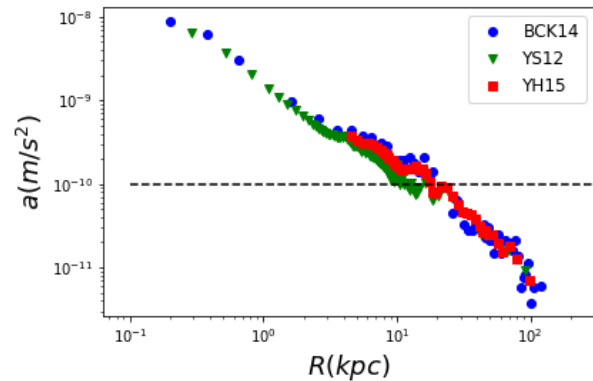


Acceleration Relations in the Milky Way as Differentiators of Modified Gravity Theories



Islam and Dutta

arXiv:1911.11836

Phys. Rev. D 101, 084015 (2020)

Dutta and Islam

arXiv:1808.06923

Phys. Rev. D 98, 124012 (2018)

Tousif Islam

Center for Scientific Computing and Visualization Research

University of Massachusetts Dartmouth



UMass
Dartmouth

With

Koushik Dutta

Saha Institute of Nuclear Physics

Indian Institute of Science Education and Research Kolkata

Cosmology at Home 2020, Virtual

Phenomenological Acceleration Relations

- Mass Discrepancy Acceleration Relation (MDAR):

$$M_{\text{obs}} \text{ and } M_{\text{bar}}$$

- Radial Acceleration Relation (RAR):

$$a_{\text{MLS}} = \frac{a_{\text{new}}^{\text{bar}}}{1 - \exp\left(-\left(\frac{a_{\text{new}}^{\text{bar}}}{a_{\dagger}}\right)^{1/2}\right)},$$

McGaugh et al 2016 - MLS

- Halo Acceleration Relation (HAR):

$$a_h = a_{\text{obs}} - a_{\text{new}}^{\text{bar}}.$$

Tian and Ko 2019

Modified Gravity Theories

- Weyl Conformal Gravity:

$$g_{\mu\nu}(x) \rightarrow \Omega^2(x)g_{\mu\nu}(x), \quad \text{Mannheim 1989}$$

$$v_{tot}^2(r) = v_{loc}^2(r) + \frac{\gamma_0 c^2 r}{2} - \kappa c^2 r^2. \quad (3.4)$$

The corresponding centripetal acceleration is thus : $\frac{v_{tot}^2(r)}{r}$.
 The values of the four universal Weyl gravity parameters are fixed by previous fits to the rotation curves of ~ 100 galaxies [26–28]: $\beta^* = 1.48 \times 10^5 \text{ cm}$; $\gamma^* = 5.42 \times 10^{-41} \text{ cm}^{-1}$; $\gamma_0 = 3.06 \times 10^{-30} \text{ cm}^{-1}$ and $\kappa = 9.54 \times 10^{-54} \text{ cm}^{-2}$.

Islam and Dutta 2020

- MOND:

$$a_{MOND} = \frac{a_N}{\sqrt{2}} \left[1 + \left(1 + \left(\frac{2a_0}{a_{new}^{bar}} \right)^2 \right)^{1/2} \right]^{1/2}, \quad \text{Milogram 1983}$$

