

# Redshift Space Distortions from the extended Baryon Oscillation Spectroscopic Survey

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# Galaxy Surveys 101

eBOSS contains 4 tracers

Catalogue	Range	Objects
LRG	0.6 < z < 1.0	250k
ELG	0.6 < z < 1.1	190k
Quasars	0.8 < z < 2.2	350k
Ly- $\alpha$	0.9 < z < 3.5	350k



$\delta(x)$  **stochastic field**

$$\delta(x) \equiv \frac{\rho(x)}{\bar{\rho}} - 1 \quad \delta(k) = \int dx \delta(x) e^{-ikx}$$

**Cosmology information**  
**2-point function statistics**

$$\langle \delta(x) \delta(x + R) \rangle = \xi(R) \quad \text{Config. Space}$$

$$\langle \delta(k) \delta(k') \rangle = P(k) \delta^D(k + k') \quad \text{Fourier Space}$$

\*see J. Bautista & E. Müller talk for more eBOSS tracers

# Main Goal of redshift surveys: BAO & RSD

**Growth of structure:** Ratio monopole to quadrupole  $\propto f\sigma_8$

**BAO peak position:** Isotropic signal  $\propto [D_M^2(z)/H(z)]^{1/3}/r_{\text{drag}}$

**BAO relative peak position:** isotropic vs. anisotropic  $\propto D_M(z)H(z)$

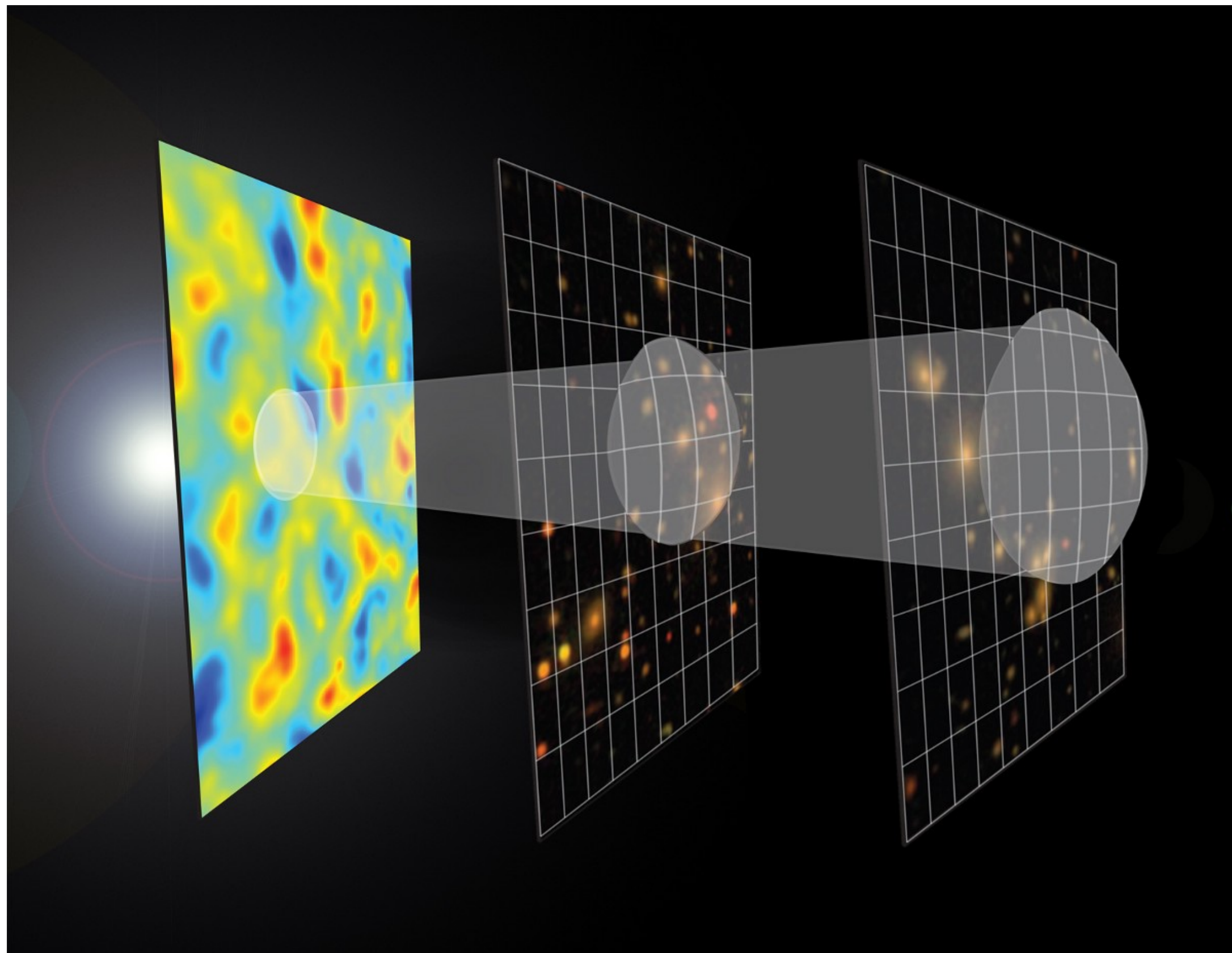


$$D_H(z, \Omega) = \frac{c}{H(z, \Omega)}$$

$$D_M(z, \Omega) = \int_0^z \frac{cdz'}{H(z', \Omega)}$$

$$f(z, \Omega) = \frac{d \log D_{\text{lin}}(z, \Omega)}{d \log a(z)} = \Omega_m(z, \Omega)^\gamma$$

