



# Common Origin of Warm Dark Matter & Dark Radiation

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BROWN

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# Outline

- I. Motivation
- II. Model
- III. Results
- IV. Outlook and Conclusions

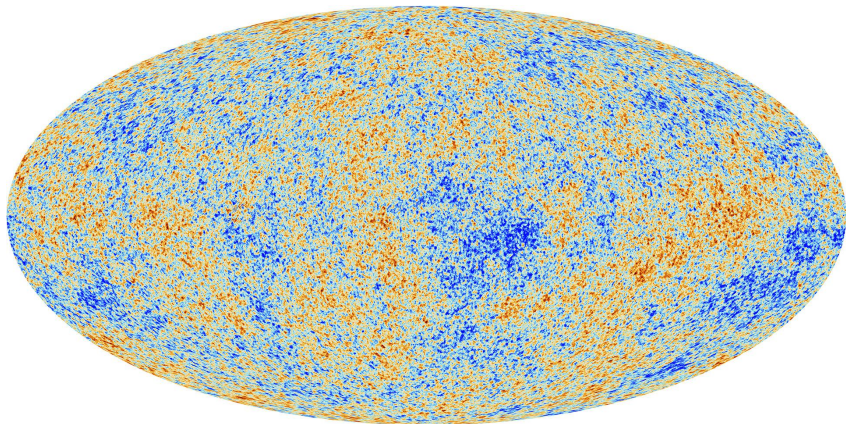
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# I. Motivation

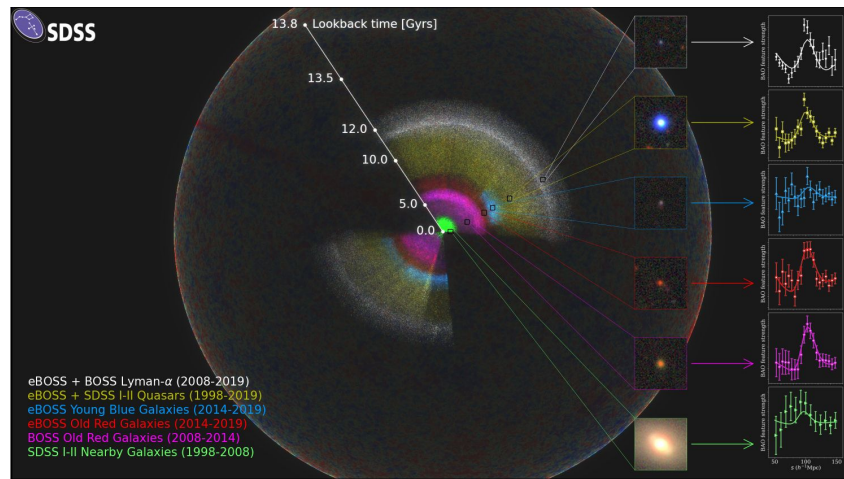


# Precision Cosmology

e.g.:



CMB - Planck



MPS - SDSS



## Standard Framework

ΛCDM



# However...

## Experimental Tensions, e.g:

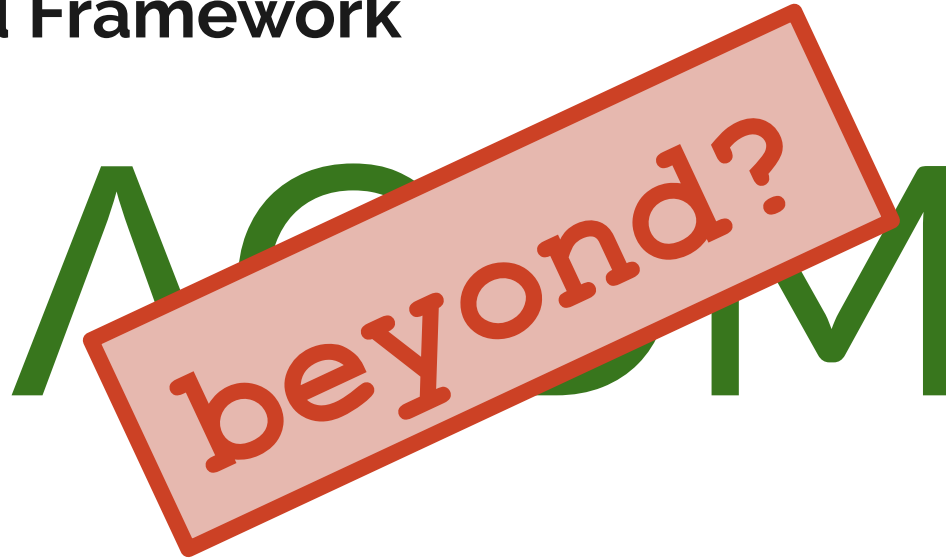
- **$H_0$  crisis:** Direct > Indirect
  - SH0ES etc. v. Planck
  - recent reviews: [1907.10625](#) [2001.03624](#)
- **$\sigma_8$ :** Direct < Indirect
  - KiDS etc. v. Planck
  - recent results: [2007.15632](#)

## Theoretical Motivations, e.g.:

- DM origin  $\Rightarrow$  rich DS
- Particle Physics Problems:
  - Hierarchy: SUSY & WIMPs
  - Strong CP: axions
  - $\nu$  Masses: sterile neutrinos



# Standard Framework





# Dark Sectors

- Dark Matter...
- ... Dark Radiation...
- ... also Dark Energy







## Beyond $\Lambda$ CDM: common paths

Dark Radiation (DR):  $\Delta N_{\text{eff}}$

$$\Delta N_{\text{eff}} \frac{\pi^2}{30} \frac{7}{4} \left( \frac{4}{11} \right)^{\frac{4}{3}} T^4$$

- CMB: peaks, damping, equality...
- MPS: increase structure &  $\sigma_8$  [maintain equality]

Warm Dark Matter (WDM):  $f_{\text{wdm}}$

$$a_{\text{r...}} (\propto 1/T_{\text{...}})$$

$$\lambda_{\text{FS}} \simeq 4 \text{ Mpc} \left( \frac{100 \text{ eV}}{T_{\text{nr}}} \right) \left( \frac{\ln(T_{\text{nr}}/T_{\text{eq}})}{5} \right)$$

- MPS: Free-streams  $\Rightarrow$  suppresses structure

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## II. Model

# Common Origin of Warm and Relativistic Decay particles

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**C**ommon  
**O**rigin of  
**W**arm  
**a**nd  
**R**elativistic  
**D**ecay particles