Milky Way: Kinematics Data

Bhattacharjee et al 2014 –
BCK14

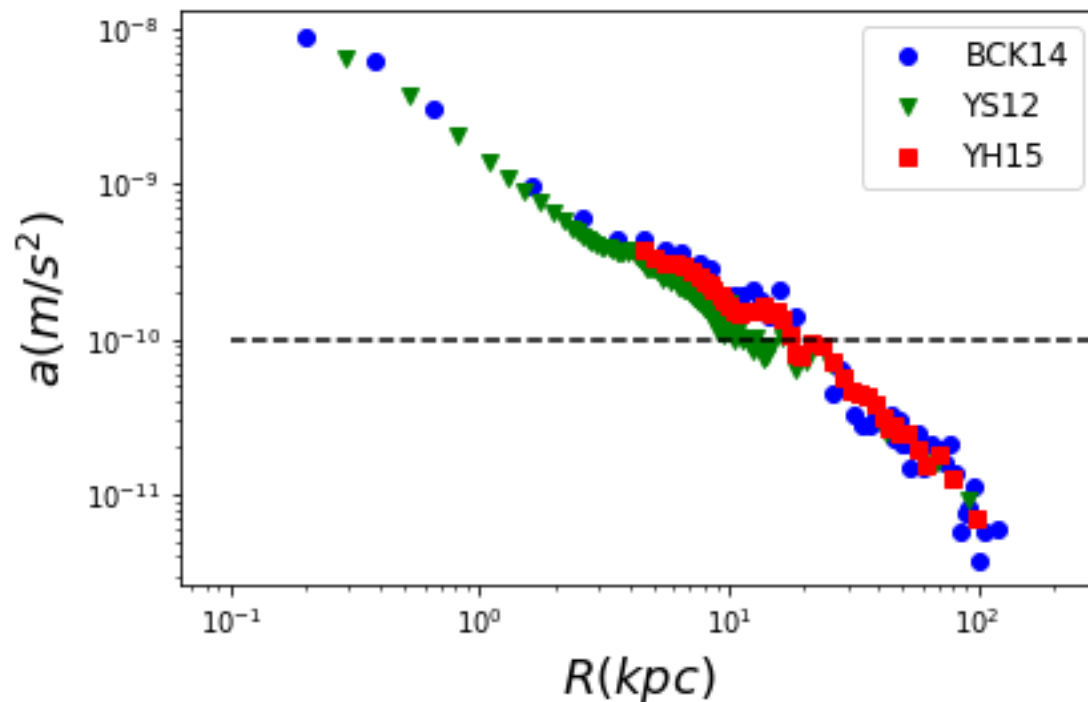
49 Points

Sofue 2012 – YS12

123 Points

Huang et al 2016 – YH16

43 Points



Milky Way: Mass Model

Bulge

Valenti et al 2016

$$\rho(r) = \frac{M_{bulge}}{2\pi^2 t^3} K_0(r/t),$$

Disk

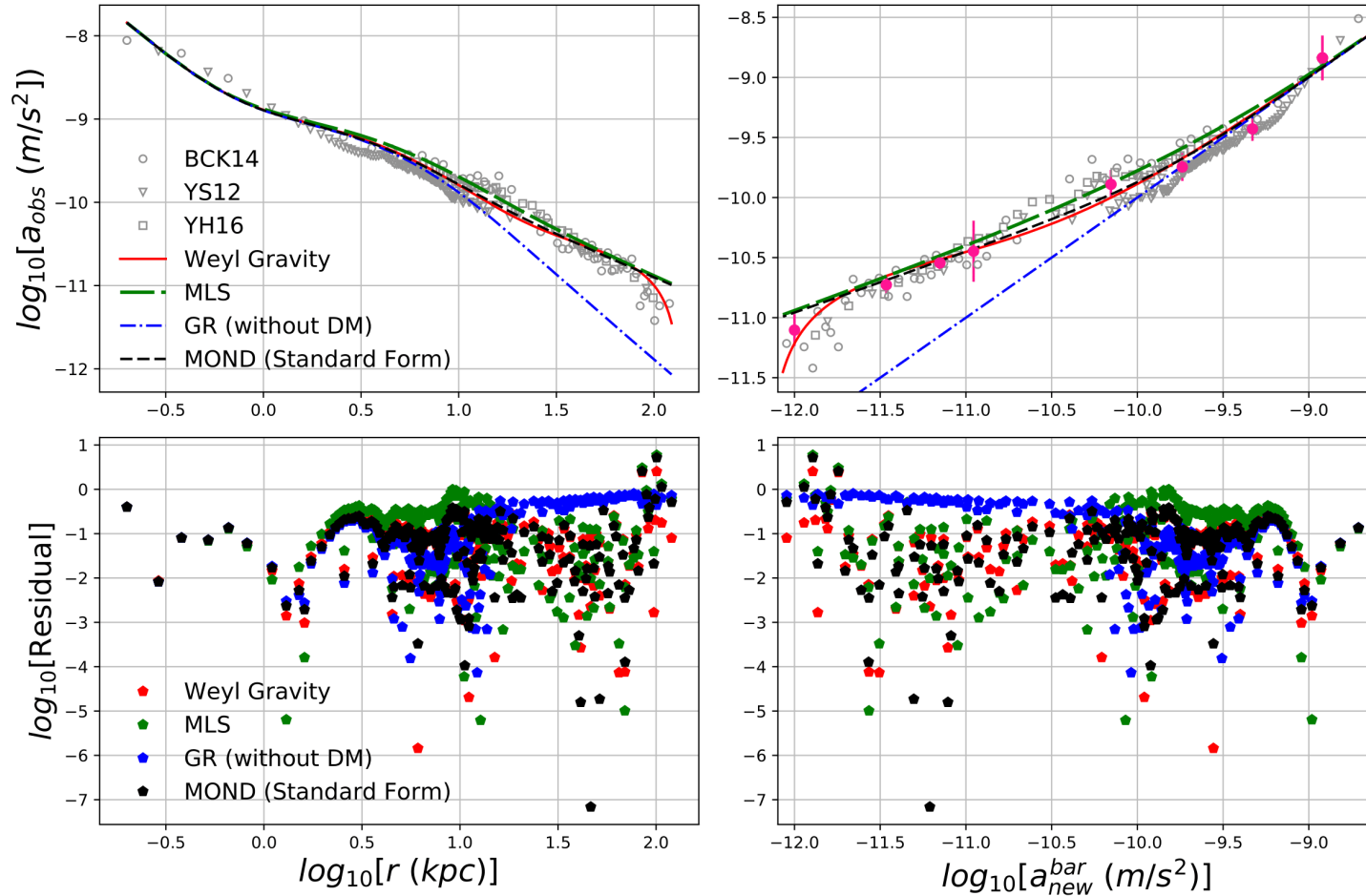
McMilan 2016

$$\Sigma(r) = \Sigma^0 e^{-r/R},$$

TABLE I: Parameters for the Milky Way mass model [22]

	Σ_0	R
Thin Stellar Disk	$886.7 \pm 116.2 M_\odot pc^{-2}$	2.6 ± 0.52 kpc
Thick Stellar Disk	$156.7 \pm 58.9 M_\odot pc^{-2}$	3.6 ± 0.72 kpc
HI Disk	$1.1 \times 10^{10} M_\odot$	7.0 kpc
H2 Disk	$1.2 \times 10^9 M_\odot$	1.5 kpc

Radial Acceleration Relation (RAR)