# BAO as a standard ruler

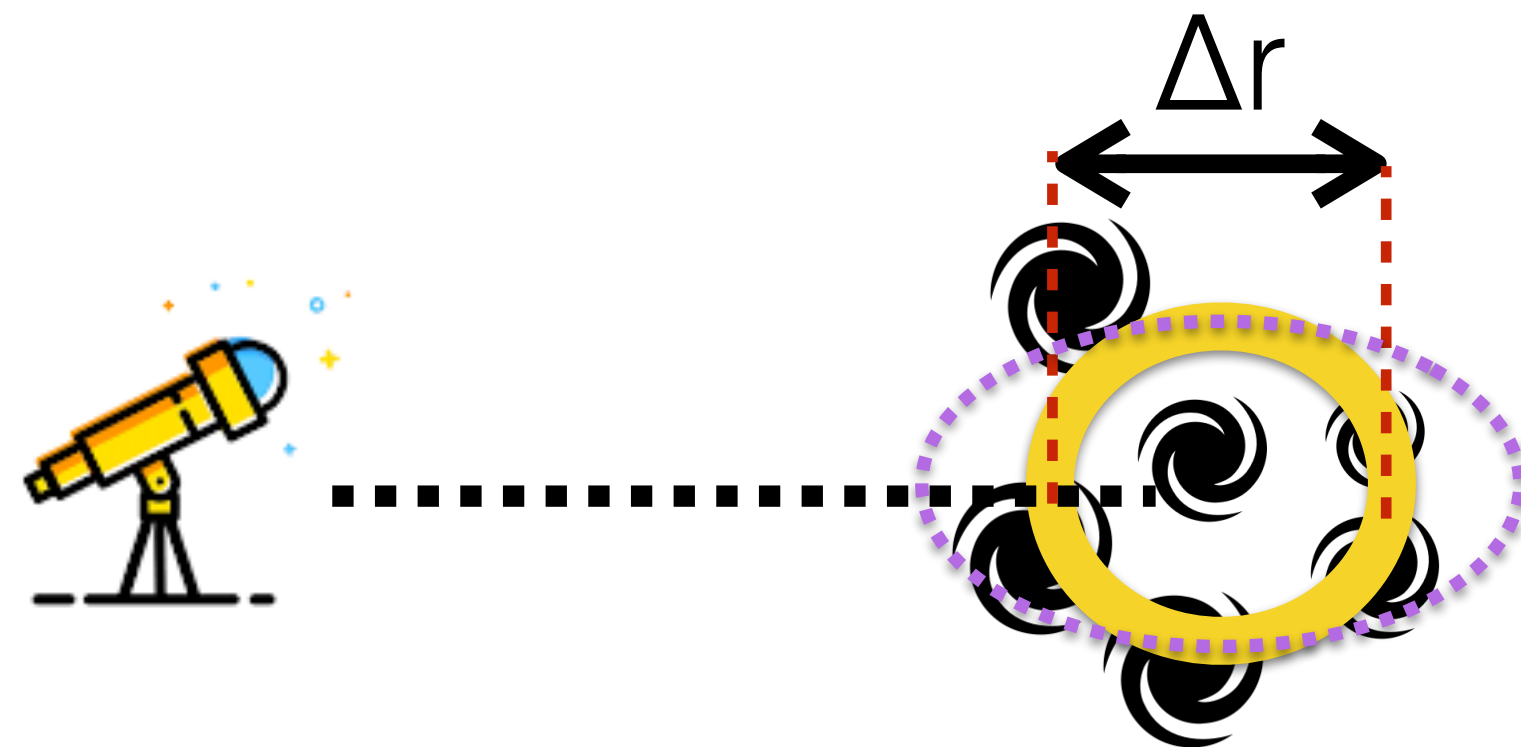
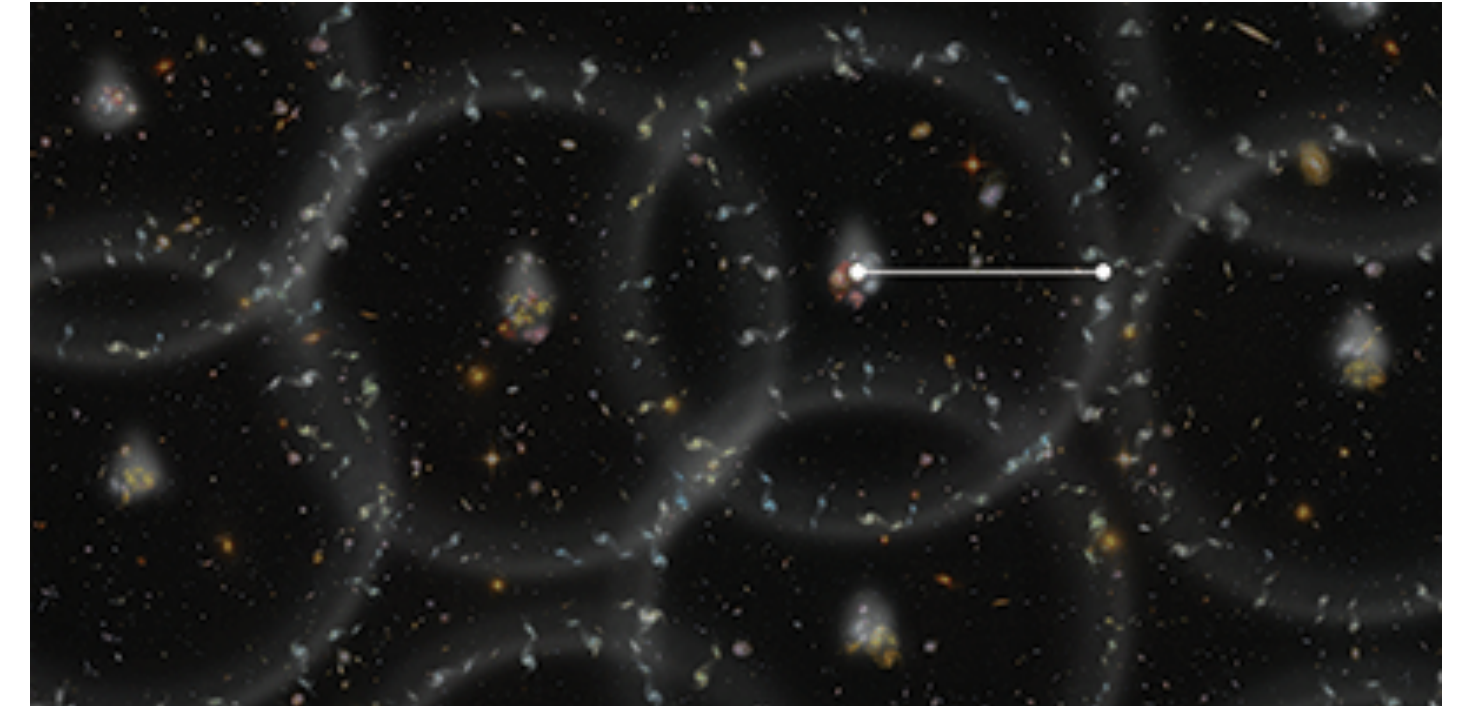


- Cleanest probe to measure expansion in the LSS
- Provide expansion along and across the line-of-sight
  - ↳ requires knowledge of the horizon scale at recombination times:  $r_{\text{drag}}$
- Systematic floor beyond BOSS/eBOSS statistical precision

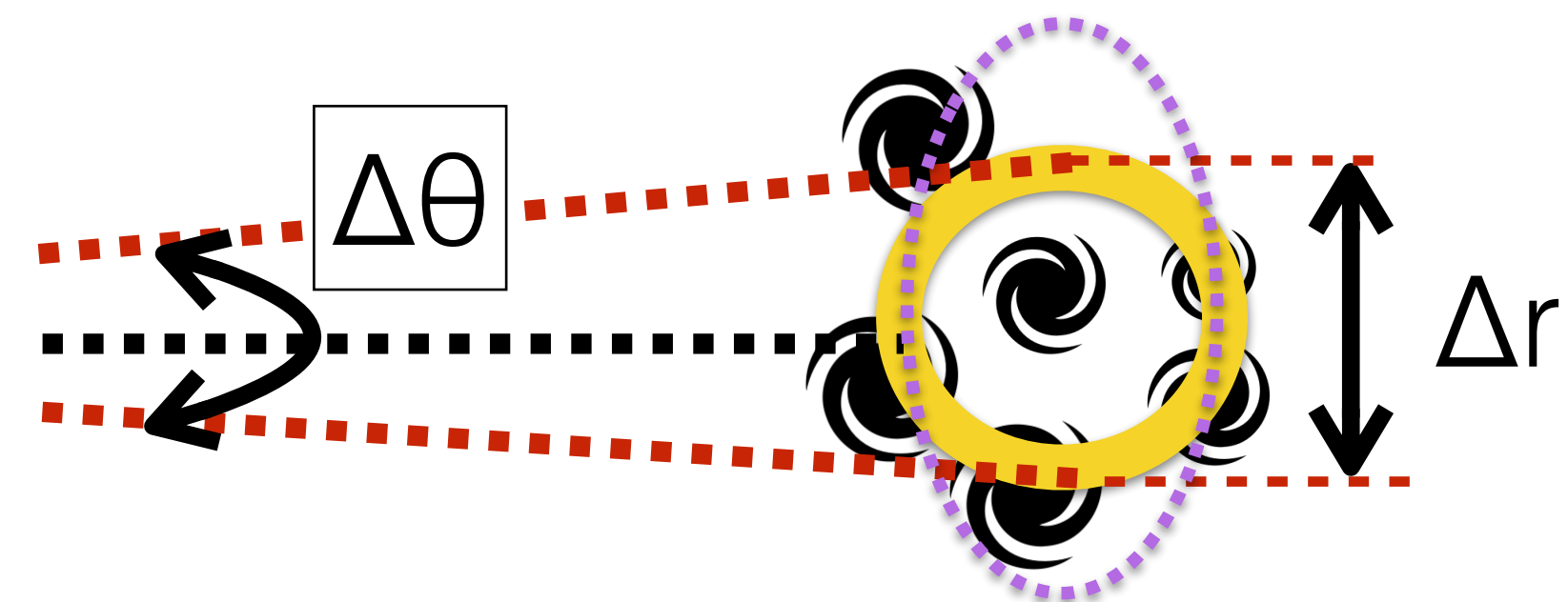
# Alcock-Paczynski

- Universe assumed **isotropic** and **homogeneous**
- **AP effect**: Anisotropy induced by transforming redshifts into comoving distances assuming an arbitrary cosmology