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**COWaRD:**

$$X_1 \longrightarrow X_2 + \varphi$$

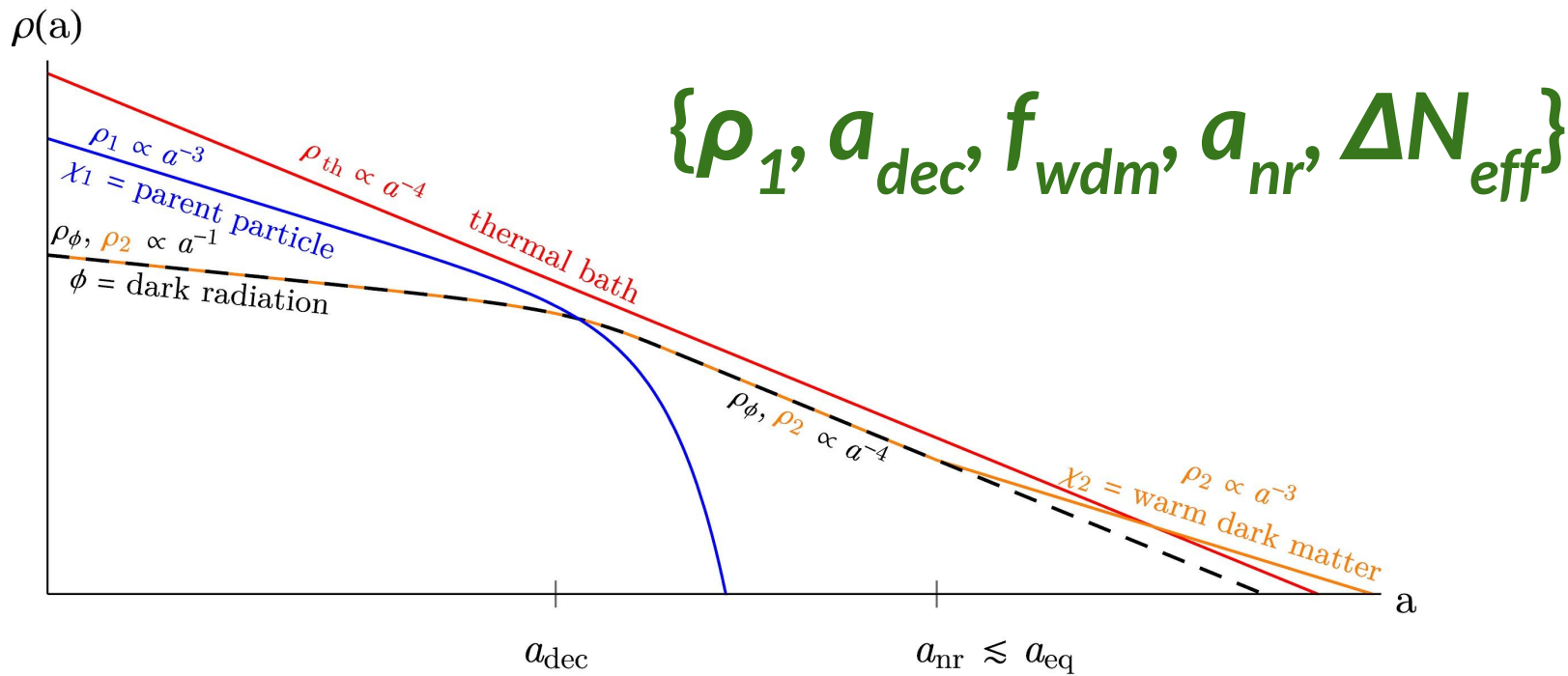
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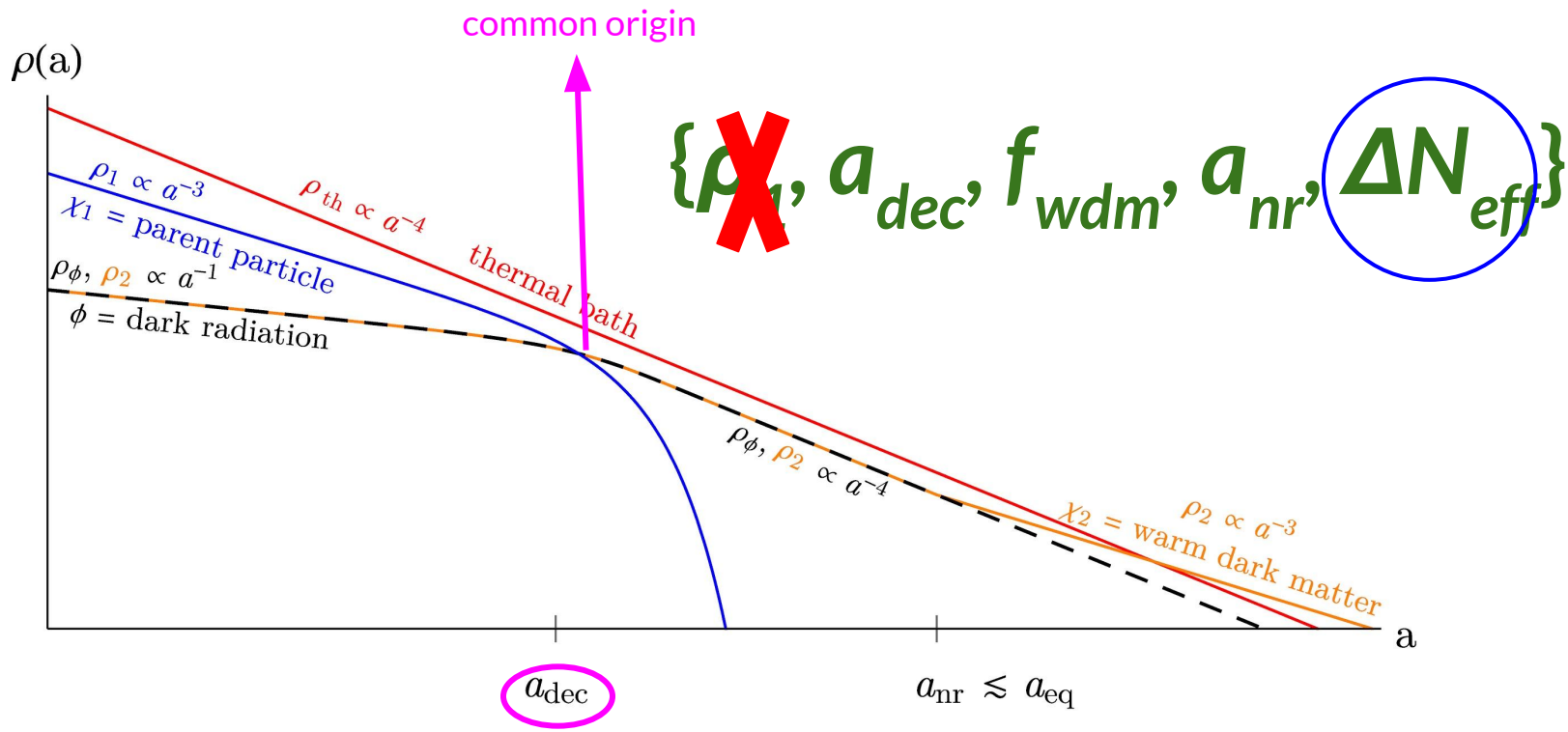
## COWaRD: $\chi_1 \rightarrow \chi_2 + \varphi$