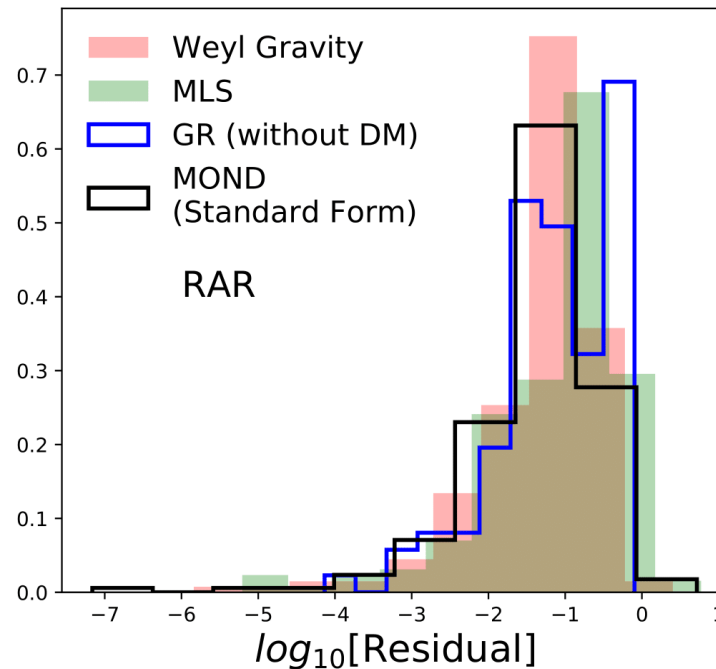


$$\text{Residual} = (Data - Model)^2 / Data^2.$$

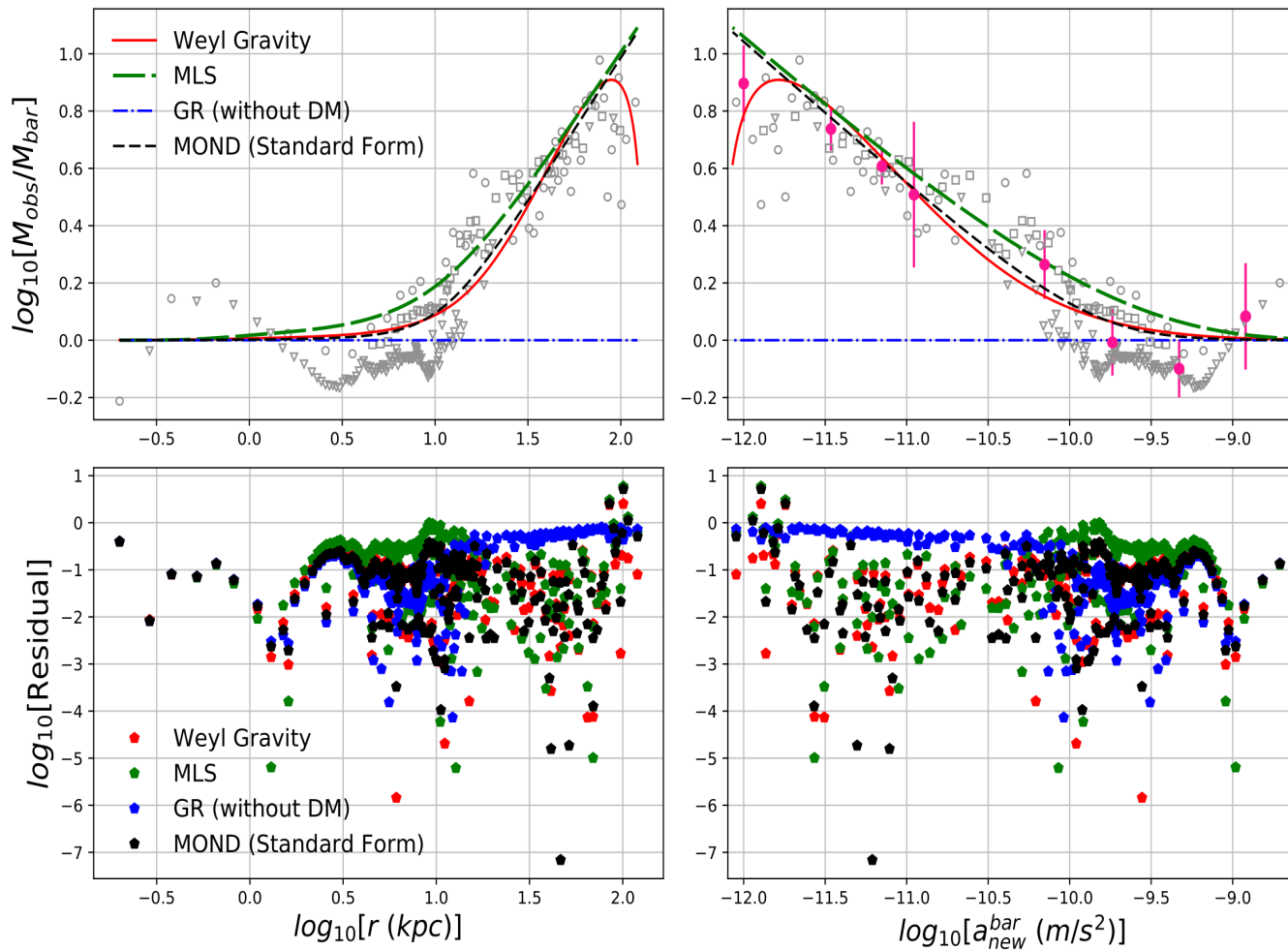
Radial Acceleration Relation (RAR)

