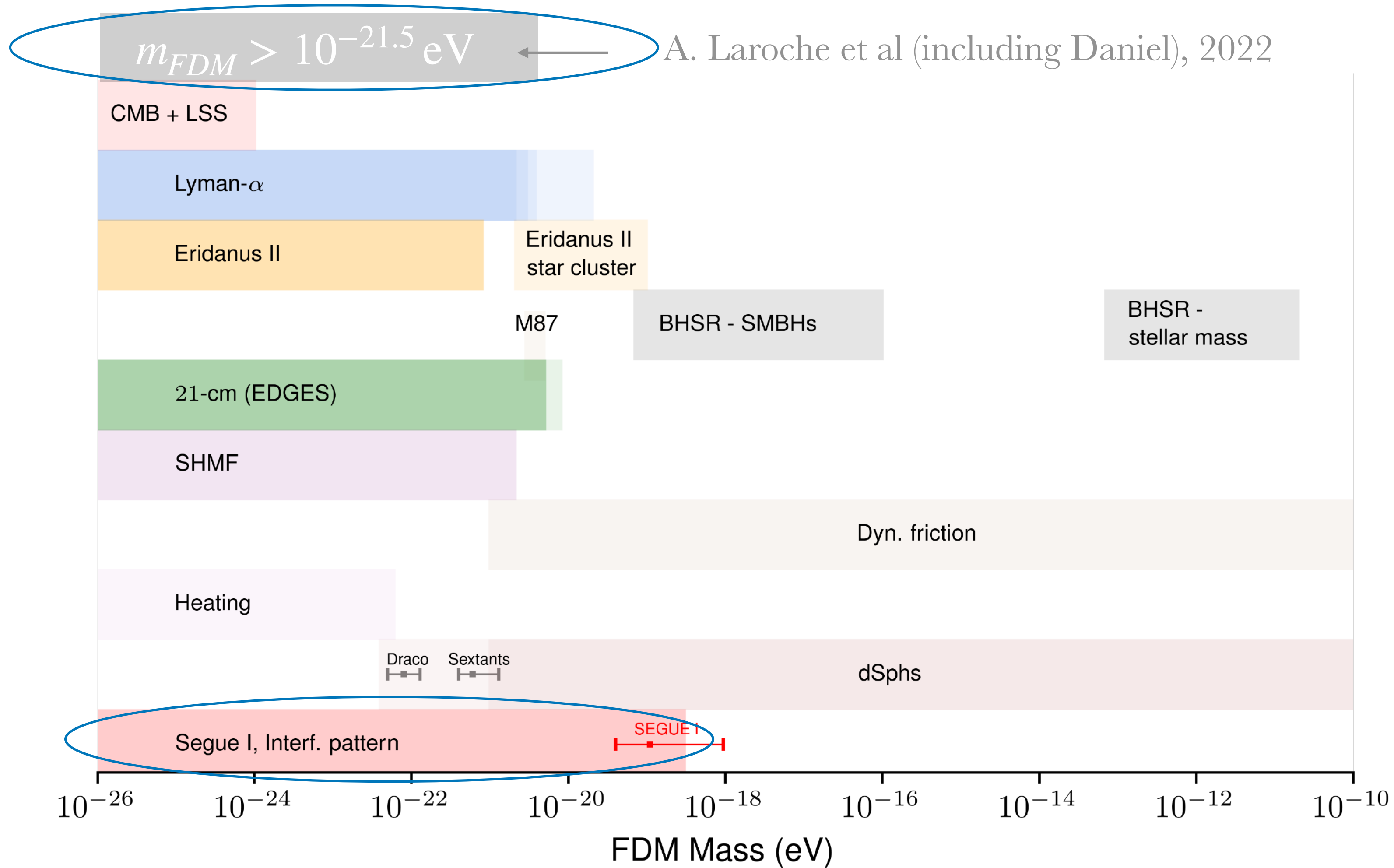
- Heating



In collaboration with Jowett Chan and Simon May

Observational implications and constraints

Fuzzy Dark Matter - bounds on the mass



INTERFERENCE PATTERNS

N. Dalal, A. Kravtsov, 2203.05750

$$m_{FDM} > 1 \times 10^{-19} \text{ eV}$$



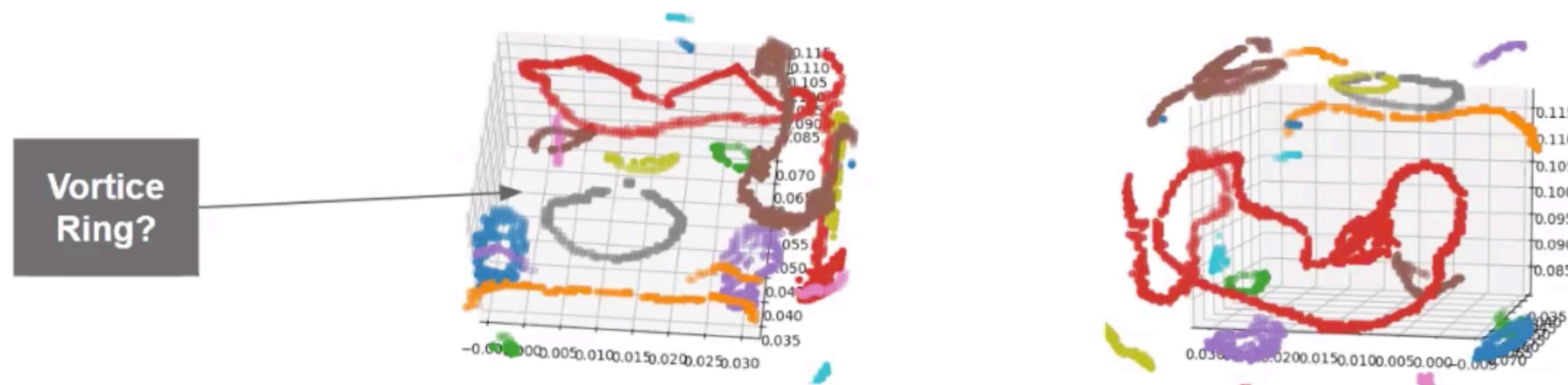
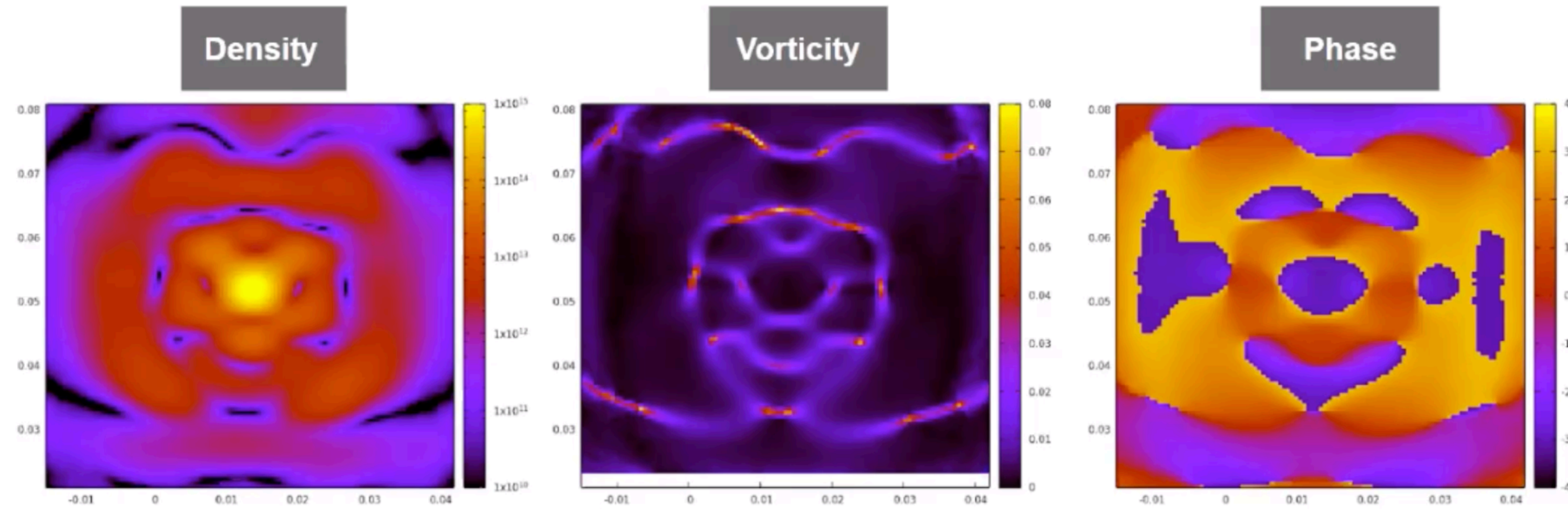
What is the predicted **size and abundance** of vortices in the halo?
Are they **observable**?
Strong lensing? Stellar streams?
Can they be formed in the filaments?