- $\chi_1$ : Decaying DM
  - Unstable massive parent
  - $\rho_1, \Gamma \Rightarrow a_{dec}$
- $\chi_2$ : WDM
  - Stable massive daughter
  - $f_{wdm}, a_{nr}$
- $\varphi$ : DR
  - Lightest/massless daughter
  - $\Delta N_{eff}$

$$\{\rho_1, a_{dec}, f_{wdm}, a_{nr}, \Delta N_{eff}\}$$

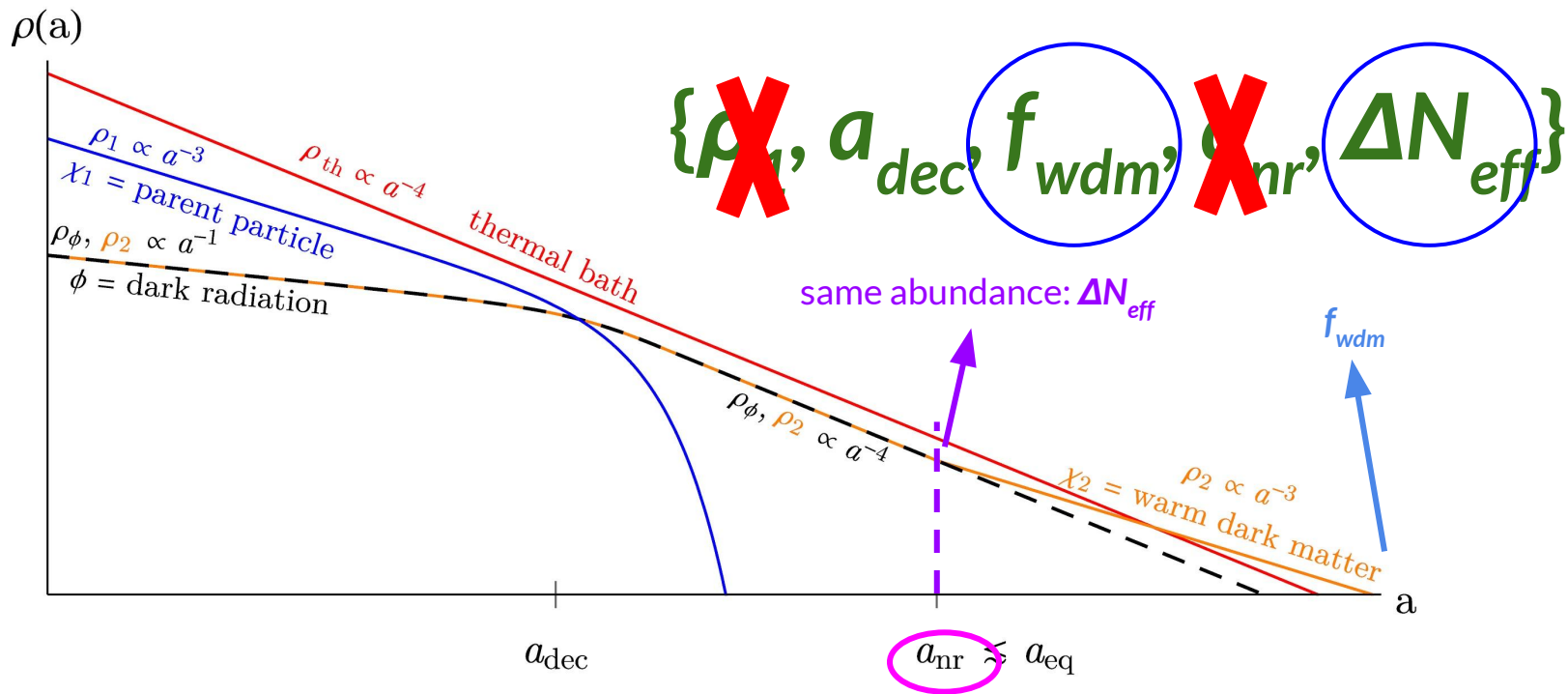


COWaRD Thermal History

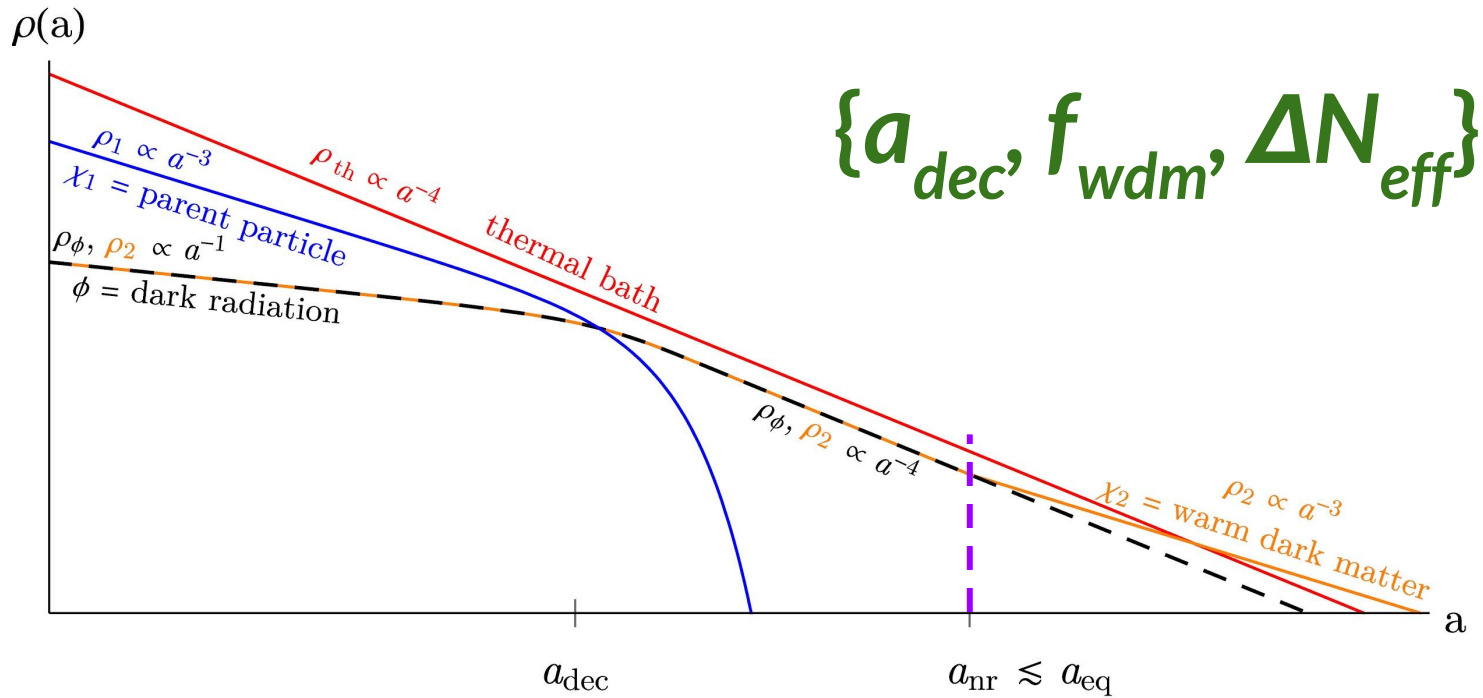


COWaRD Thermal History



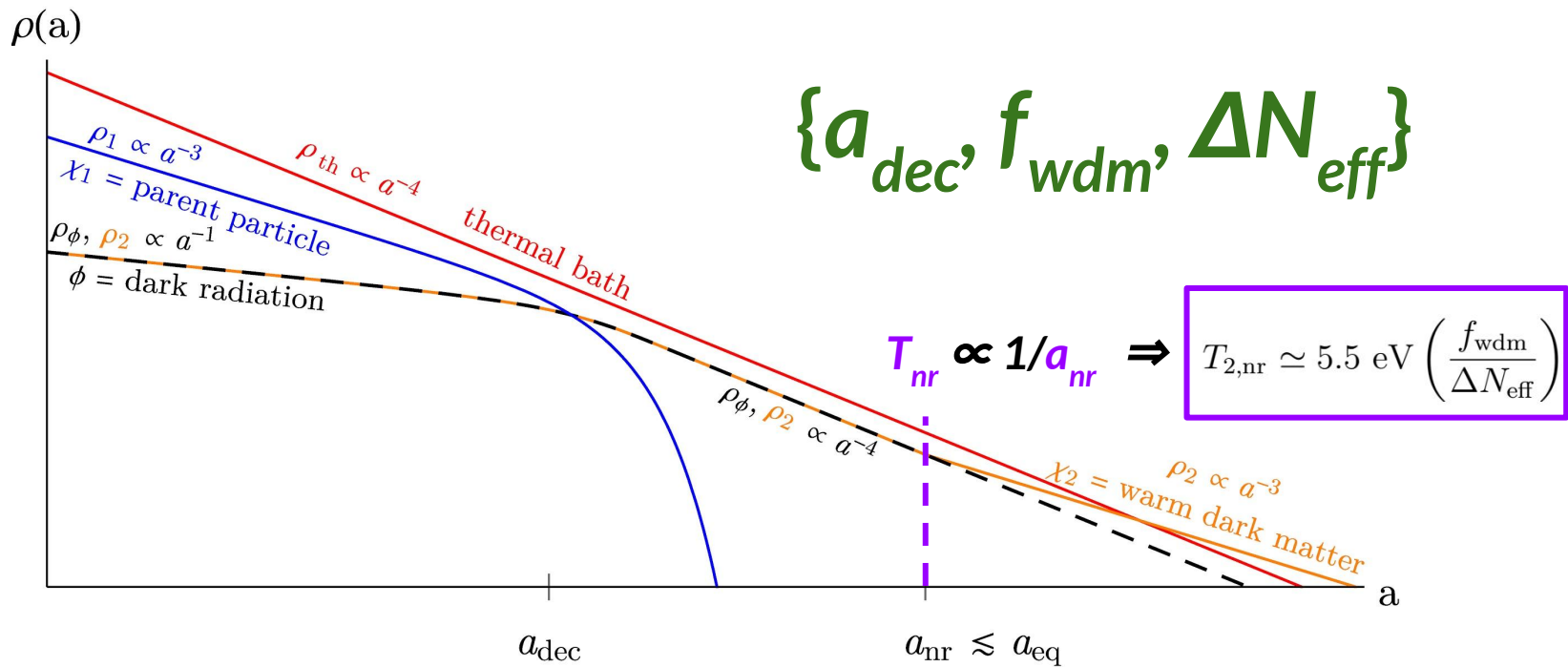


COWaRD Thermal History



COWaRD Thermal History

$$a_{\text{nr}} \propto \frac{\Delta N_{\text{eff}}}{f_{\text{wdm}}}$$



$\{a_{dec}, f_{wdm}, \Delta N_{eff}\}$

$a_{nr} \propto \frac{\Delta N_{eff}}{f_{wdm}}$

COWaRD Thermal History

$$\lambda_{\text{FS}} \simeq 4 \text{ Mpc} \left( \frac{100 \text{ eV}}{T_{\text{nr}}} \right) \left( \frac{\ln(T_{\text{nr}}/T_{\text{eq}})}{5} \right) \quad \text{WDM}$$

$$T_{2,\text{nr}} \simeq 5.5 \text{ eV} \left( \frac{f_{\text{wdm}}}{\Delta N_{\text{eff}}} \right) \quad \text{COWaRD}$$