\* aka reference cosmology



Radial distance



Angular diameter distance

$$\Delta r_{\parallel}(z_1, z_2; \Omega_m) = \int_{z_1}^{z_2} \frac{cdz'}{H_0 \sqrt{\Omega_m (1+z')^3 + 1 - \Omega_m}} \approx \frac{c\Delta z}{H(\bar{z}, \Omega_m)} \sim \frac{c}{H(z)} \equiv D_H(z)$$

$$\Delta r_{\perp}(\theta_1, \theta_2; z, \Omega_m) = \Delta\theta \int_0^z \frac{cdz'}{H(z', \Omega_m)} \sim D_M(z)$$

BAO provides a reference-structure for the AP effect

# Alcock-Paczynski

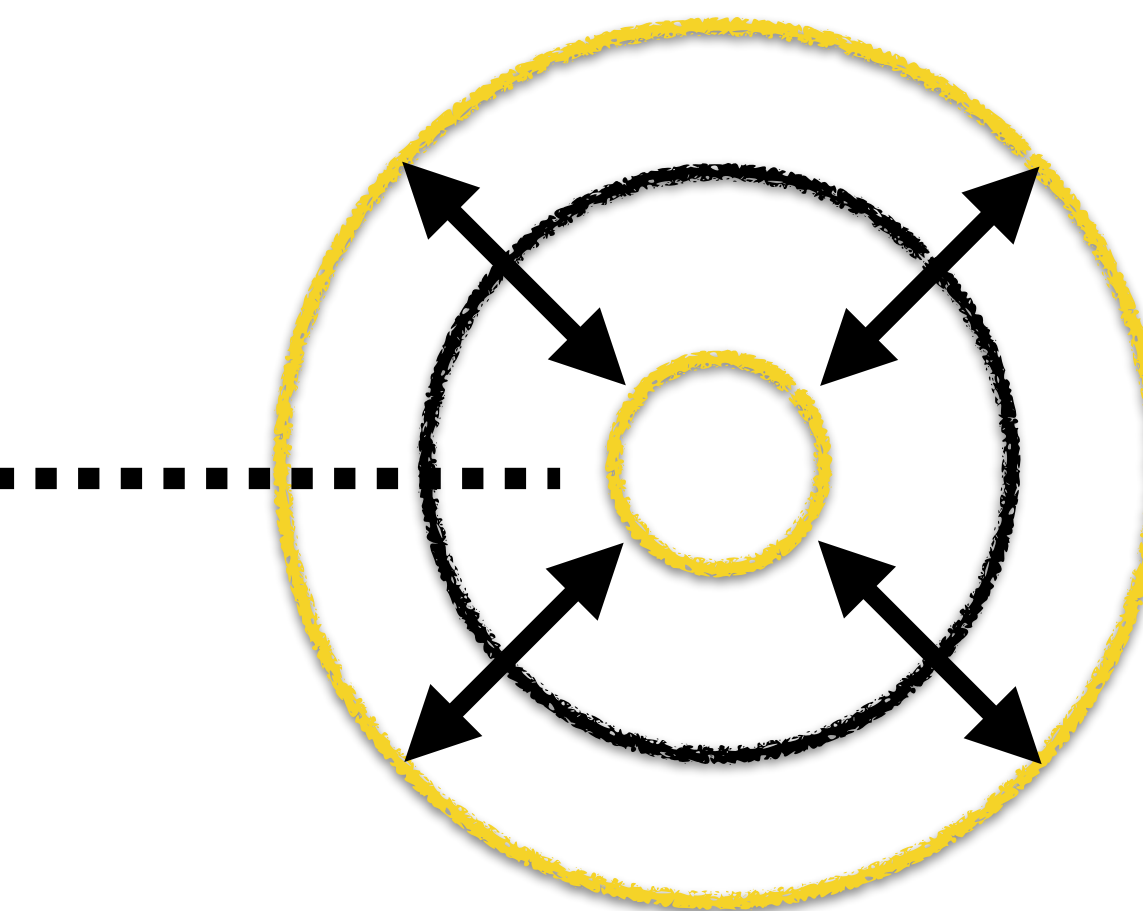
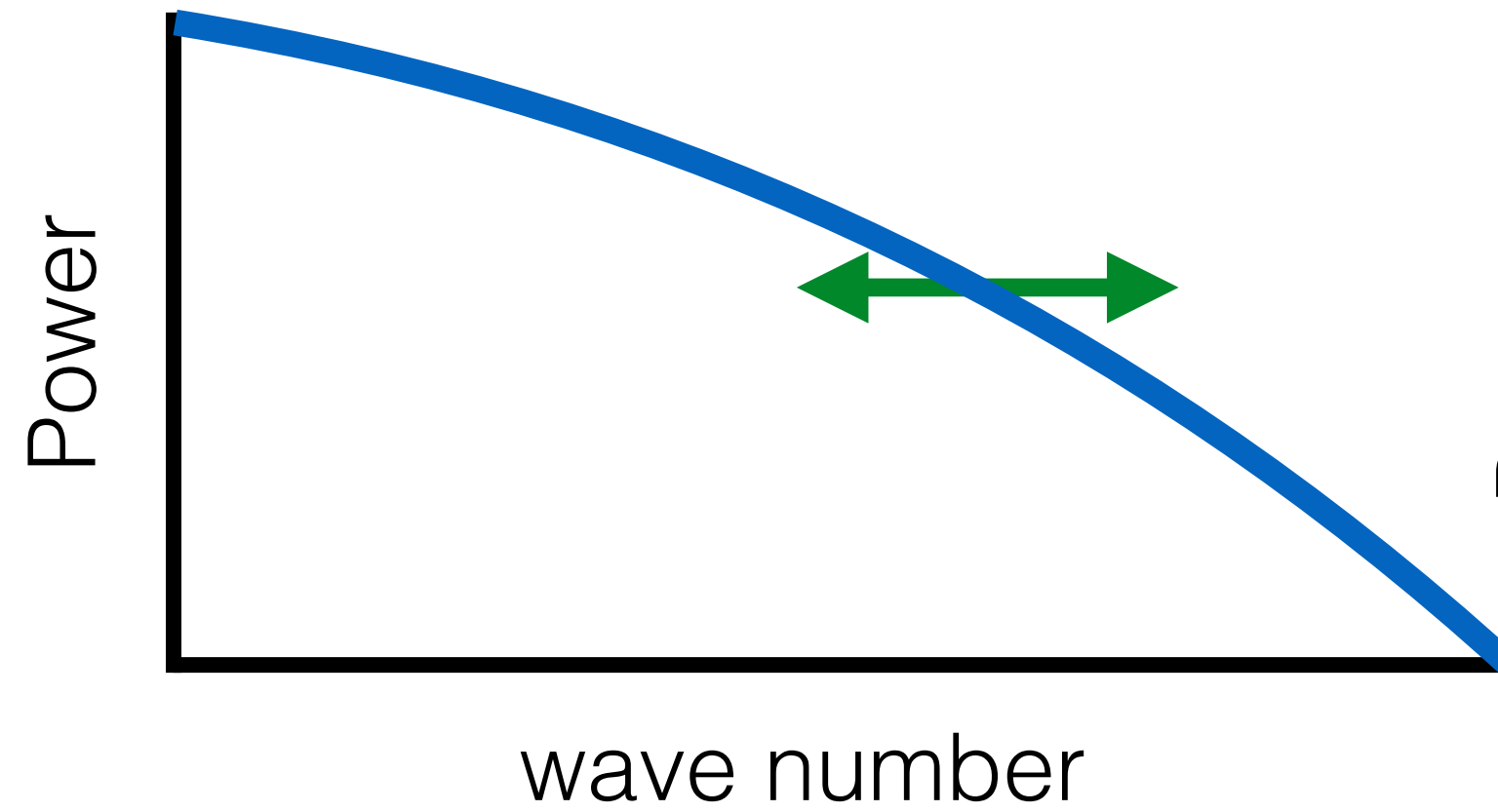
$$k_{\parallel} = q_{\parallel} k'_{\parallel} \longrightarrow q_{\parallel}(z) = \frac{D_H(z)}{D_H^{\text{fid}}(z)}$$