New observables/new probes

Ongoing: Vortices

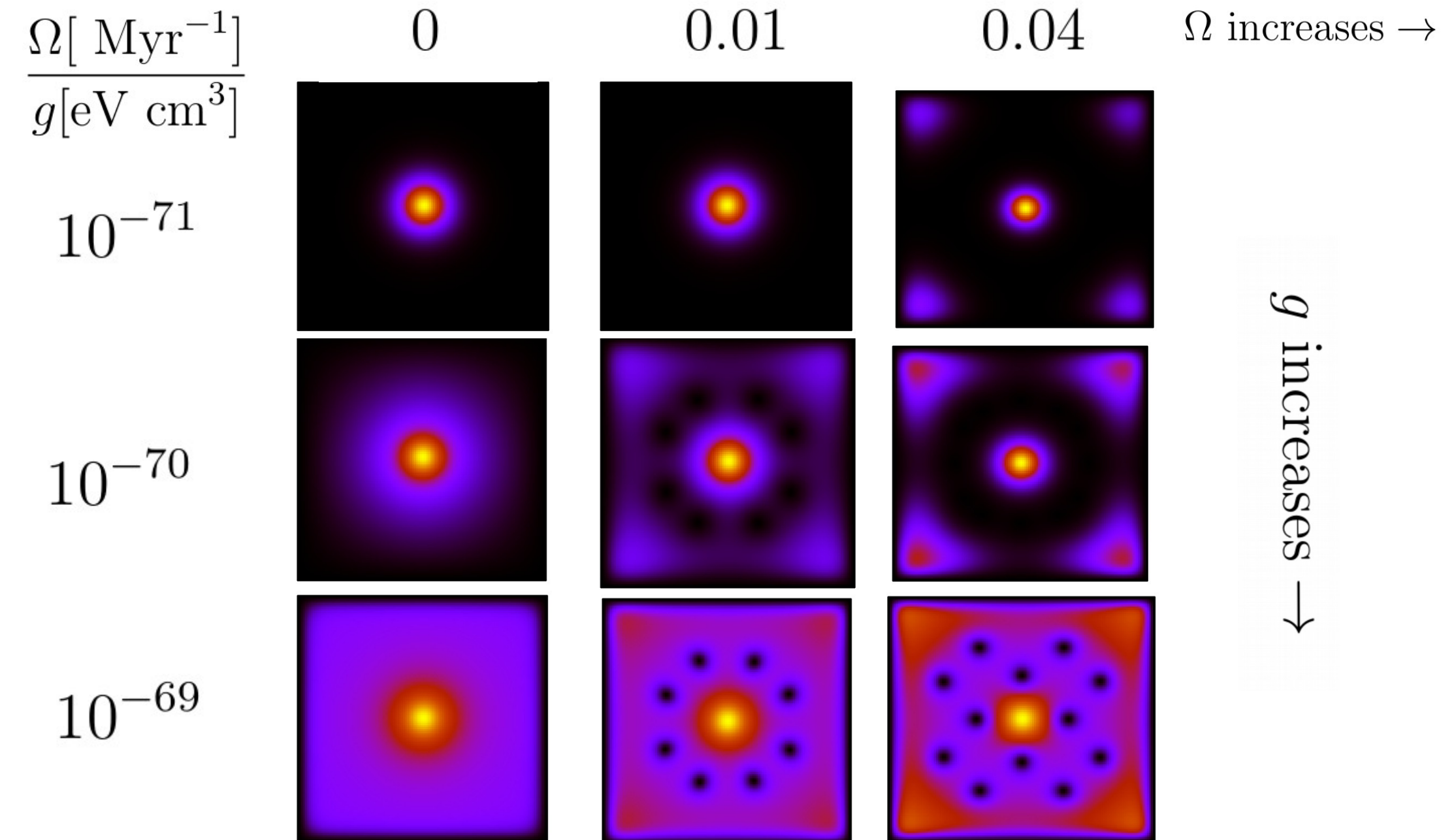
PRELIMINARY

Fuzzy DM



In collaboration with Jowett Chan

Self-interacting Fuzzy DM



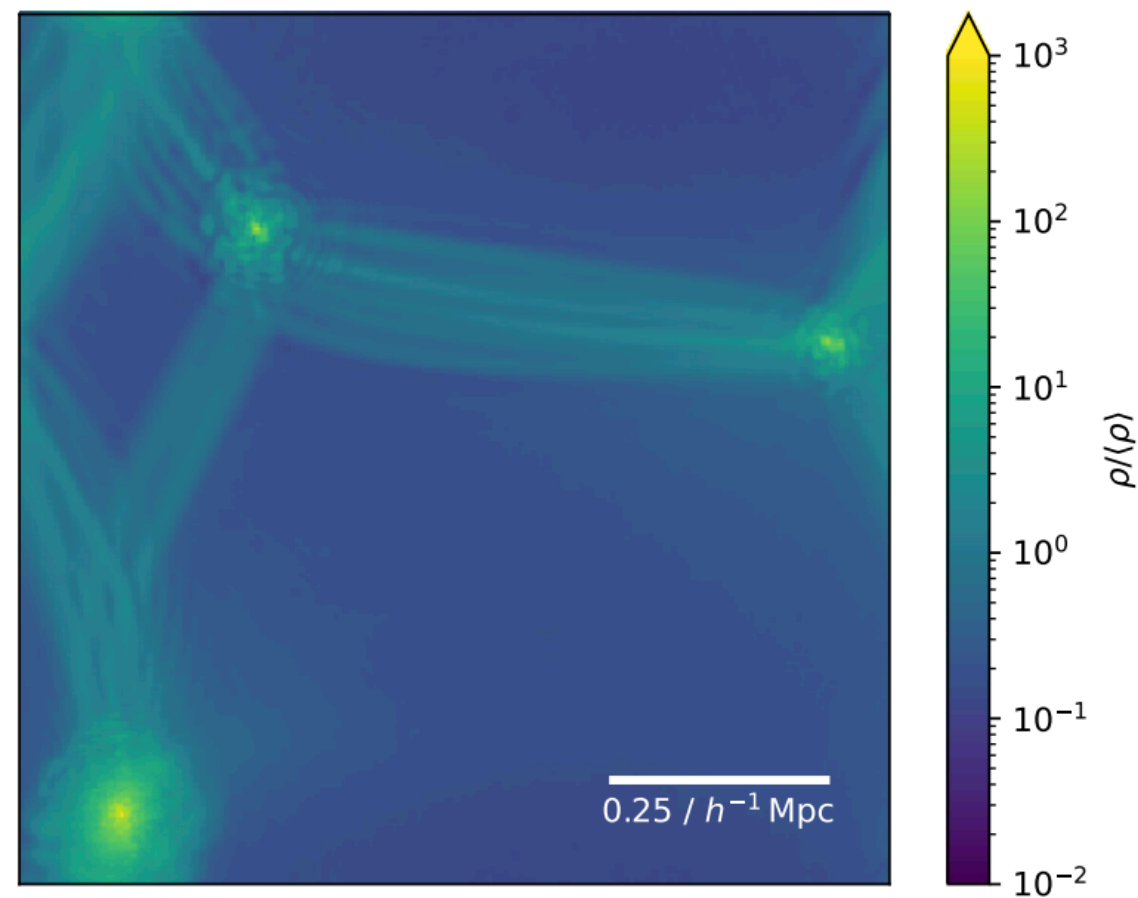
+ Improve theoretical understanding of these DM vortices