$$\lambda_{\text{FS}} \simeq 4 \text{ Mpc} \left( \frac{100 \text{ eV}}{T_{\text{nr}}} \right) \left( \frac{\ln(T_{\text{nr}}/T_{\text{eq}})}{5} \right) \quad \text{WDM}$$


$$\lambda_{\text{FS}} \sim \Delta N_{\text{eff}} / f_{\text{wdm}}$$

$$T_{2,\text{nr}} \simeq 5.5 \text{ eV} \left( \frac{f_{\text{wdm}}}{\Delta N_{\text{eff}}} \right) \quad \text{COWaRD}$$

$$\lambda_{\text{FS}} \simeq 4 \text{ Mpc} \left( \frac{100 \text{ eV}}{T_{\text{nr}}} \right) \left( \frac{\ln(T_{\text{nr}}/T_{\text{eq}})}{5} \right)$$

WDM

$$\lambda_{\text{FS}} \sim \Delta N_{\text{eff}} / f_{\text{wdm}}$$

$$\sigma_8 \leftrightarrow \Delta N_{\text{eff}}$$

COWaRD: anti-correlated  
(naive DR: correlated)

$$T_{2,\text{nr}} \simeq 5.5 \text{ eV} \left( \frac{f_{\text{wdm}}}{\Delta N_{\text{eff}}} \right)$$

COWaRD

# BSM COWaRD examples

$\chi_1 \rightarrow \chi_2 + \phi$ : SUSY + axions

- axino  $\rightarrow$  gravitino + axion
- gravitino  $\rightarrow$  axino + axion