$$k_{\perp} = q_{\perp} k'_{\perp} \longrightarrow q_{\perp}(z) = \frac{D_M(z)}{D_M^{\text{fid}}(z)}$$

Observed wave-vector  
True wave-vector

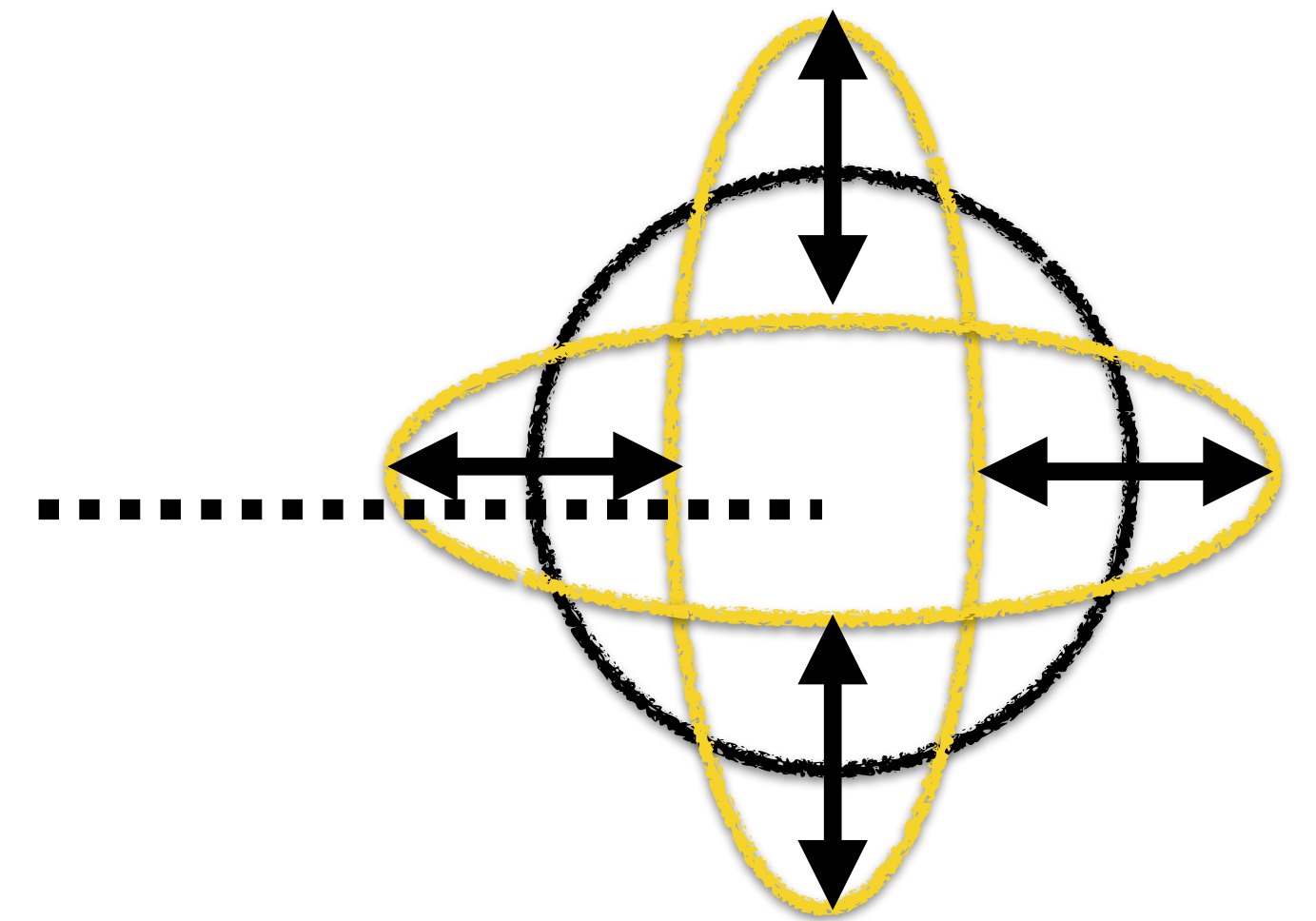
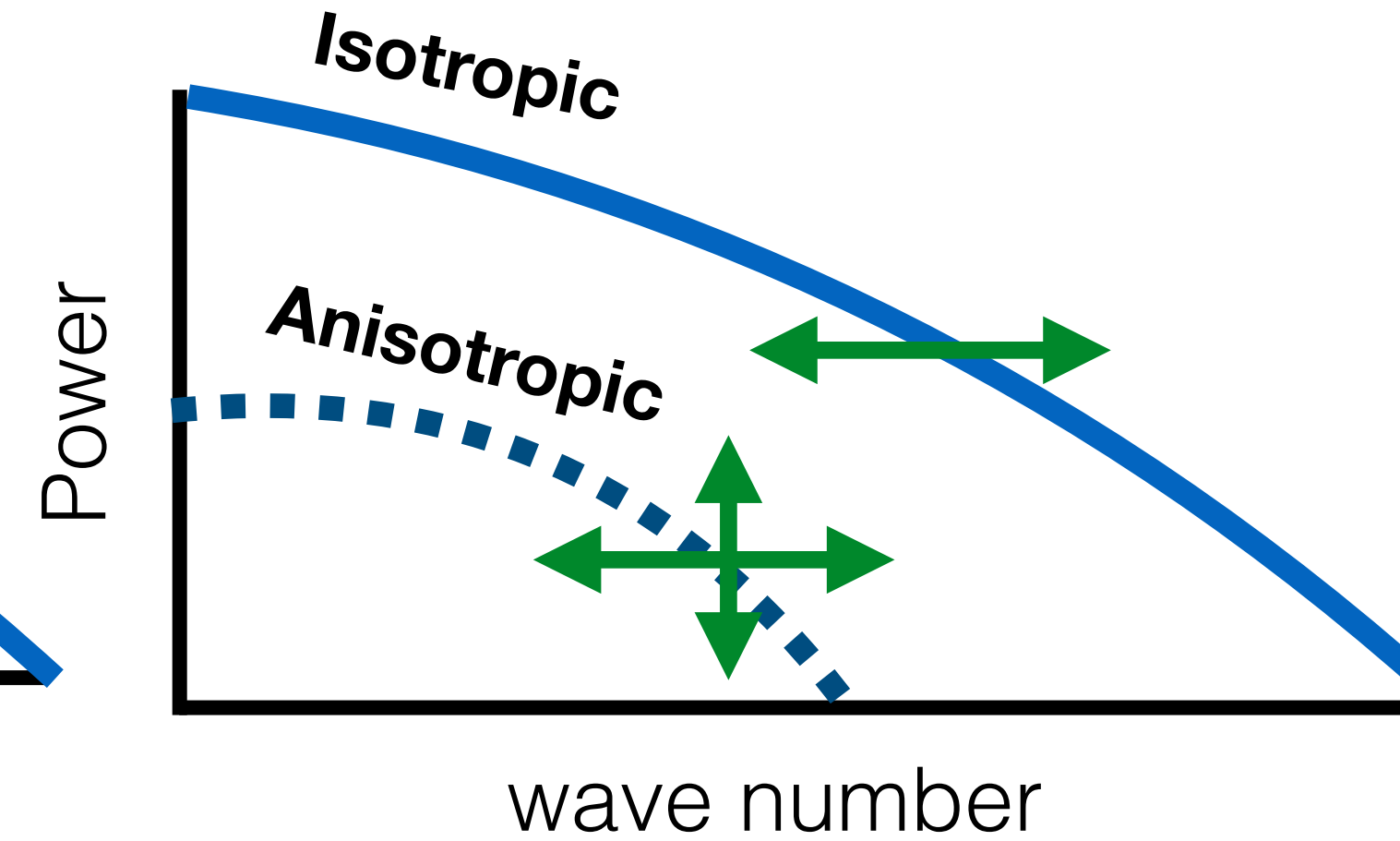