In collaboration with P. Bittar

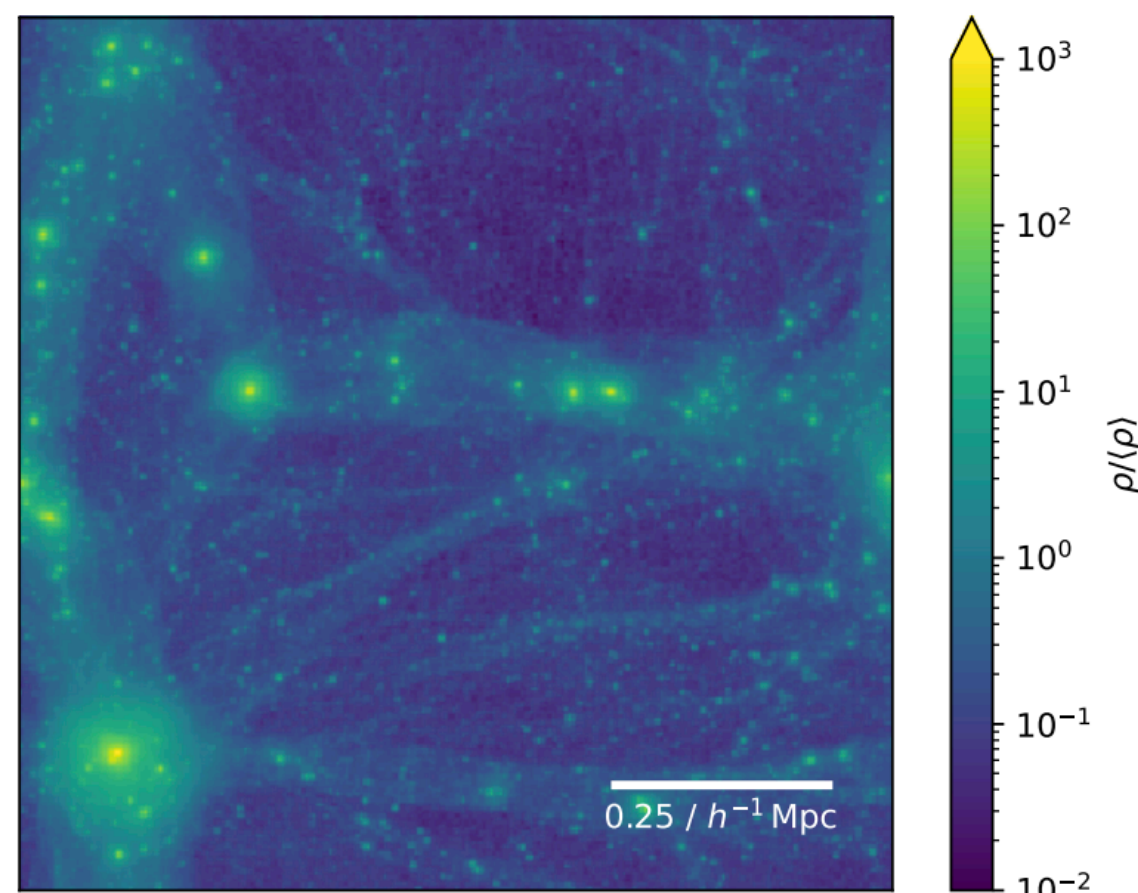
New observables/new probes

Filaments in FDM

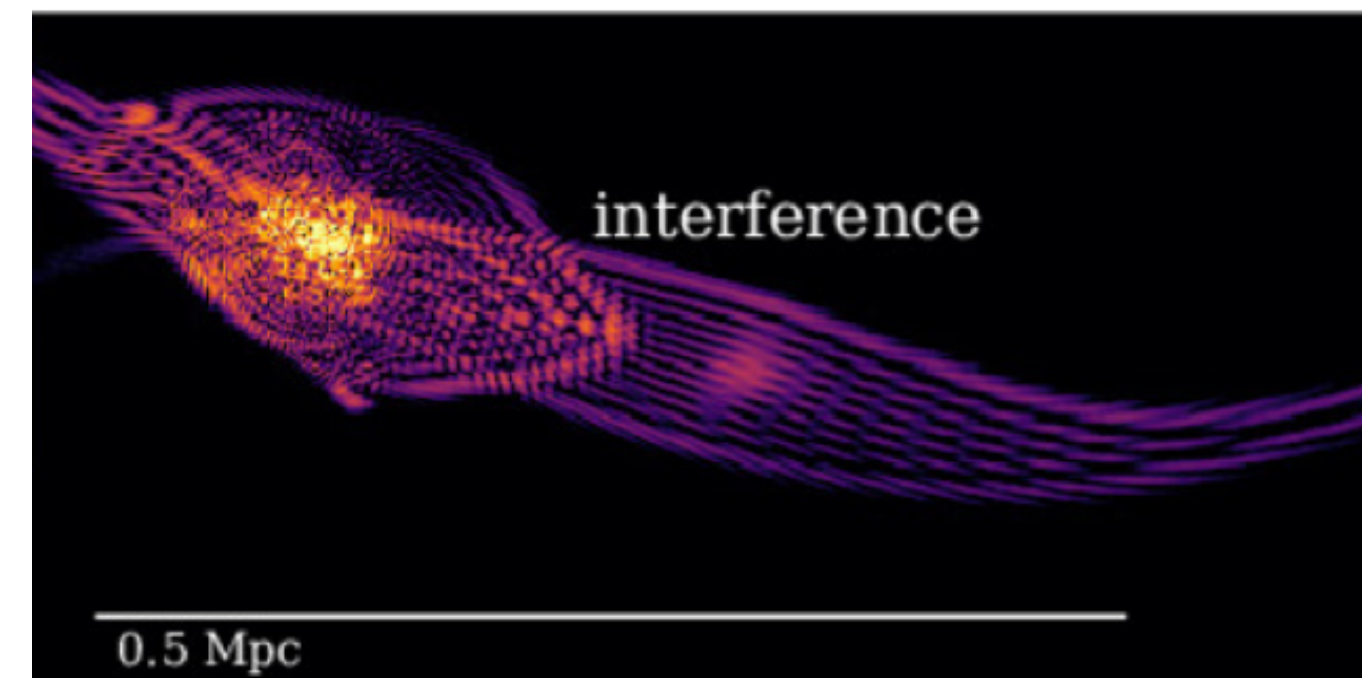
FDM: 256^3 , $mc^2 = 1.75 \times 10^{-23}$ eV, $z = 0.00$
 $v_{\max} = 88.1$ km/s



CDM: 256^3 , $z = 0.00$



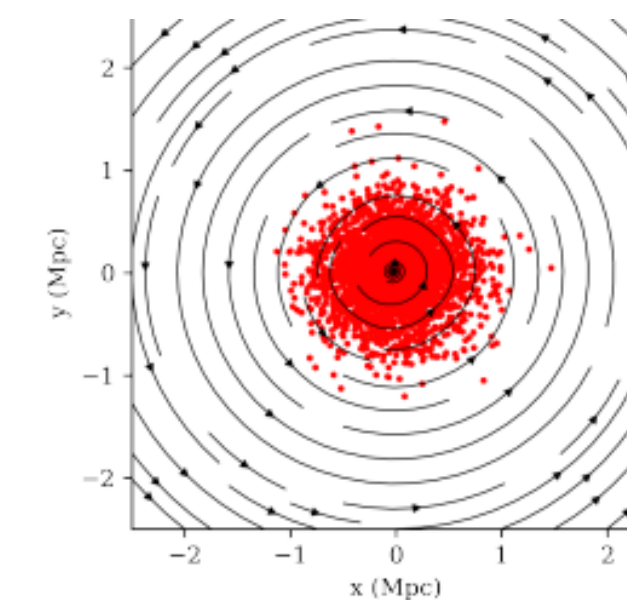
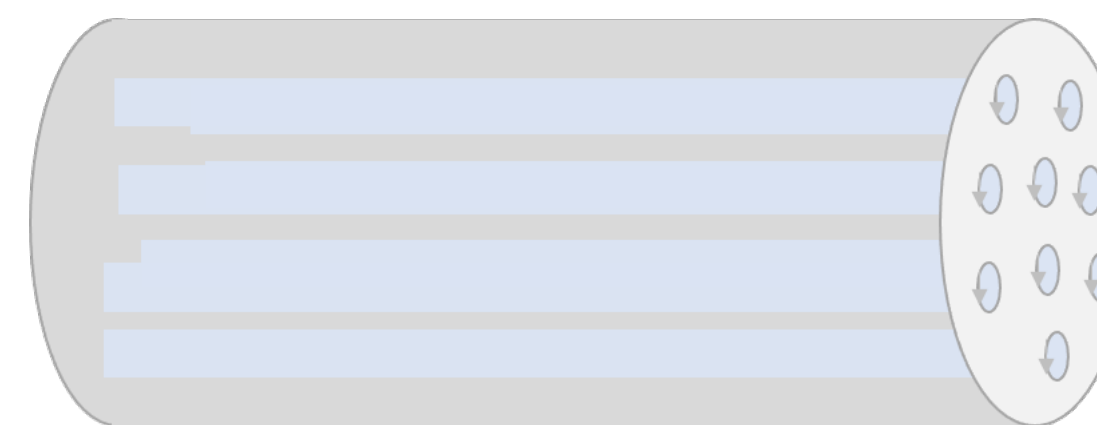
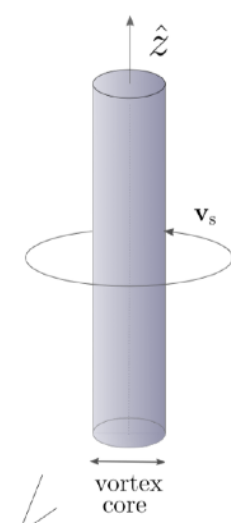
S. May et al. 2021