$\{m_1, m_2, N_{1,ini}\}$

particle physics



$\{a_{dec}, f_{wdm}, \Delta N_{eff}\}$

cosmology

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# III. Results





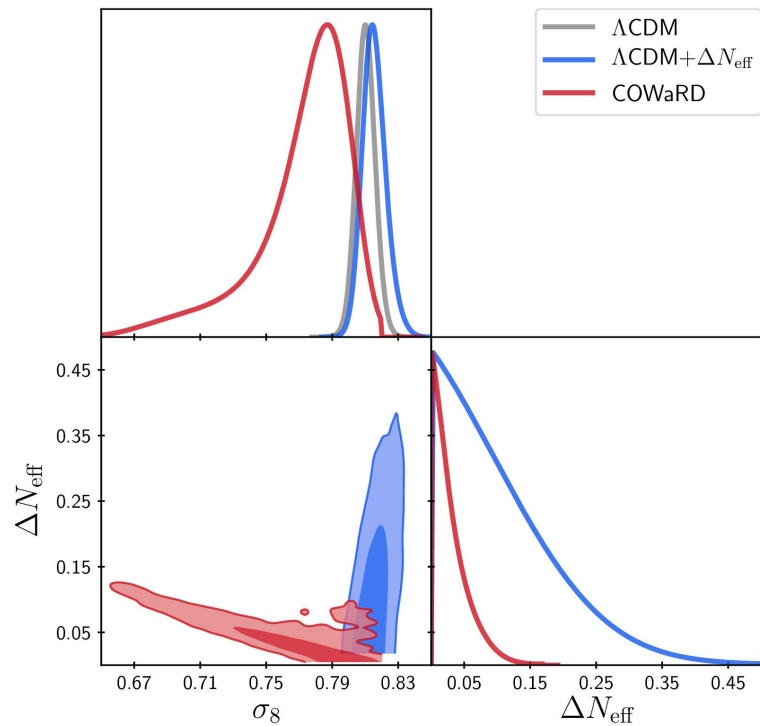
# Implementation

## Numerics

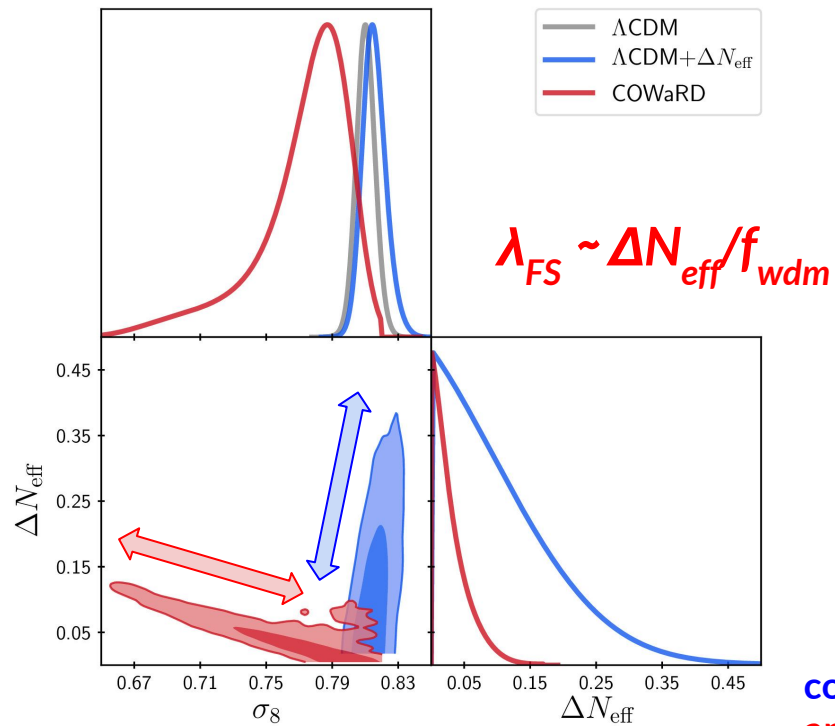
- CLASS Boltzmann solver
- MontePython MCMC
  - Small  $a_{dec}$  no effect on fit  $\Rightarrow$  assumed  $\chi_1$  already decayed (fixed  $a_{dec} = 10^{-7}$ )
  - $\Rightarrow$  Fit only  $\{\Delta N_{eff}, f_{wdm}\}$