TABLE II: **Reduced chi-square values as goodness-of-fits for different theories of gravity and RAR scaling law. No dark matter is assumed. (Section IV A in text)**

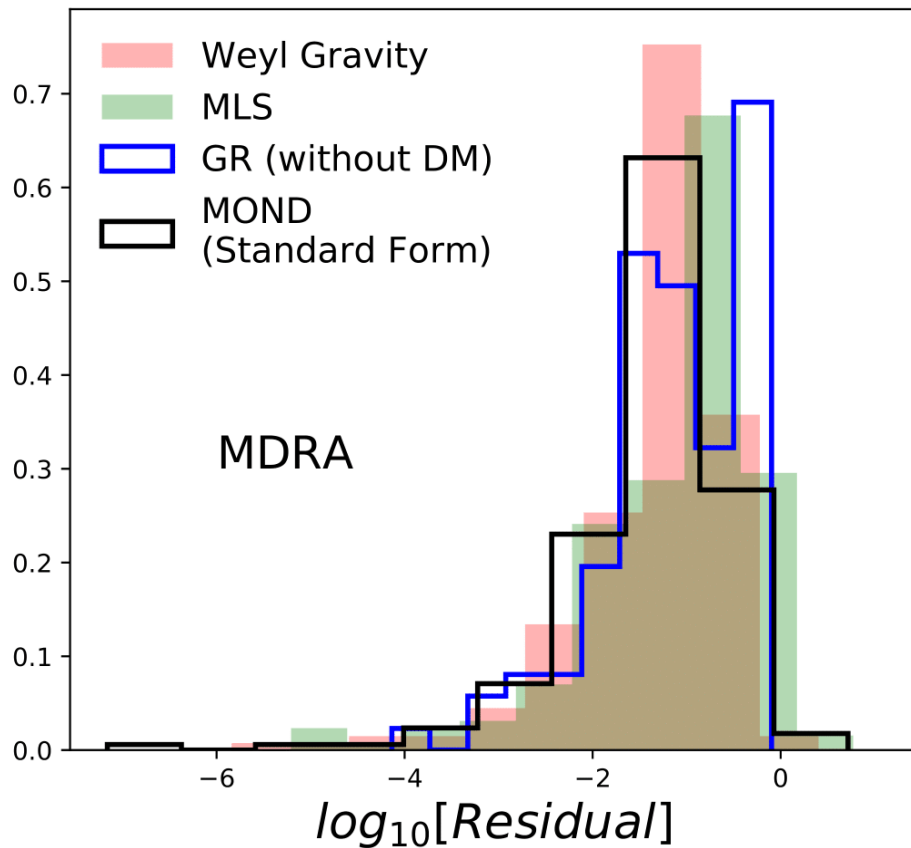
	χ^2/dof
General Relativity (GR) without dark matter	7.56
MOND (Standard Form)	5.90
Weyl Conformal Gravity	6.11
Radial Acceleration Relation / MLS 2016	5.71