Mocz et al. 2017

Vortices in filaments

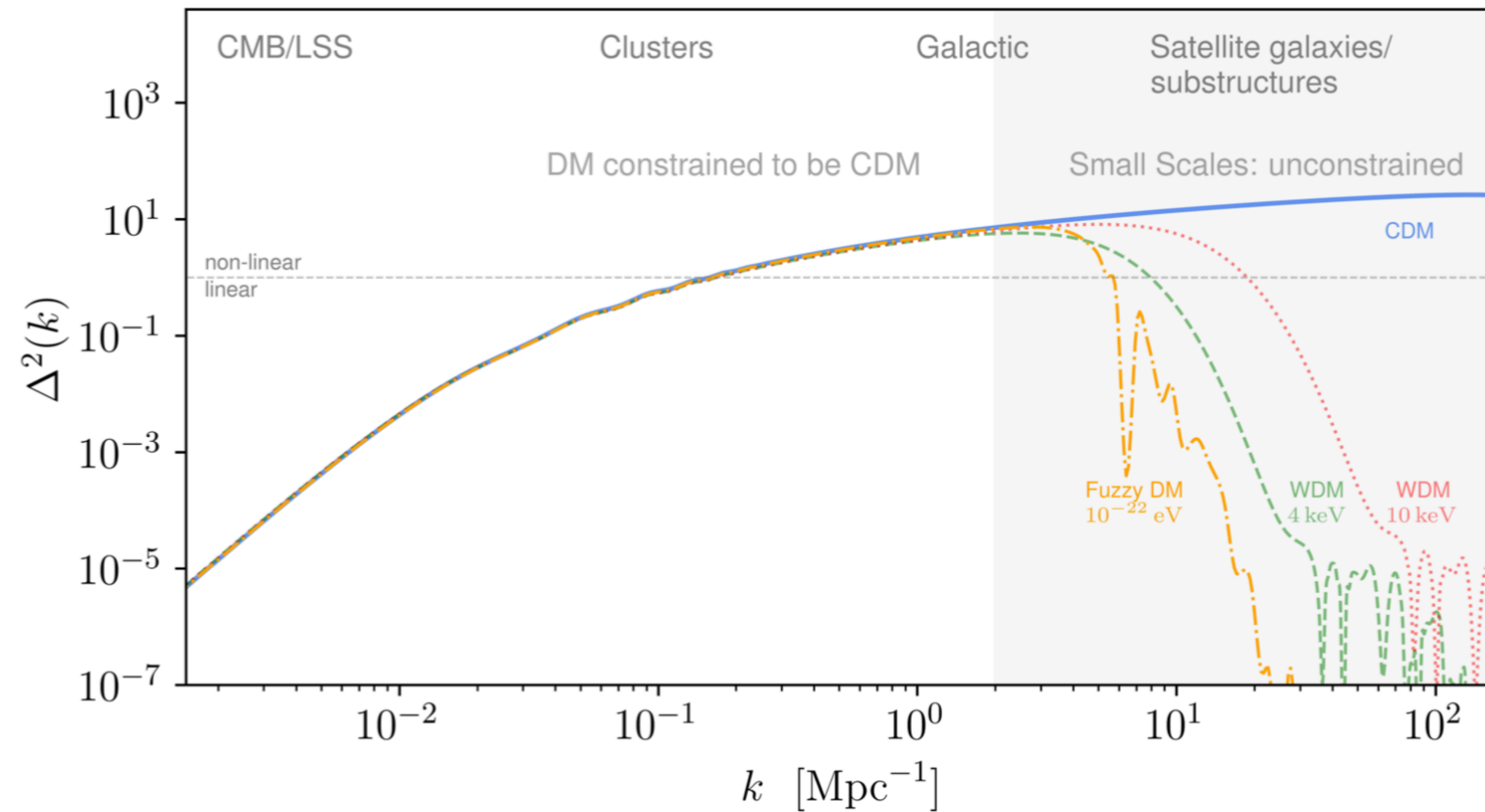
"Cosmic Filament Spin from Dark Matter Vortices",
 S. Alexander, C. Capanelli, EF, and E. McDonough (2021)



Sub-galactic *power spectrum*

New probes

Using gravitational probes, strong lensing and stellar streams, to describe substructures



Sub-galactic *power spectrum*

Using gravitational probes, strong lensing and stellar streams, to describe substructures

Substructure convergence power spectrum

Develop a formalism to compute the substructure convergence power spectrum for different populations of dark matter subhalos.

A. Diaz Rivero, et al. (2017); Diaz Rivero, et al., (2018)

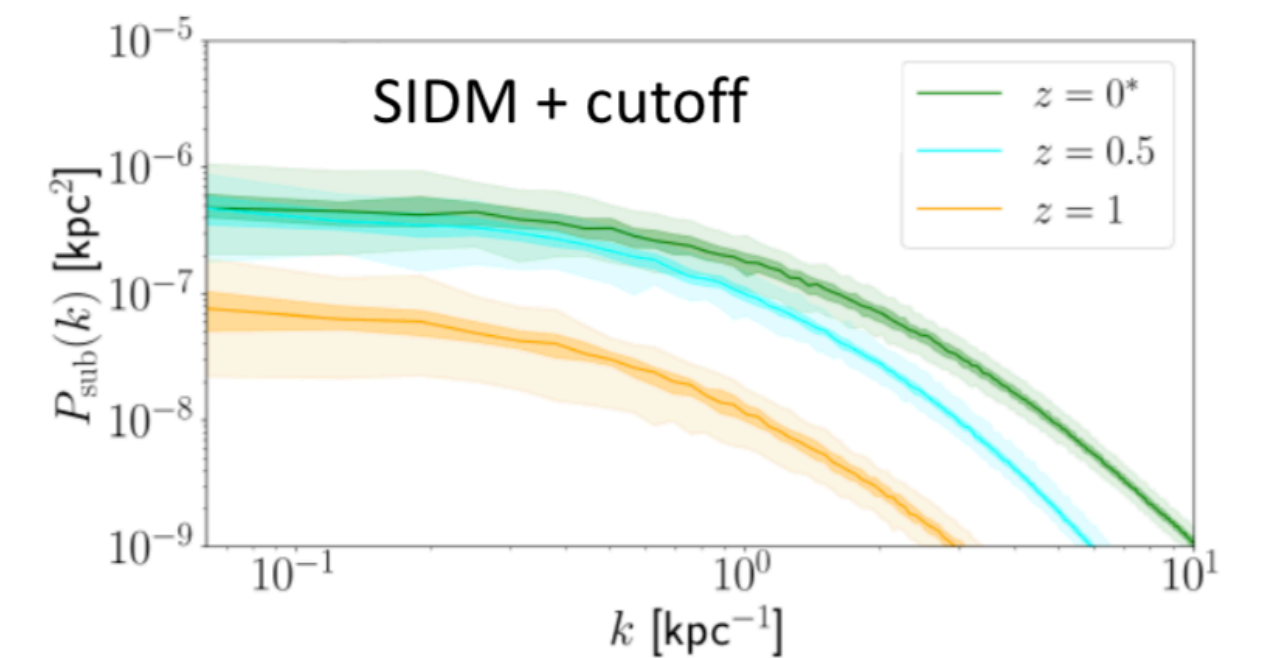
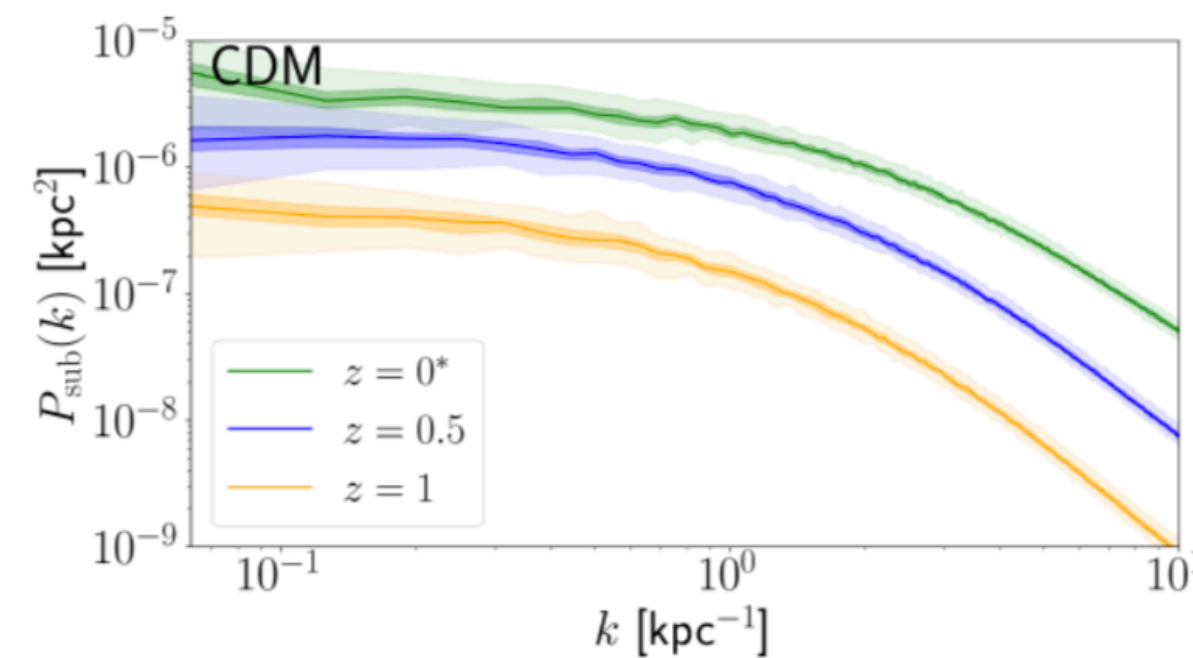
Bayer et al. (2018) ; Auger et al. 2009
 FDM: *Kawai et al. (2021)*

Hezaveh et al. (2016) (projected mPS by using strong lensing)

Change of language: instead of talking about lensing perturbations in terms of individual subhalos, look at the correlation function of the projected density field.

(based on Dvorkin's slide)

$$P_{\text{sub}}(k) = P_{1\text{sh}}(k) + P_{2\text{sh}}(k)$$



Sub-galactic *power spectrum*

Using gravitational probes, strong lensing and **stellar streams**, to describe substructures

Substructure convergence power spectrum

Sten Delos and Fabian Schmidt (2021)

Stellar streams: perturbed by passing substructure. Good gravitational probe, since given their low dynamical temperature and negligible self-interaction, it retains the memory of those encounters.