## Data

- CMB: Planck TT+TE+EE+lens
- BAO: 6dFGS+SDSS+BOSS
- **No  $\sigma_8$  data**

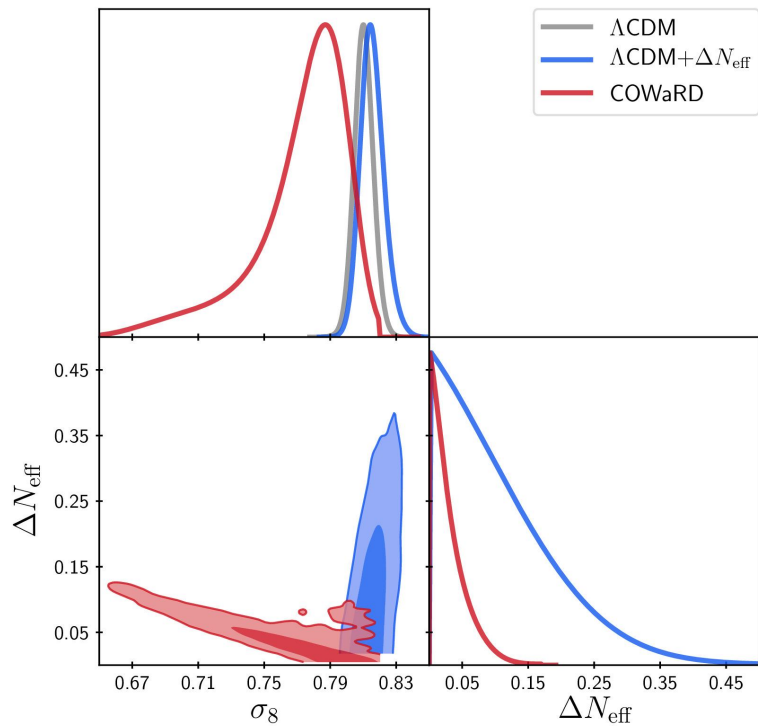


## Numerical Results

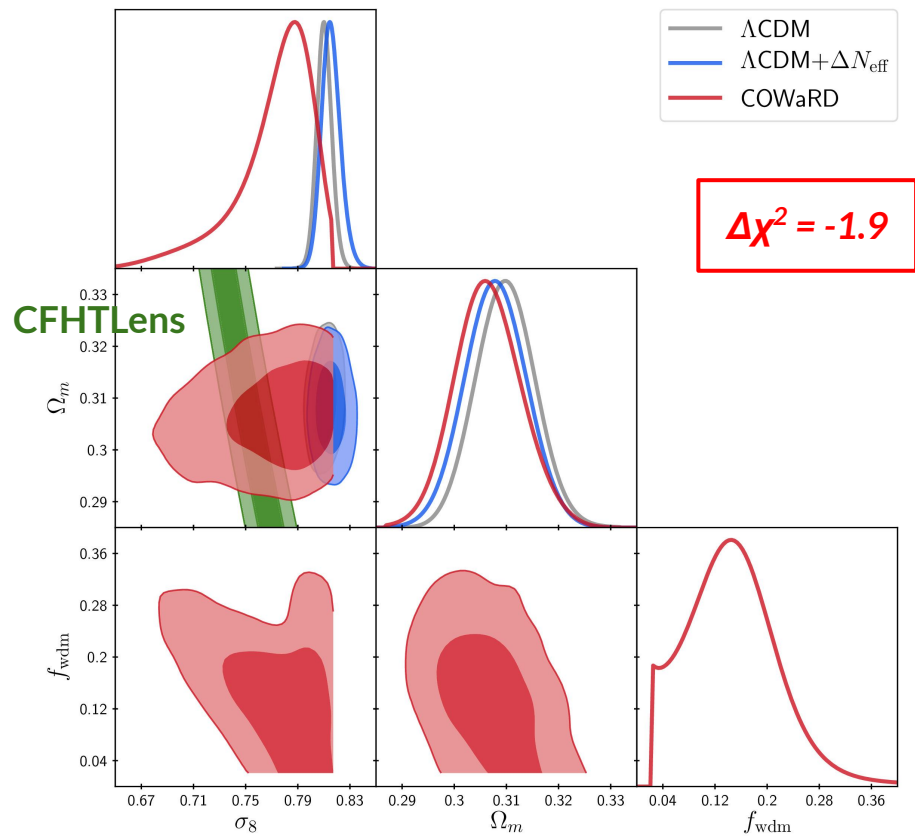


**correlated:** usual DR ( $\Delta N_{eff}$ ) behavior  
**anti-correlated:** COWaRD

Numerical Results



Numerical Results

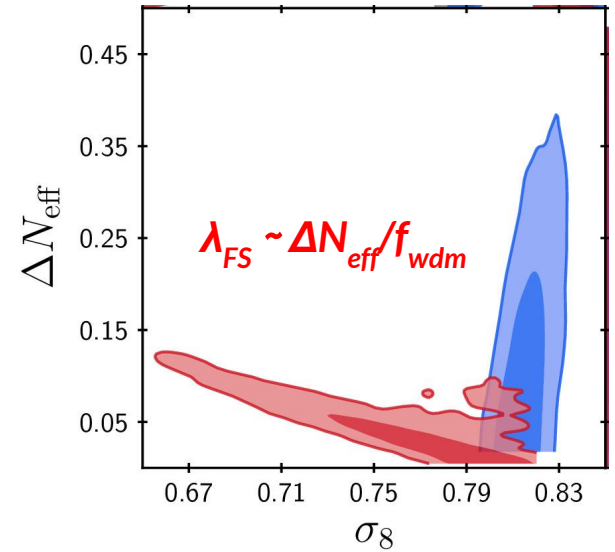


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# IV. Outlook & Conclusions

# Outlook

- CMB-S4:  $\Delta N_{eff} \geq 0.03$ 
  - COWaRD fit to CMB: predicts  $\sigma_8(\Delta N_{eff})$
- Future work:
  - Full decay implementation (solve psd function)





# Conclusions

## Particular: COWaRD

- Theoretically motivated model
- Solves  $\sigma_8$  tension w/o degrading CMB fit, *and w/o asking it to!*
- Combines DR & WDM
  - Interesting effects
  - Few parameters

## General: moral

- **Naive  $\Lambda$ CDM extensions  $\neq$  their actual model realization!!!**
  - Within pheno models:
    - parameters can act differently...
    - ... and be related!
  - Actual realizations can give surprising cosmology!

**iGracias!**





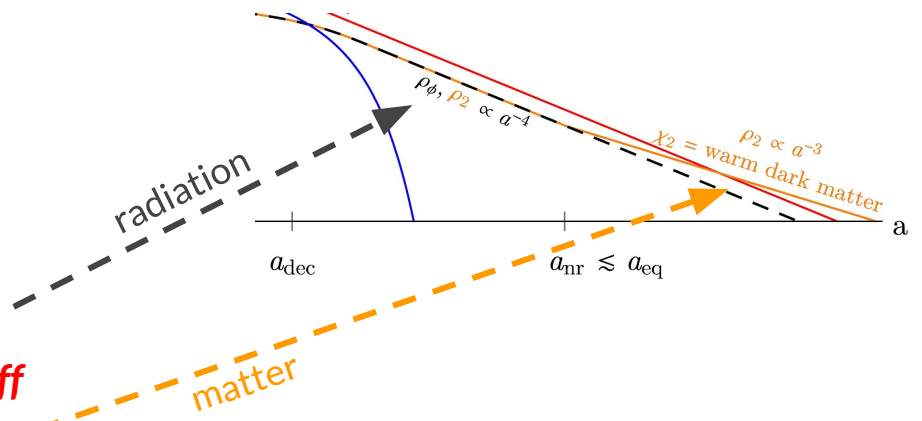
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# Back-up slides

# COWaRD: $a_{nr}$

$$\rho_{2,nr}(a_{nr})^4 \sim \rho_{\varphi,nr}(a_{nr})^4 \propto \Delta N_{eff}$$