BAO Isotropic shift



$$\propto [D_M^2(z) D_H(z)]^{1/3} \equiv D_V(z)$$

BAO Warping (AP-effect)



$$\propto D_M(z) / D_H(z) \quad 5$$

# Horizon Scale $r_{\text{drag}}$

LSS is not sensitive to the horizon scale at CMB times.

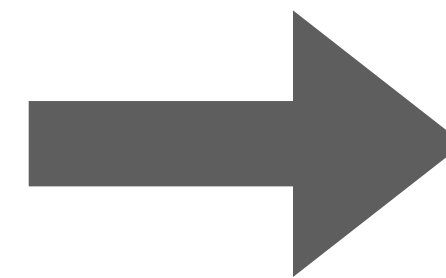
Need to assume one fixed template (or a functional form)

\* aka **template cosmology**

**AP effect +  $r_{\text{drag}}$  unknown value**

$$\alpha_{\parallel}(z) = q_{\parallel}(z) \frac{r_{\text{drag}}^{\text{fid}}}{r_{\text{drag}}} = \frac{D_H(z)/r_{\text{drag}}}{D_H^{\text{fid}}(z)/r_{\text{drag}}^{\text{fid}}} \longrightarrow k_{\parallel} = \alpha_{\parallel}(z)k'_{\parallel}$$

$$\alpha_{\perp}(z) = q_{\perp}(z) \frac{r_{\text{drag}}^{\text{fid}}}{r_{\text{drag}}} = \frac{D_M(z)/r_{\text{drag}}}{D_M^{\text{fid}}(z)/r_{\text{drag}}^{\text{fid}}} \longrightarrow k_{\perp} = \alpha_{\perp}(z)k'_{\perp}$$



This adds an extra factor to the isotropic BAO-shift, but not on the relative trans-to-long BAO

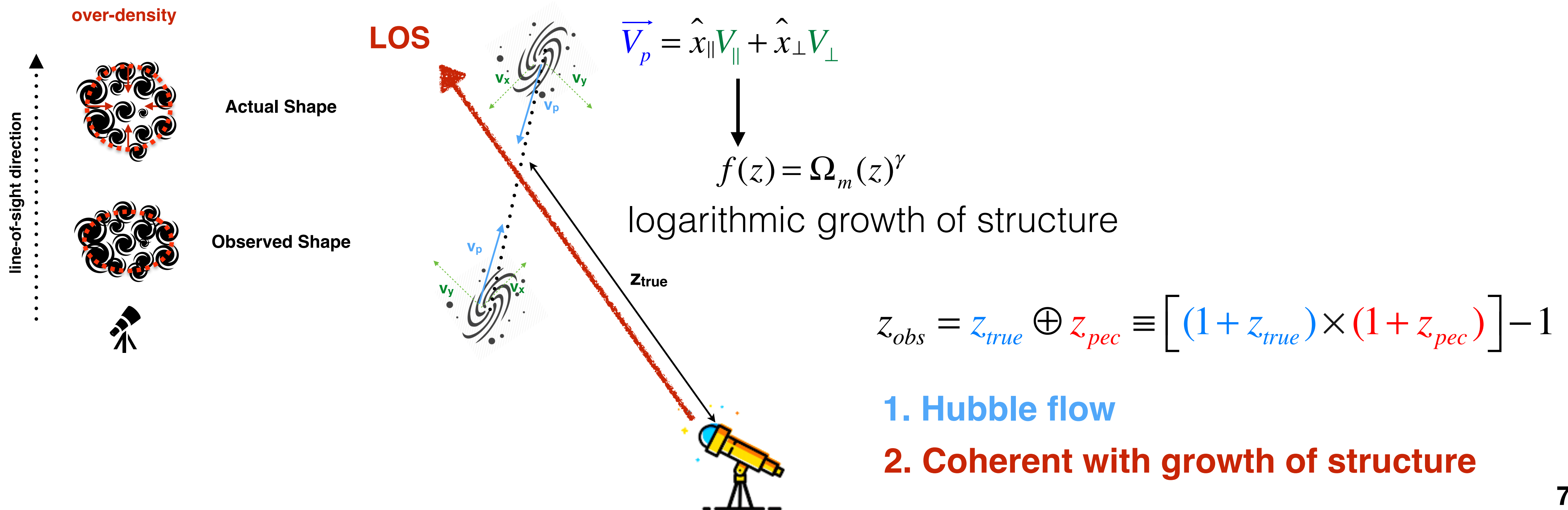
$$\propto [D_M^2(z)D_H(z)]^{1/3}/r_{\text{drag}}$$

$$\propto D_M(z)/D_H(z)$$

For simplicity **template** & **reference cosmology** set to be the same (fid cosmology)