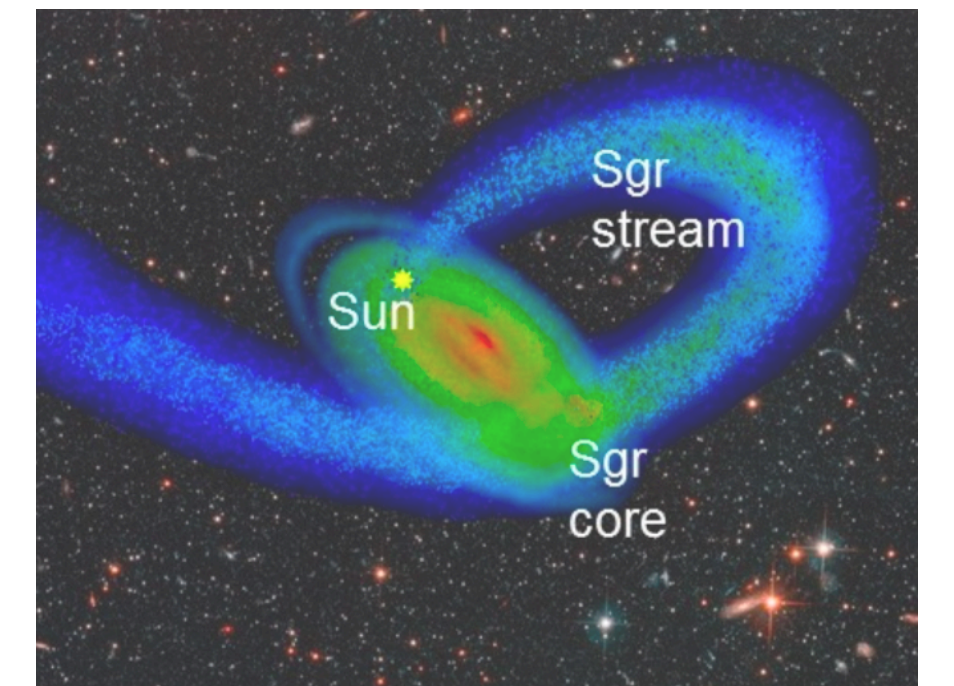
THIS WORK: Fully analytical understanding of the stream perturbations!

Power spectrum of a stream's stellar density is analytically related to that of the substructure background:

$$\boxed{P_*(k, t)} = \chi_* \left(k\sigma_0 t, \frac{D}{k\sigma_0^3} \right) \frac{k^2 t^2}{3} P_{\Delta v}(k, t)$$

Stream power Substructure power

$$P_{\Delta v}(k, t) = 16\pi^4 G^2 \bar{\rho}^2 k^2 t \int_k^\infty \frac{dq}{q} \frac{\mathcal{P}(q)}{q^6} \int d^3 \mathbf{u} \frac{f(\mathbf{u})}{u} \theta_H(qu - kv)$$



Previous:

- Mostly numerical
- Perturbations → sub-halo mass function

Relates the stellar stream perturbation to the surrounding matter distribution, from dark and luminous substructure

Simulations of *ULDM*

Very challenging!

Might be interesting to the C02 (simulation) group!

- Hybrid simulations: large scales (hydro) + small scales (SP-sims)
- Zoom-in
- Soliton mergers
 - Soliton oscillations
- Adding baryons



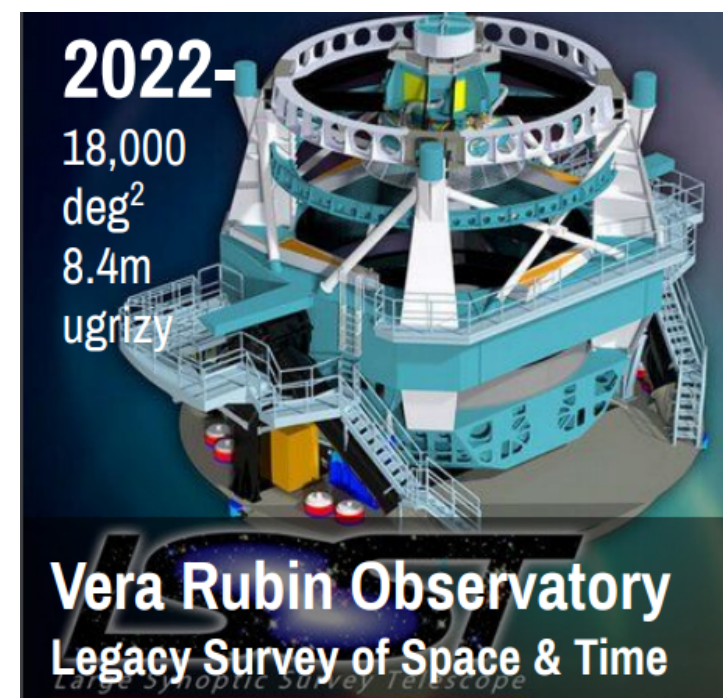
Jowett Chan

(See works from S. May & V. Springel, L. Hui, Veelmat, Niemeyer & Schwabe, Schive, Chiueh & Broadhurst, Mocz et al., ...)

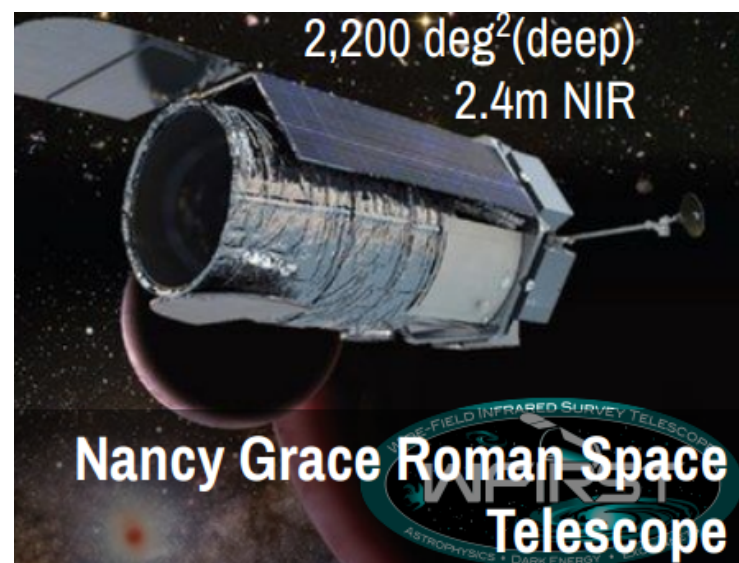
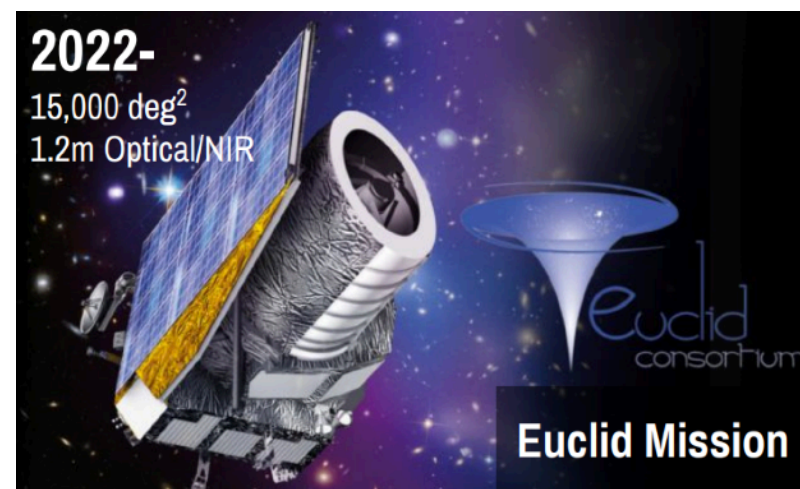
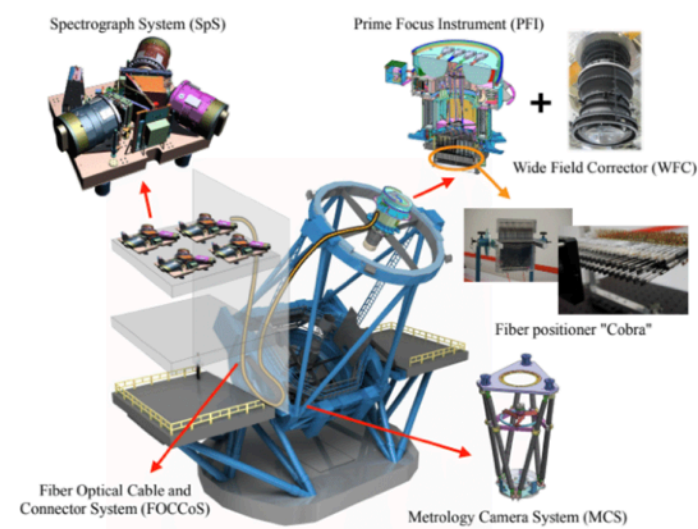
Future - signals in cosmology

Observations

Photometric and spectroscopic surveys



Prime Focus Spectrograph (PFS)