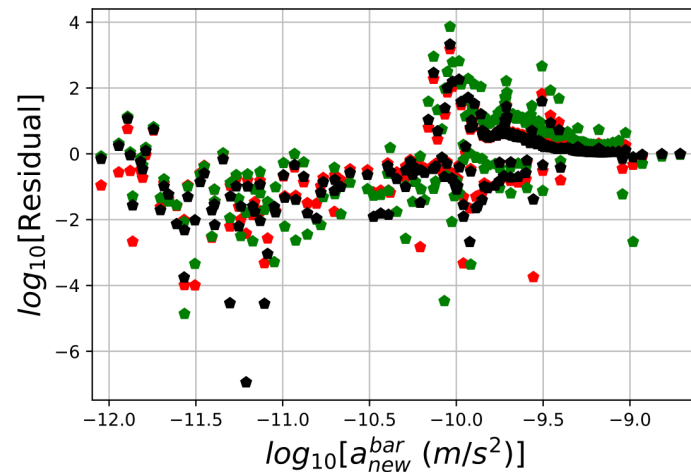
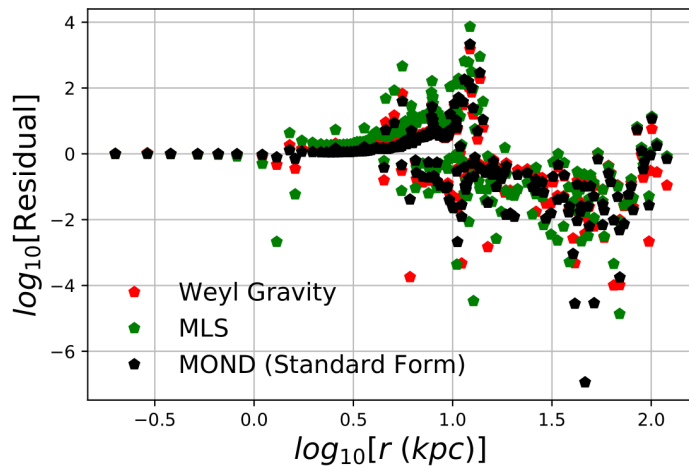
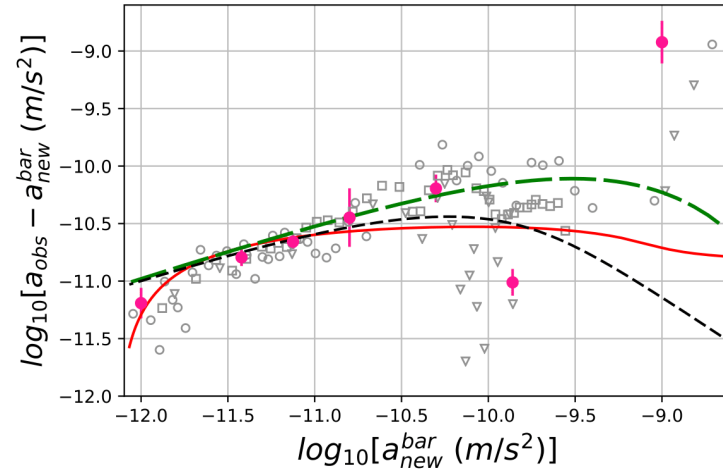
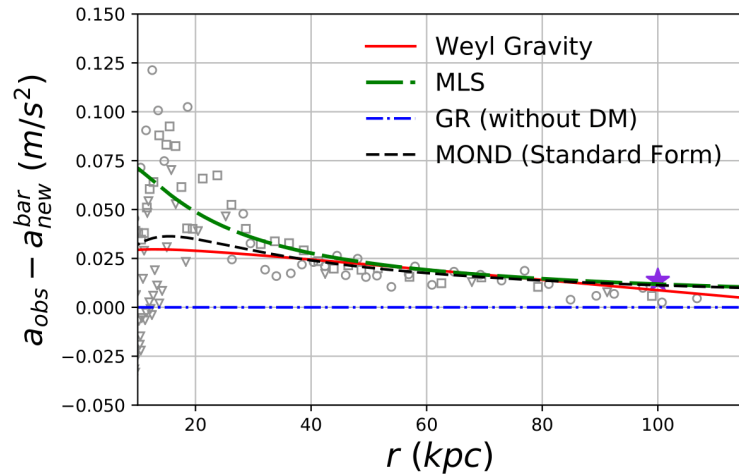
Mass Discrepancy Acceleration Relation (MDAR)