$$\rho_{2,nr}(a_{nr})^3 \approx \rho_{2,0} \propto f_{wdm}$$



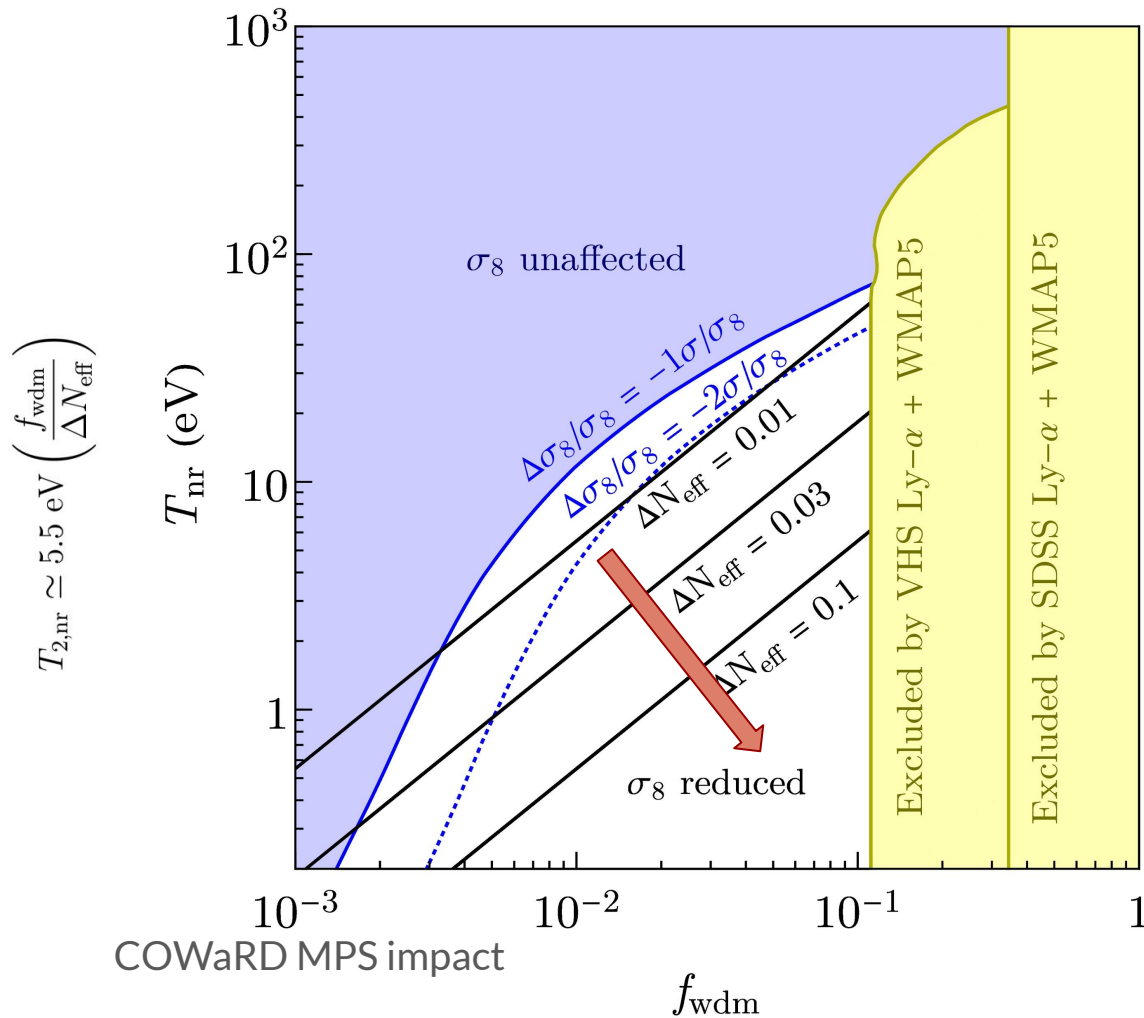
## COWaRD: $\alpha_{nr}$

$$\left. \begin{aligned} \rho_{2,nr}(a_{nr})^4 &\sim \rho_{\varphi,nr}(a_{nr})^4 \propto \Delta N_{\text{eff}} \\ \rho_{2,nr}(a_{nr})^3 &\approx \rho_{2,0} \propto f_{\text{wdm}} \end{aligned} \right\}$$

$$\Rightarrow f_{\text{wdm}} a_{nr} \propto \Delta N_{\text{eff}}$$

$$T_{nr} \propto 1/a_{nr} \Rightarrow$$

$$T_{2,nr} \simeq 5.5 \text{ eV} \left( \frac{f_{\text{wdm}}}{\Delta N_{\text{eff}}} \right)$$



$$\lambda_{\text{FS}} \sim \Delta N_{\text{eff}} / f_{\text{wdm}}$$

$$\sigma_8 \leftrightarrow \Delta N_{\text{eff}}$$

Naive DR: correlated  
**COWaRD: anti-correlated**

# BSM COWaRD examples

$X_1 \rightarrow X_2 + \phi$ : SUSY + axions

- axino  $\rightarrow$  gravitino + axion
- gravitino  $\rightarrow$  axino + axion

$$\Gamma_{\tilde{a} \rightarrow \tilde{G}a} = \frac{m_{\tilde{a}}^5}{96\pi m_{3/2}^2 M_{\text{Pl}}^2} \left(1 - \frac{m_{3/2}}{m_{\tilde{a}}}\right)^2 \left(1 - \left(\frac{m_{3/2}}{m_{\tilde{a}}}\right)^2\right)^3$$