GWs

21cm



CMB

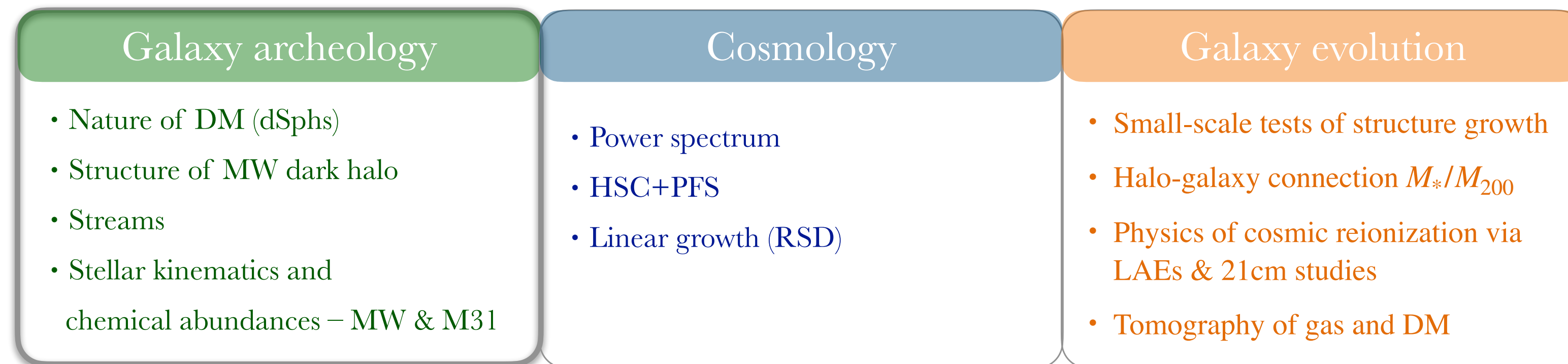


PFS (Prime Focus Spectrograph)

PFS is going to be exquisite to measure the properties of DM

PFS: spectroscopy part of *SuMIRe project*

DM with PFS → synergy between science goals



Wide & deep survey of MW dwarf galaxies w. Subaru/PFS

PFS - Galactic Archaeology

TESTING ULTRA LIGHT DM/DM with PFS

Galaxy archeology

- Nature of DM (dSphs)
- Structure of MW dark halo
- Streams
- Stellar kinematics and chemical abundances – MW & M31

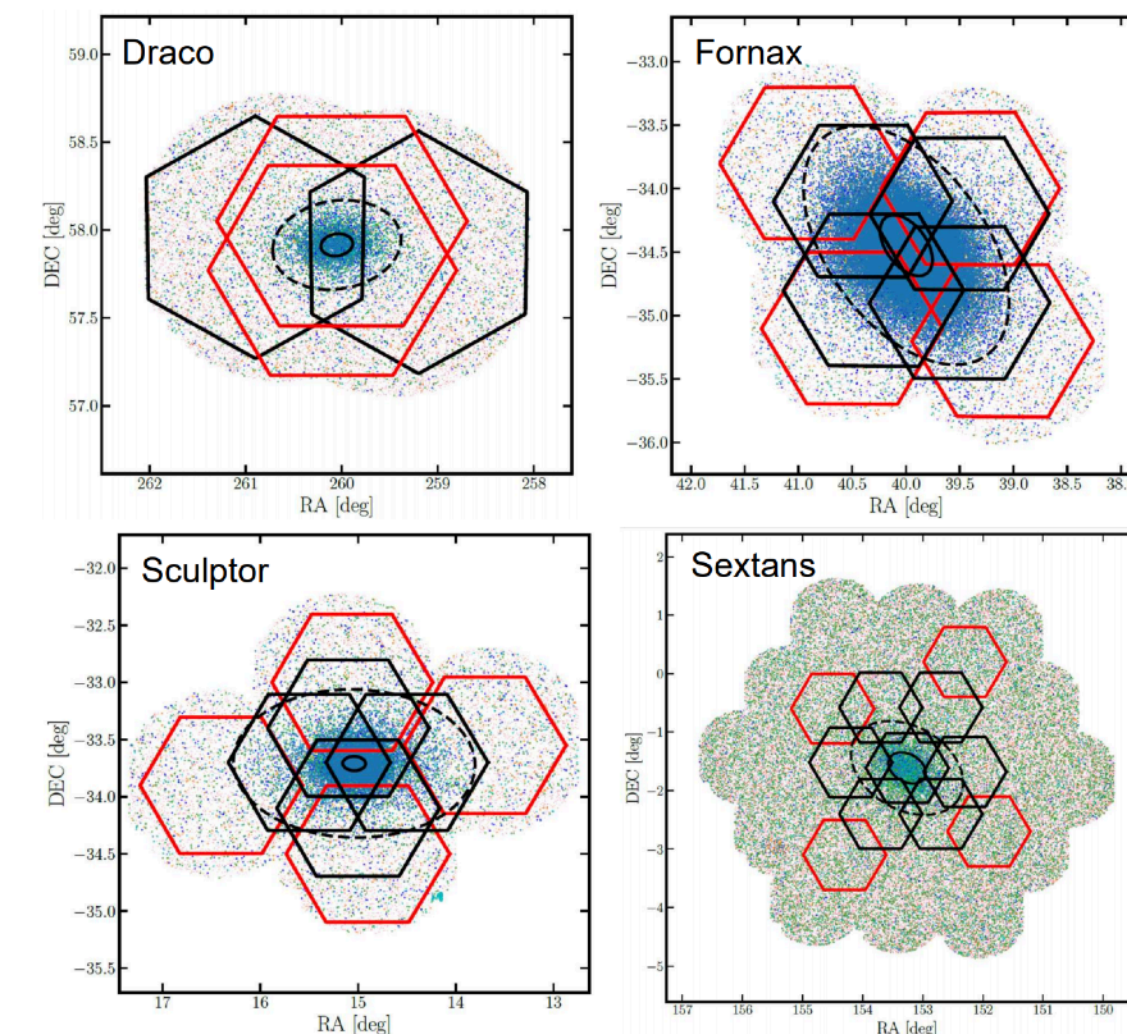
Wide & deep survey of MW dwarf galaxies w. Subaru/PFS

Dwarf galaxies:

- (1) Sample sizes in excess of 1000 stars per dSph,
- (2) Wide-area coverage well suited for dSphs,
- (3) Velocity precision much smaller than the velocity dispersion of a dSph,
- (4) Abundance measurements
- (5) Synergy with Subaru/HSC pre-imaging.

GA → potential to put unprecedented constraints on ULDM.

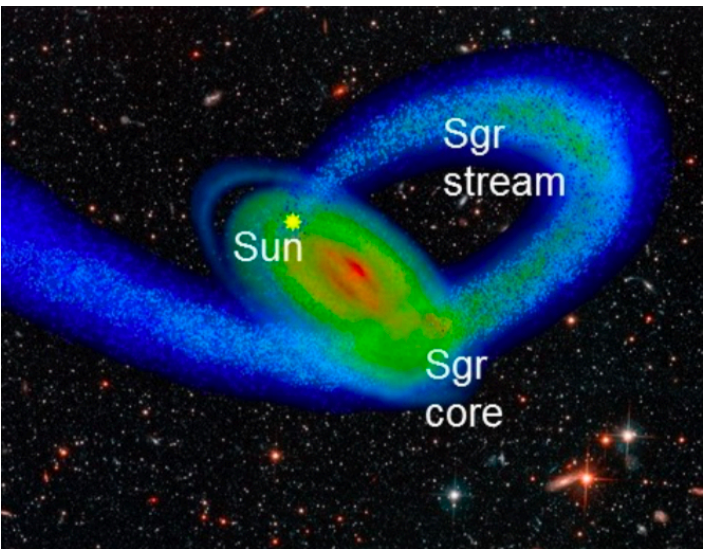
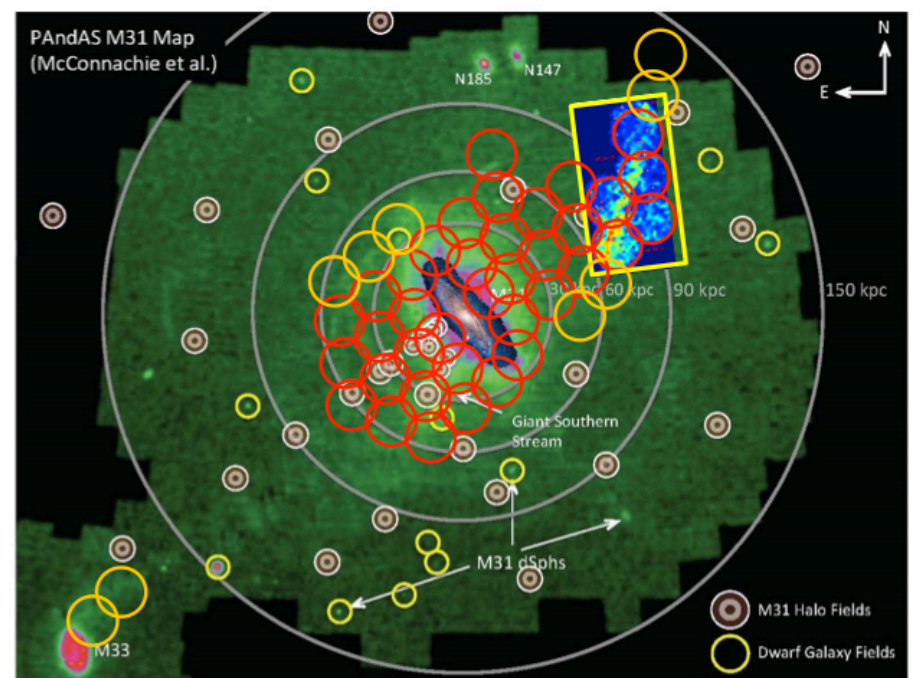
B02 group (Subaru spectroscopy)