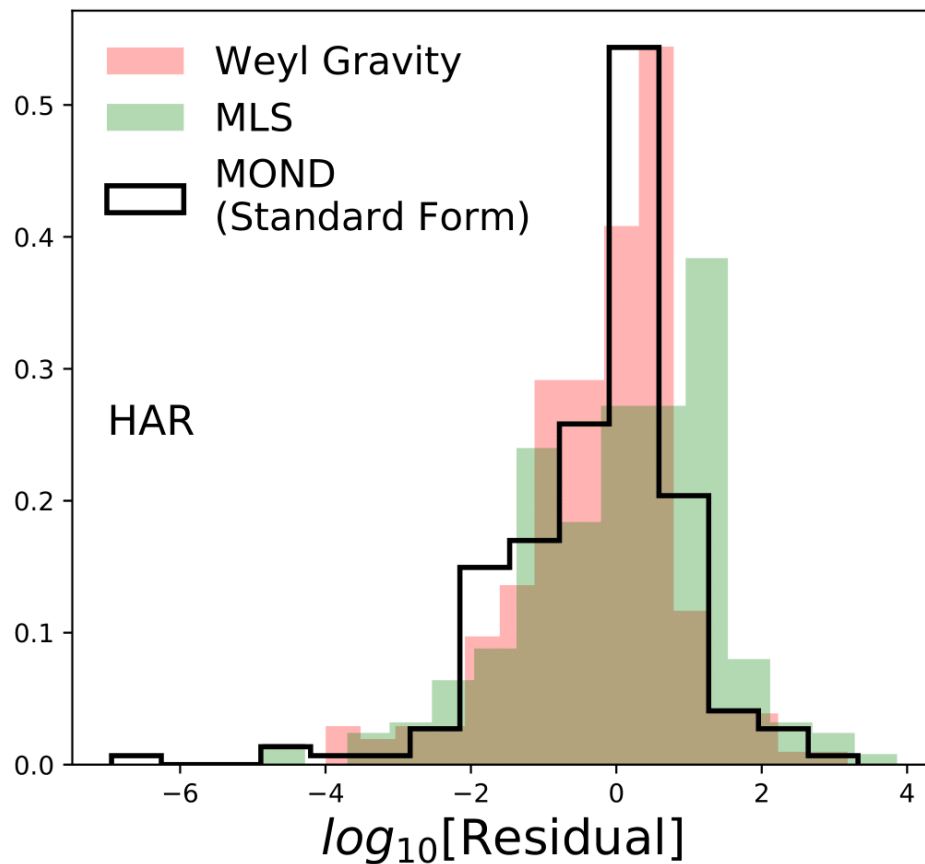
Mass Discrepancy Acceleration Relation (MDAR)



Halo Acceleration Relation (HAR)



Halo Acceleration Relation (HAR)



Conclusion

- Both the modified gravity theories in question as well as RAR can explain the radial acceleration data well
- Data in the $a_{\text{obs}} - a_{\text{new}}^{\text{bar}}$ plane is unable to discriminate between different models or gravity and scaling laws
- $a_{\text{halo}} - a_{\text{new}}^{\text{bar}}$ plane gives a stronger test for them
- Both the high acceleration and low acceleration regime becomes equally important for such test