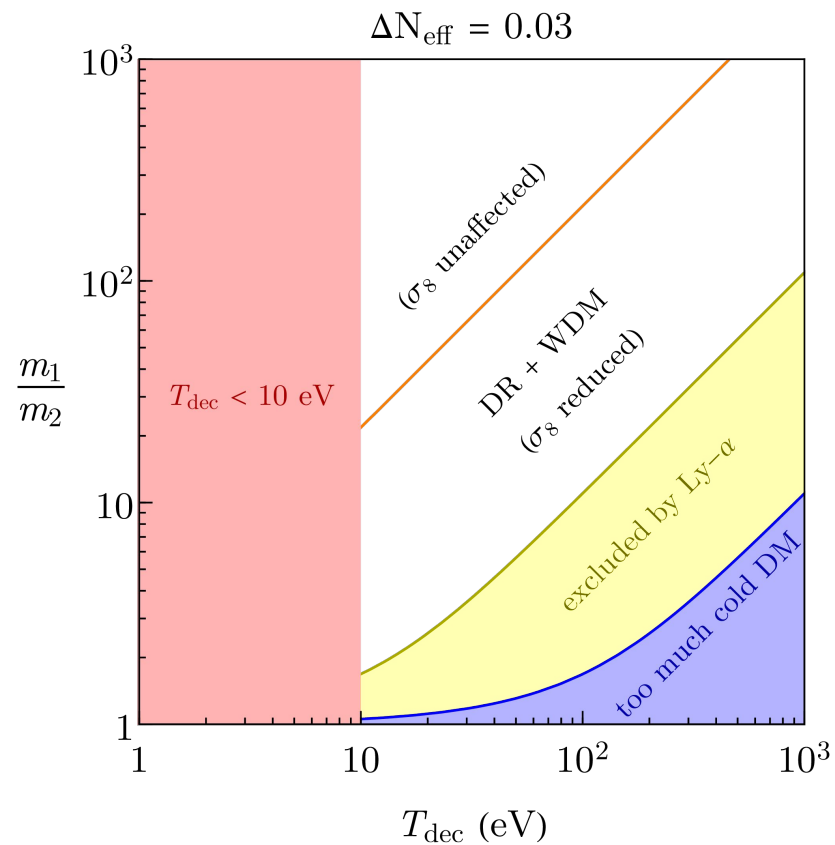
$\{m_1, m_2, N_{1,ini}\}$

particle physics

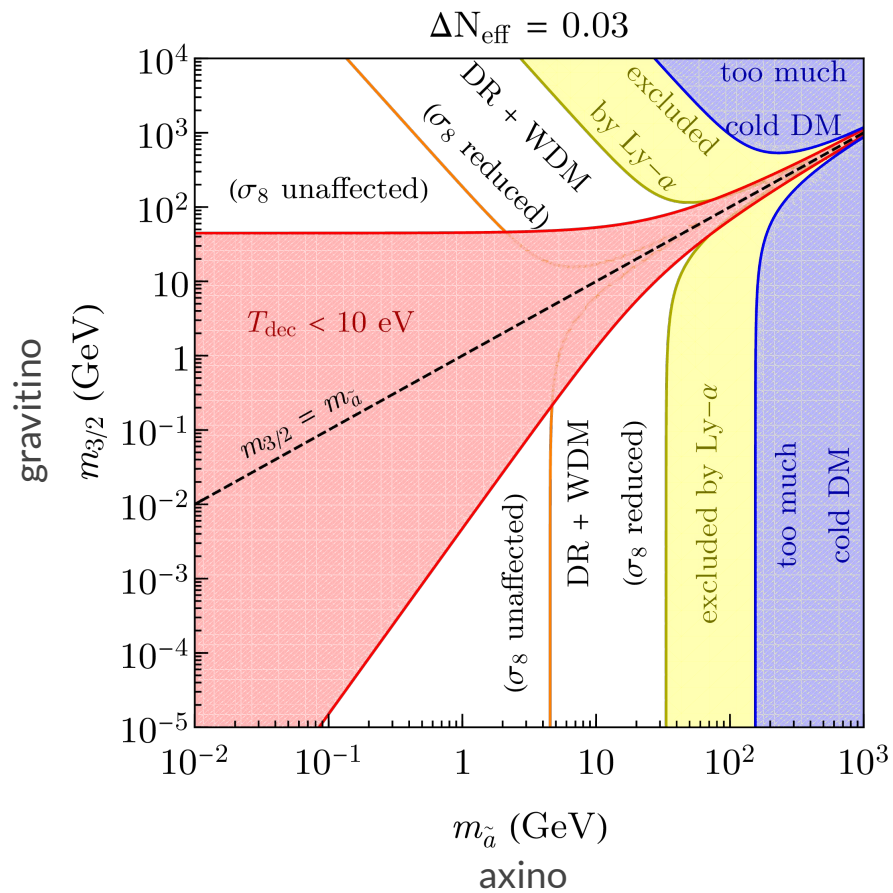


$\{a_{dec}, f_{wdm}, \Delta N_{eff}\}$

cosmology



Other parameters:  $T_{\text{dec}}$  &  $m_1/m_2$



$m_1$  &  $m_2$

Best-fit $\chi^2$					
Data Sets	$\Lambda$ CDM	$\Lambda$ CDM+ $\Delta N_{\text{eff}}$	$\Lambda$ CDM+ $\Delta N_{\text{eff}}$ (= 0.06)	COWaRD	COWaRD ( $\Delta N_{\text{eff}} = 0.03$ )
high- $l$ TTTEE	2347.56	2348.03	2349.39	2345.94	2346.38
low- $l$ EE	396.37	396.72	396.35	395.95	395.96
low- $l$ TT	22.86	22.96	22.27	22.47	22.25
lensing	8.87	8.79	9.06	10.11	10.45
Pantheon	1027.49	1027.08	1027.05	1027.06	1027.02
BAO	5.57	5.35	5.32	5.29	5.24
TOTAL	3808.72	3808.92	3809.44	3806.82	3807.28
$\Delta\chi_{\text{eff}}^2$	—	+0.2	+0.72	-1.9	-1.44

TABLE I. Minimum *effective chi square*  $\chi_{\text{eff}}^2 = -2 \ln \mathcal{L}$  of the  $\Lambda$ CDM and COWaRD models.

Best Fit  $\chi^2$



Parameter values					
Parameter	$\Lambda$ CDM	$\Lambda$ CDM+ $\Delta N_{\text{eff}}$	$\Lambda$ CDM+ $\Delta N_{\text{eff}}$ (= 0.06)	COWaRD	COWaRD ( $\Delta N_{\text{eff}} = 0.03$ )
$100 \omega_b$	$2.245^{+0.014}_{-0.014}$	$2.252^{+0.015}_{-0.015}$	$2.249^{+0.013}_{-0.014}$	$2.254^{+0.015}_{-0.015}$	$2.254^{+0.014}_{-0.015}$
$n_s$	$0.968^{+0.004}_{-0.004}$	$0.971^{+0.004}_{-0.005}$	$0.970^{+0.004}_{-0.004}$	$0.970^{+0.004}_{-0.004}$	$0.970^{+0.004}_{-0.004}$
$\tau_{\text{reio}}$	$0.056^{+0.007}_{-0.008}$	$0.057^{+0.007}_{-0.008}$	$0.057^{+0.007}_{-0.007}$	$0.052^{+0.008}_{-0.008}$	$0.052^{+0.008}_{-0.009}$
$100 \theta_s$	$1.0420^{+0.00029}_{-0.00029}$	$1.0417^{+0.00037}_{-0.00033}$	$1.0418^{+0.00028}_{-0.00029}$	$1.0419^{+0.00032}_{-0.00031}$	$1.0419^{+0.00030}_{-0.00030}$
$\ln 10^{10} A_s$	$3.048^{+0.014}_{-0.015}$	$3.053^{+0.014}_{-0.016}$	$3.051^{+0.015}_{-0.014}$	$3.037^{+0.016}_{-0.017}$	$3.037^{+0.017}_{-0.018}$
$\omega_{\text{cdm}}$	$0.1192^{+0.0009}_{-0.0009}$	$0.1210^{+0.0012}_{-0.0020}$	$0.1202^{+0.0009}_{-0.0010}$	$0.1029^{+0.0096}_{-0.0097}$	$0.1038^{+0.0056}_{-0.0087}$
$\Delta N_{\text{eff}}$	—	$0.110^{+0.028}_{-0.110}$	0.06	$0.031^{+0.007}_{-0.031}$	0.03
$f_{\text{wdm}}$	—	—	—	$0.138^{+0.074}_{-0.082}$	$0.130^{+0.067}_{-0.044}$
$H_0$	$67.77^{+0.43}_{-0.43}$	$68.43^{+0.55}_{-0.77}$	$68.13^{+0.42}_{-0.41}$	$68.19^{+0.47}_{-0.53}$	$68.21^{+0.46}_{-0.48}$
$\sigma_8$	$0.801^{+0.006}_{-0.006}$	$0.816^{+0.007}_{-0.008}$	$0.813^{+0.006}_{-0.006}$	$0.773^{+0.038}_{-0.014}$	$0.770^{+0.006}_{-0.010}$
$\Omega_m$	$0.310^{+0.006}_{-0.006}$	$0.308^{+0.006}_{-0.006}$	$0.309^{+0.005}_{-0.006}$	$0.307^{+0.006}_{-0.007}$	$0.306^{+0.006}_{-0.006}$

TABLE II. Mean values and 68% C.L. intervals of the parameters of the  $\Lambda$ CDM and COWaRD models.

Parameter values

# Contour Plots