dSphs

Stellar streams

M31



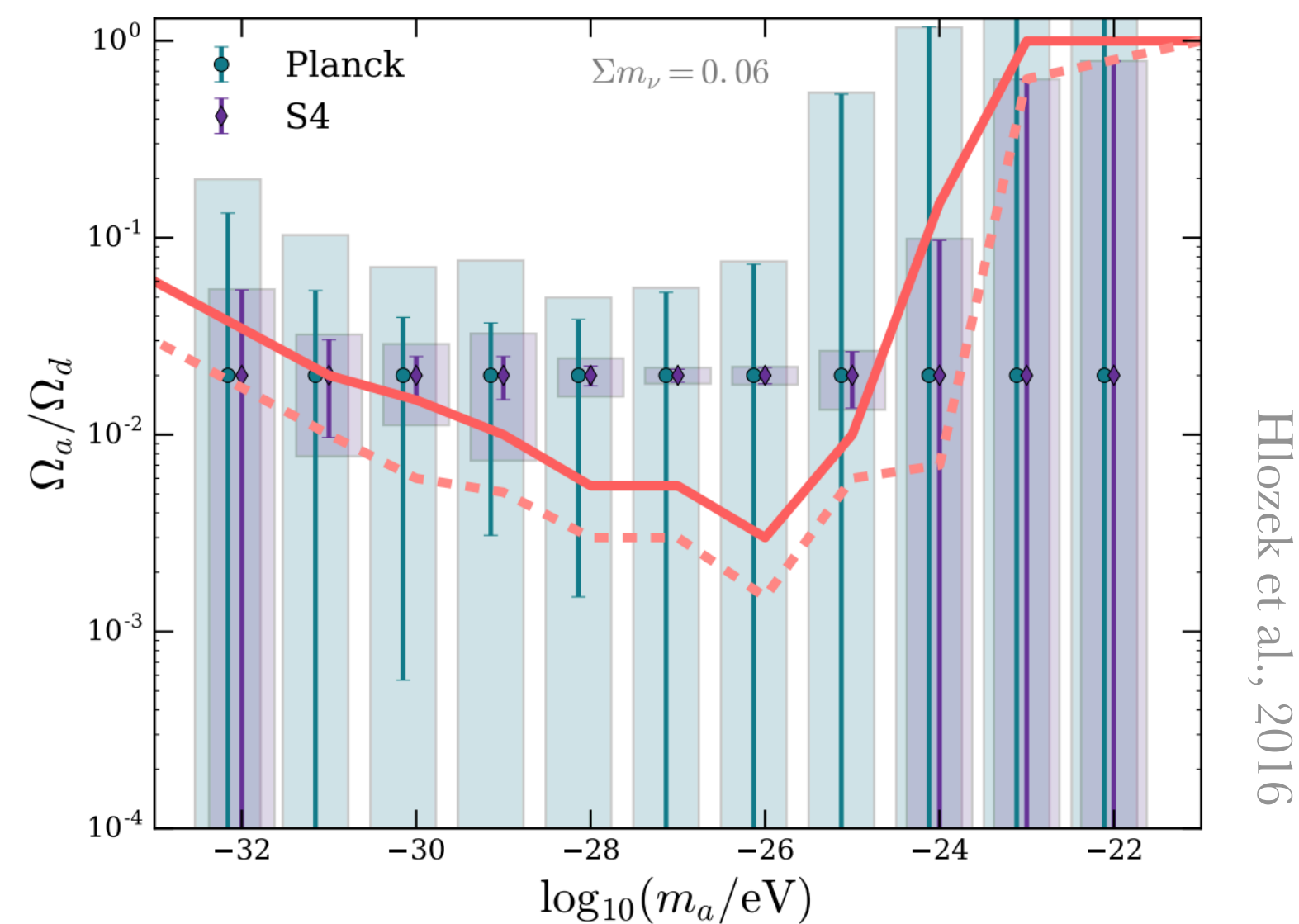
MW outer disk

Future - Cosmic Microwave Background

TESTING ULTRA LIGHT DM CMB

CMB - S4

Constraints on Ω_a/Ω_d



Significantly improve constraints on the composition of the dark sector!

Constraints on the *optical depth*

$$\tau(r_{\text{rec}})$$

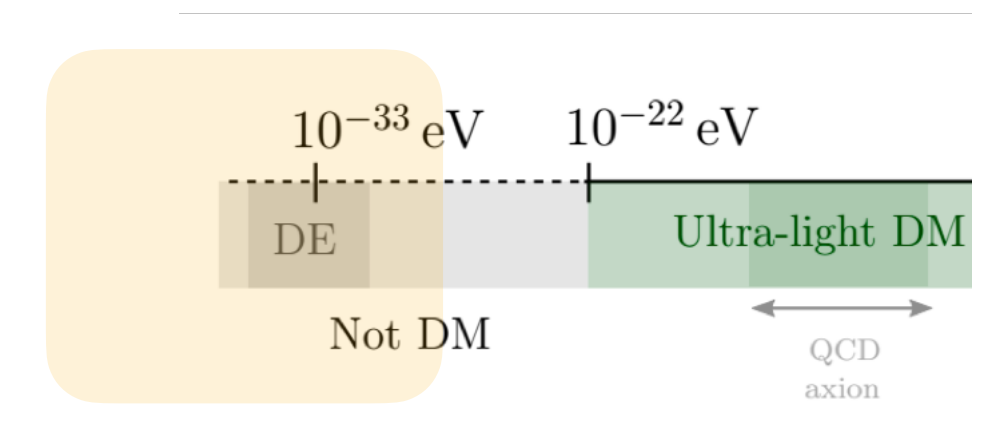
Constraint the ULDM mass

Kinematic Sunyaev-Zel'dovich effect: sensitive to the duration of the reionization

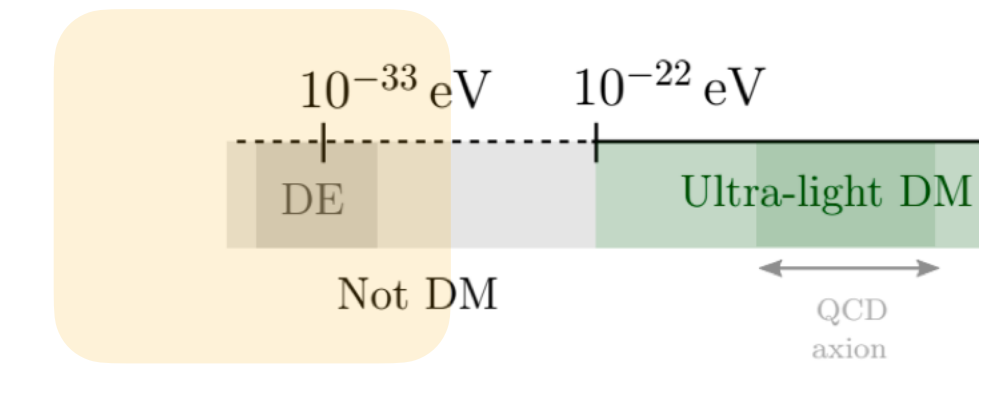
- *LiteBIRD*
- *Advances ACTPol*
- *CMB-S4*

Cosmic Birefringence

CMB and light DM groups' talks!