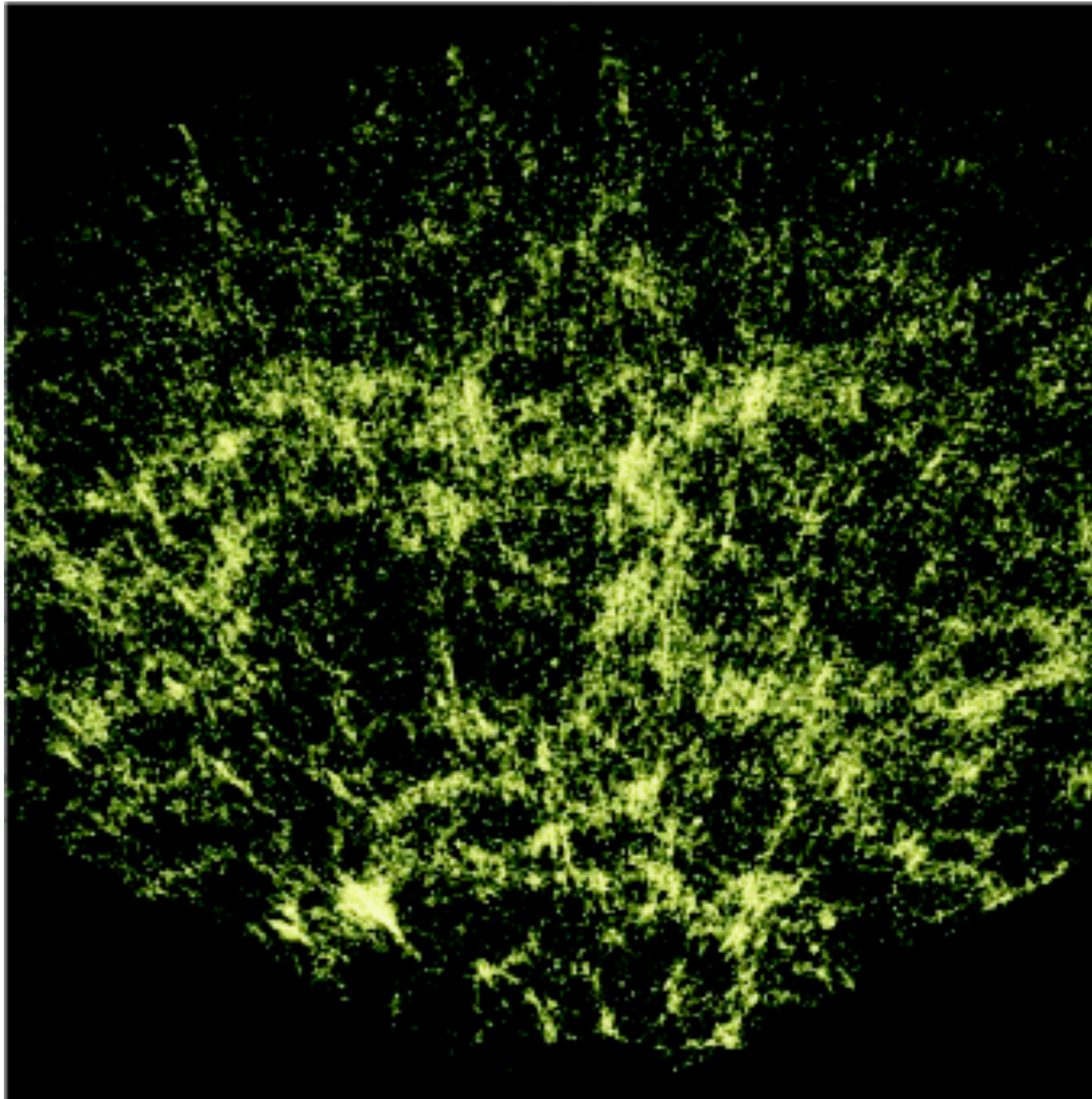
# Redshift Space Distortions

- Universe assumed **isotropic** and **homogeneous**
- **RSD**: Enhancement / reduction of the clustering along the line-of-sight (LOS) direction due to peculiar velocities (Kaiser 1987)

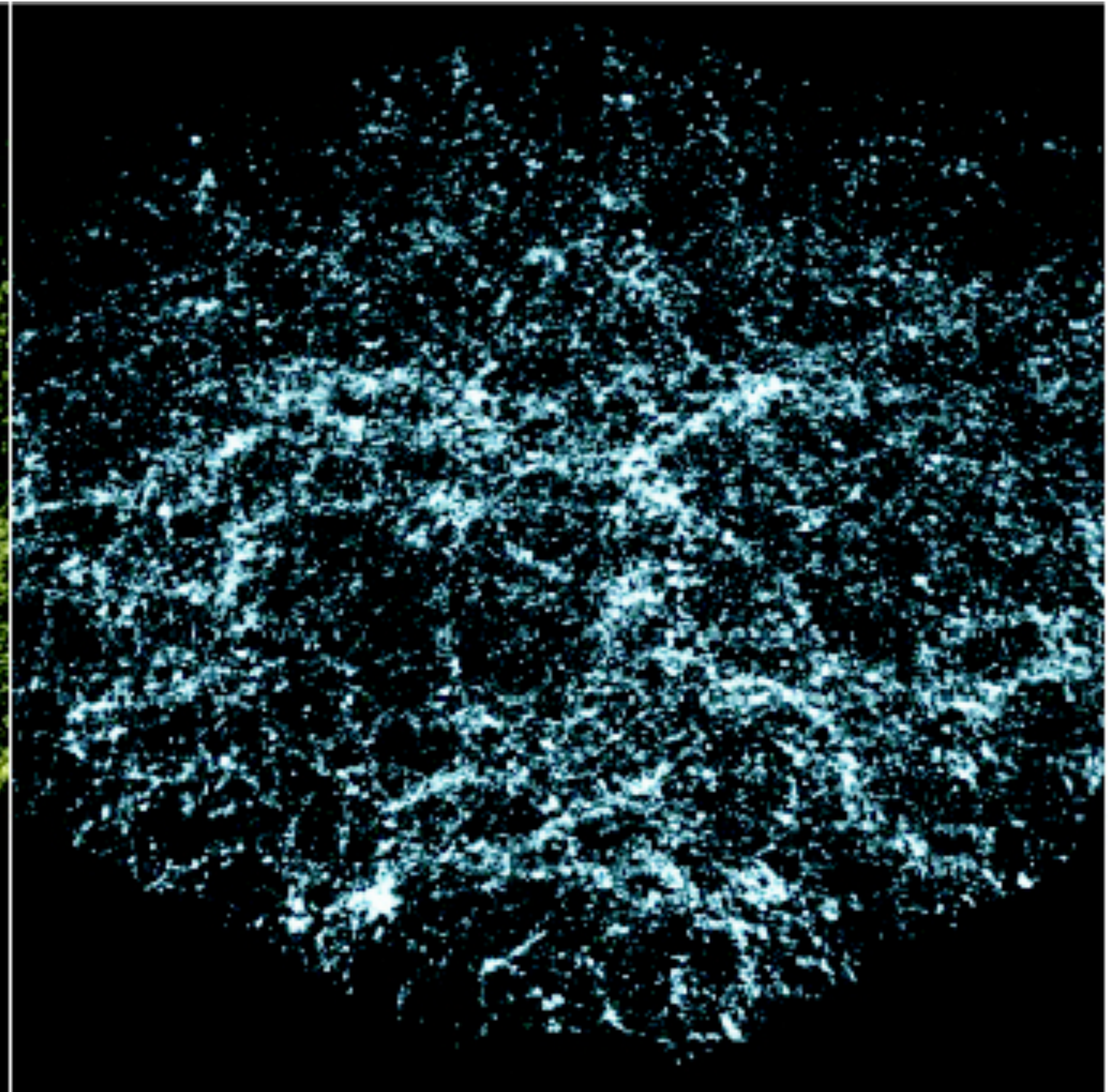




## Observed 'redshift' space



## True 'real' space



# Redshift Space Distortions

$$P_g^{(s)}(k, \mu) = [b + f\mu^2]^2 P_m(k) \longrightarrow \text{Kaiser linear term}$$