ALP as dark energy

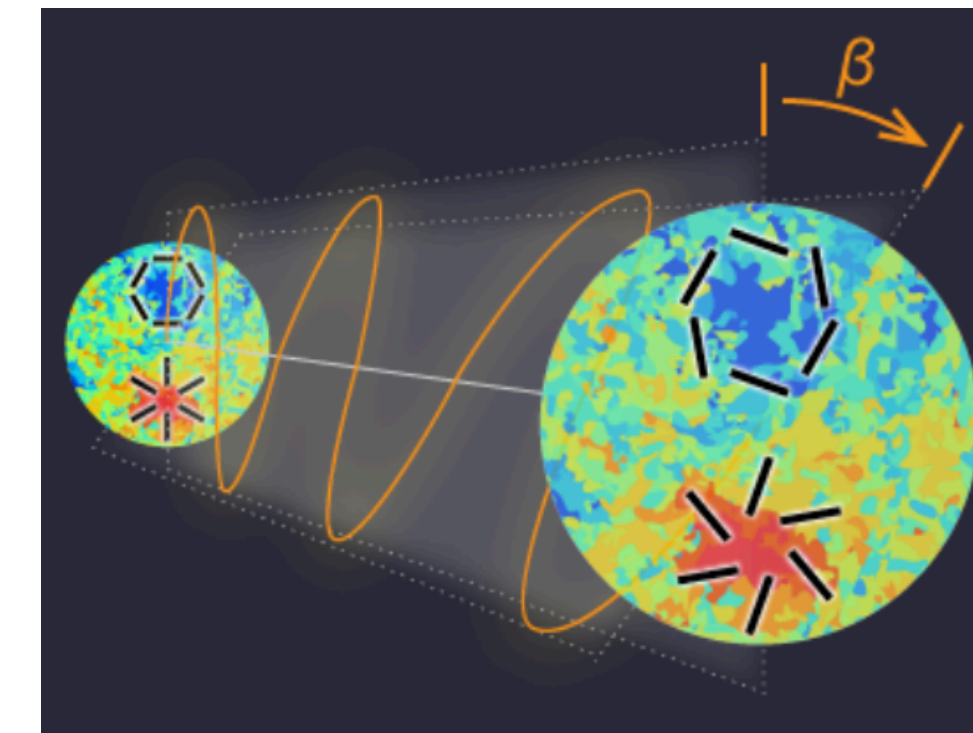


Cosmic Birefringence from axions

Parity-violating physics in polarisation of the cosmic microwave background



Rotation of the CMB polarization plane



Minami/Komatsu

Minami , Komatsu 2020

Could be cause by an **ultra-light axion** that behaves like **dark energy**

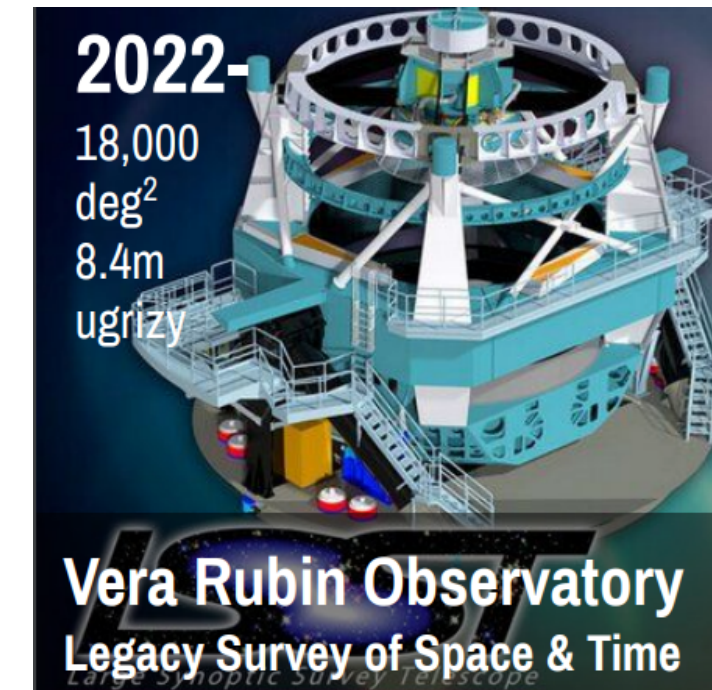
LiteBIRD can possibly constraint this effect

- Develop models with such axion
- Study their predictions
- Forecasts for LiteBIIRD

LSST probes

PFS in coordination with:

- Vera C. Rubin Legacy Survey of Space and Time (LSST)
- Atacama Large Millimeter/submillimeter Array (ALMA)
- Nancy Grace Roman Space Telescope (WFIRST)
- *Gaia*
- ...



Much stronger statistical constraints on dark matter models!

And many more creative ideas!

Summary

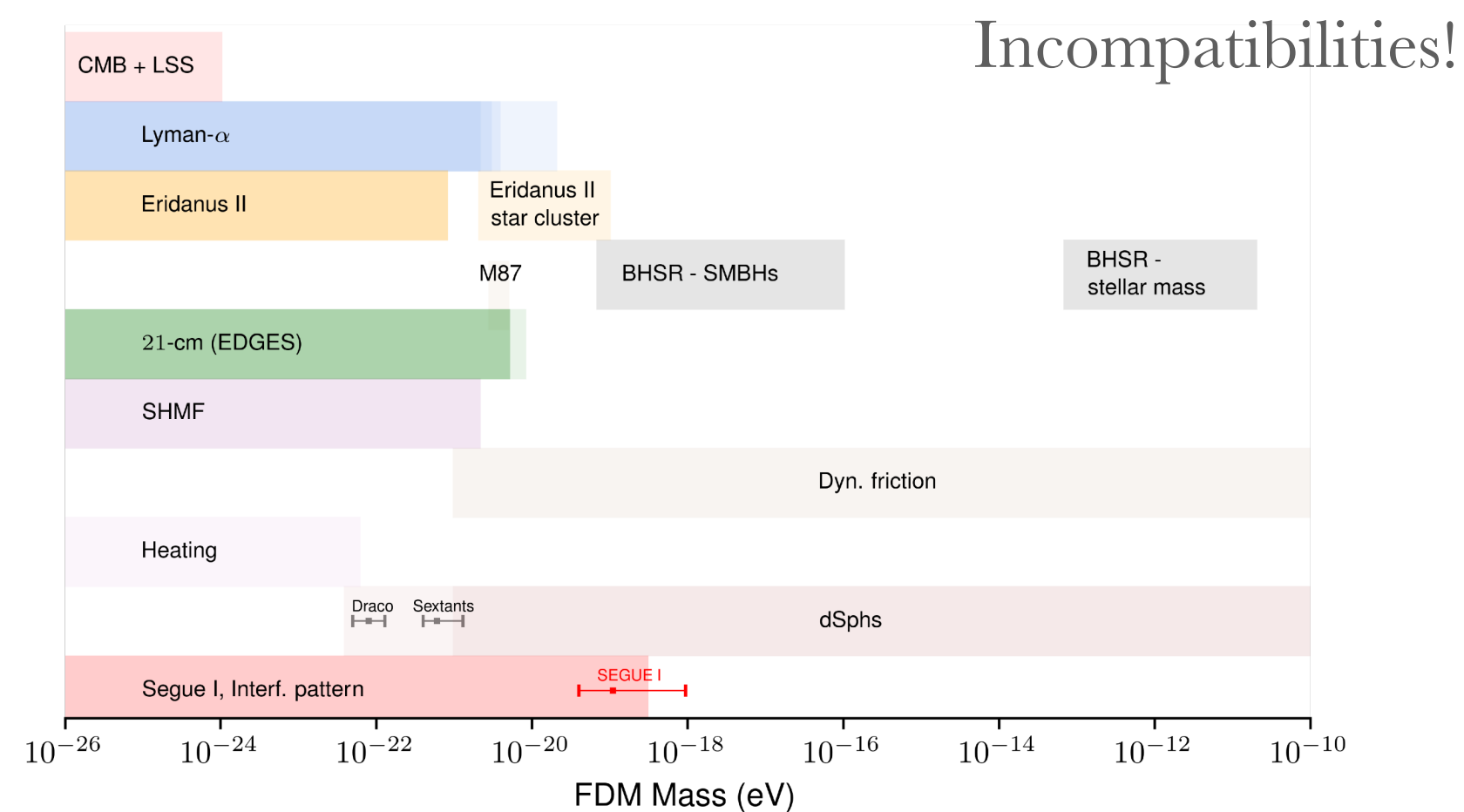
Ultra-Light Dark Matter

- Well motivated DM models
- Rich and distinct phenomenology on small scales
- Testable prediction

Small Scales

- Opportunity to probe the microphysics, particle physics properties of DM
- Small scales provide strong constraints in these models
- FDM mass being narrowed down
- Incompatibility between dwarf bounds

Current status



Future

Observations: **PFS**

PFS-GA

CMB

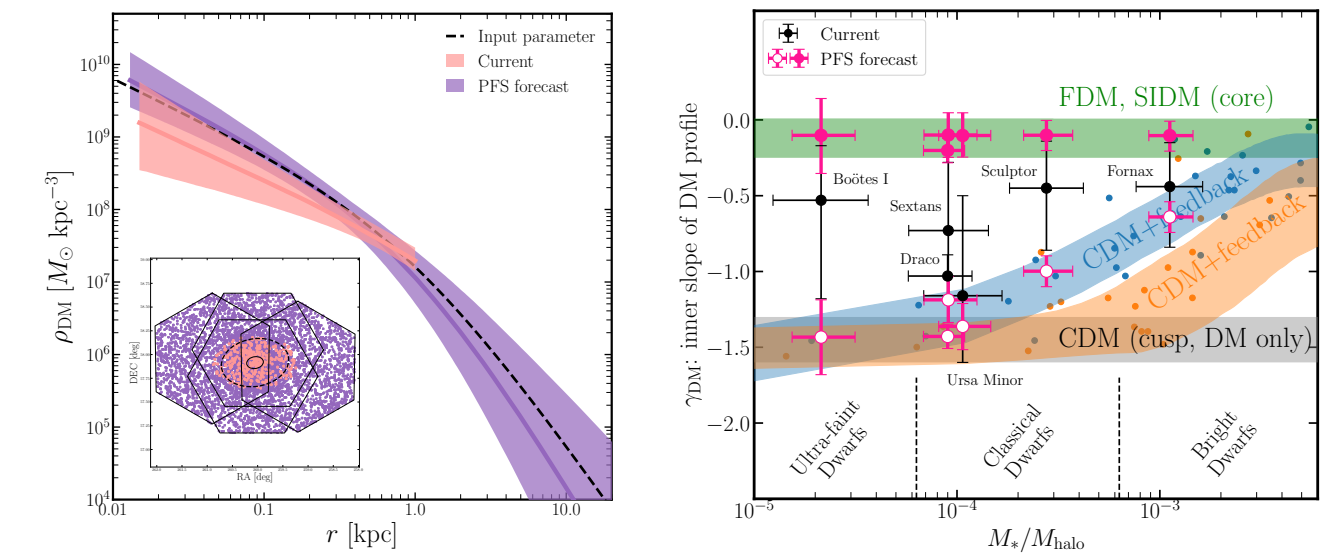
LSS

Small scales

Simulations: cosmological

New observables: interference patterns and vortices

New probes



Thank you very much!