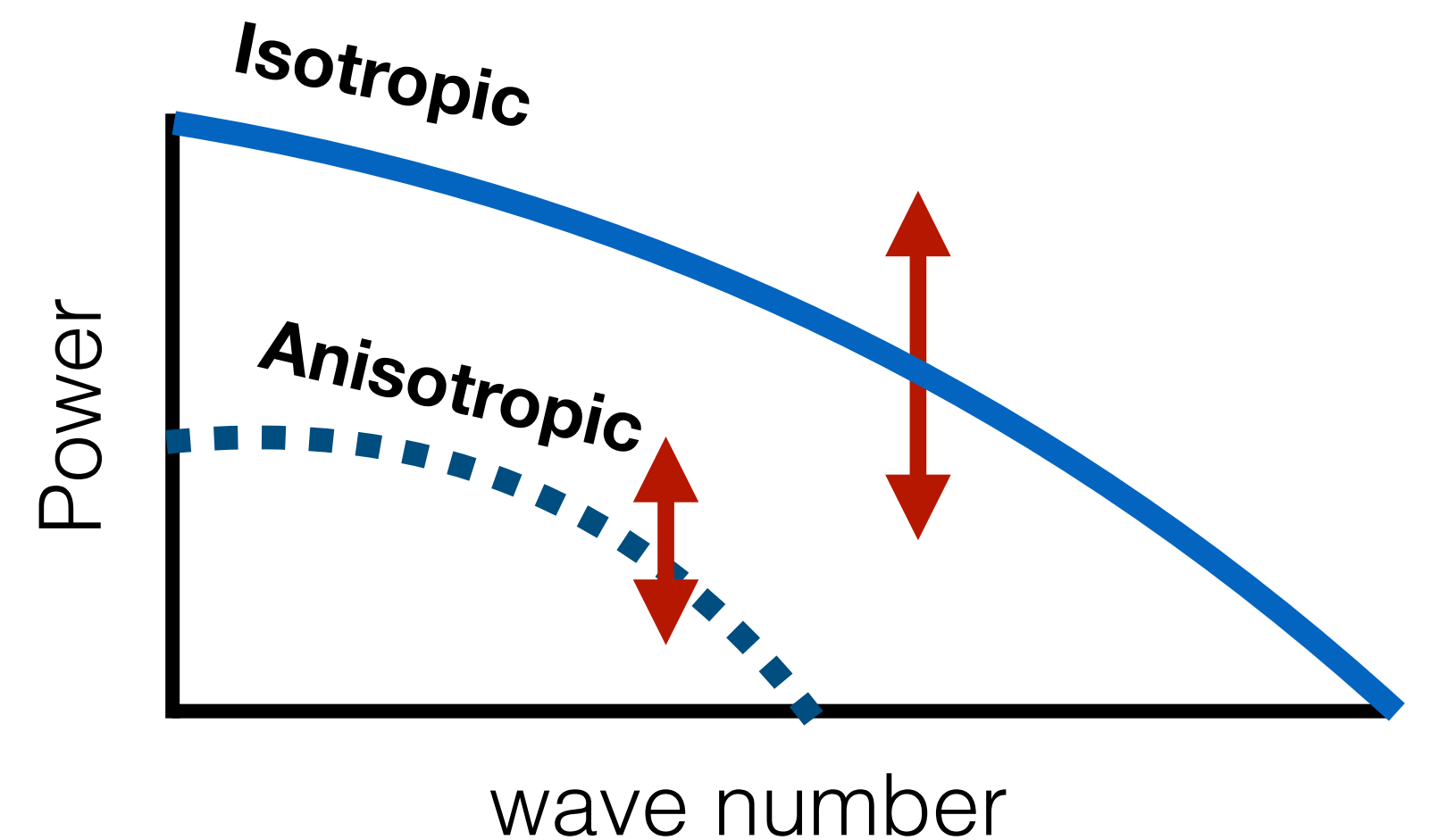
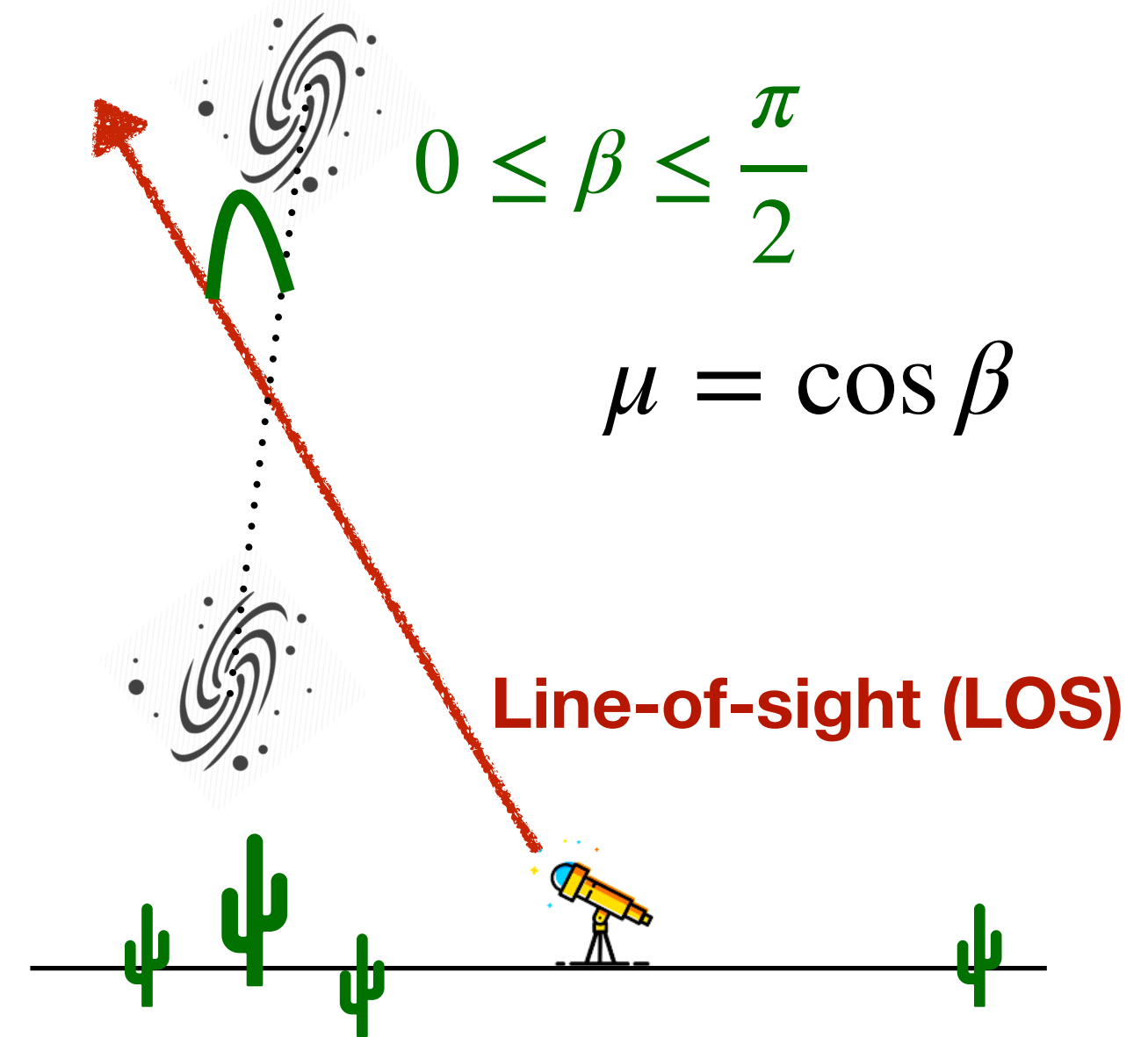
$$P^{(s)}(k, \mu) = \underbrace{P^{(0)}(k)L_0(\mu)}_{\text{monopole}} + \underbrace{P^{(2)}(k)L_2(\mu) + P^{(4)}(k)L_4(\mu)}_{\text{quadrupole hexadecapole}}$$

Isotropic signal
Anisotropic signal

$$P^{(0)}(k) = \left(b^2 + \frac{2}{3}bf + \frac{1}{5}f^2\right)P_m(k)$$

$$P^{(2)}(k) = \left(\frac{4}{3}bf + \frac{4}{7}f^2\right)P_m(k)$$

$$P^{(4)}(k) = \left(\frac{8}{35}f^2\right)P_m(k)$$



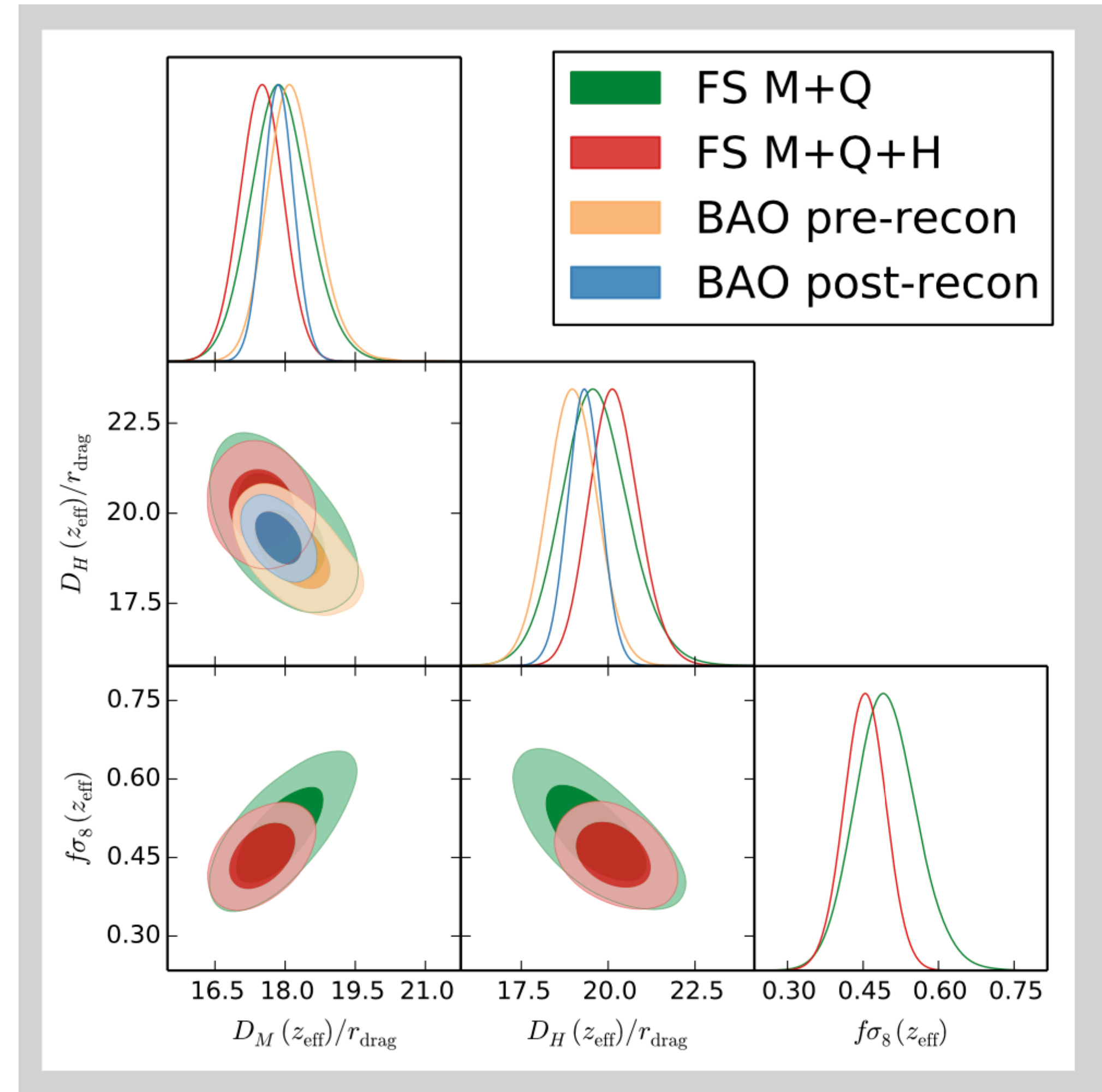
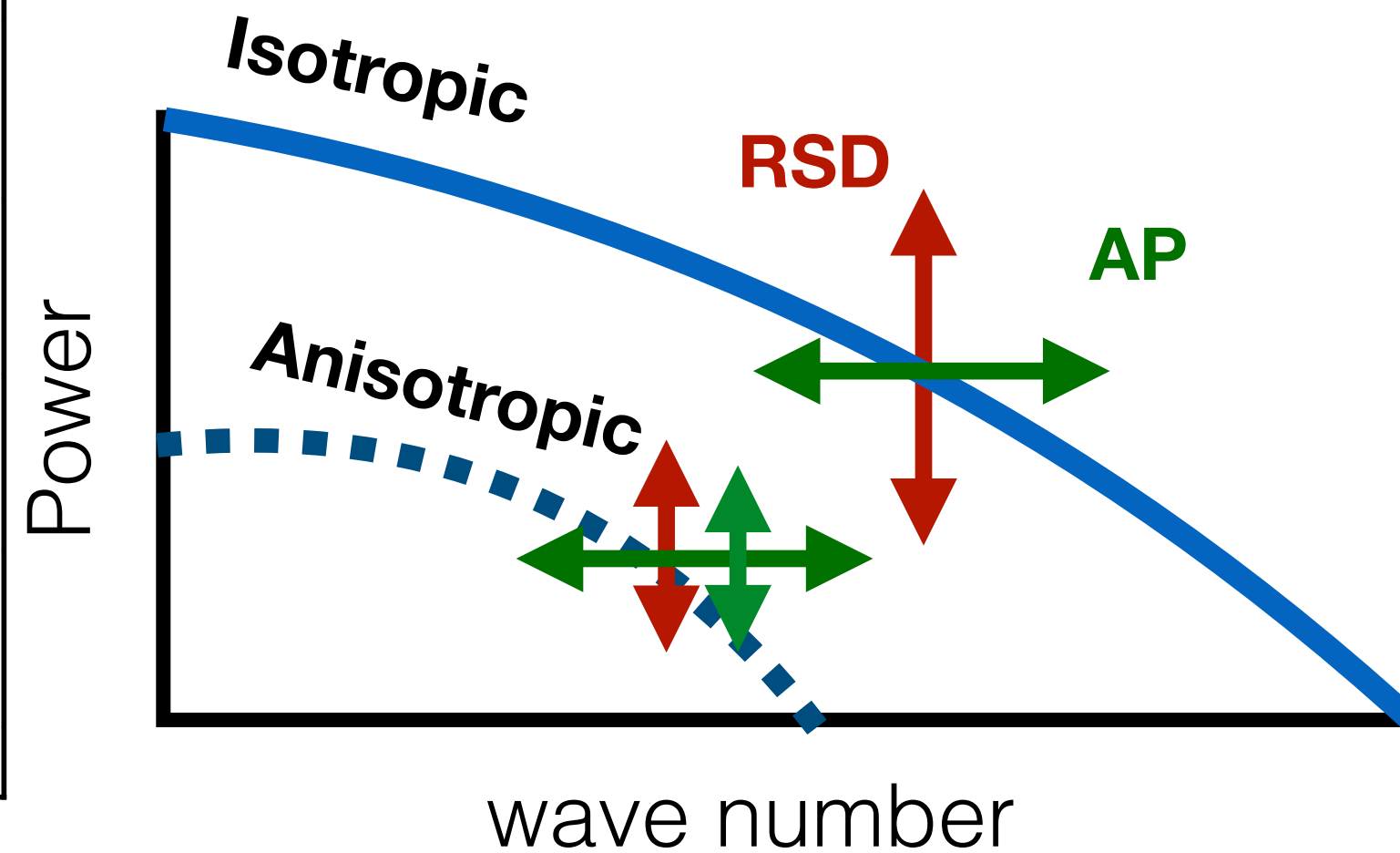
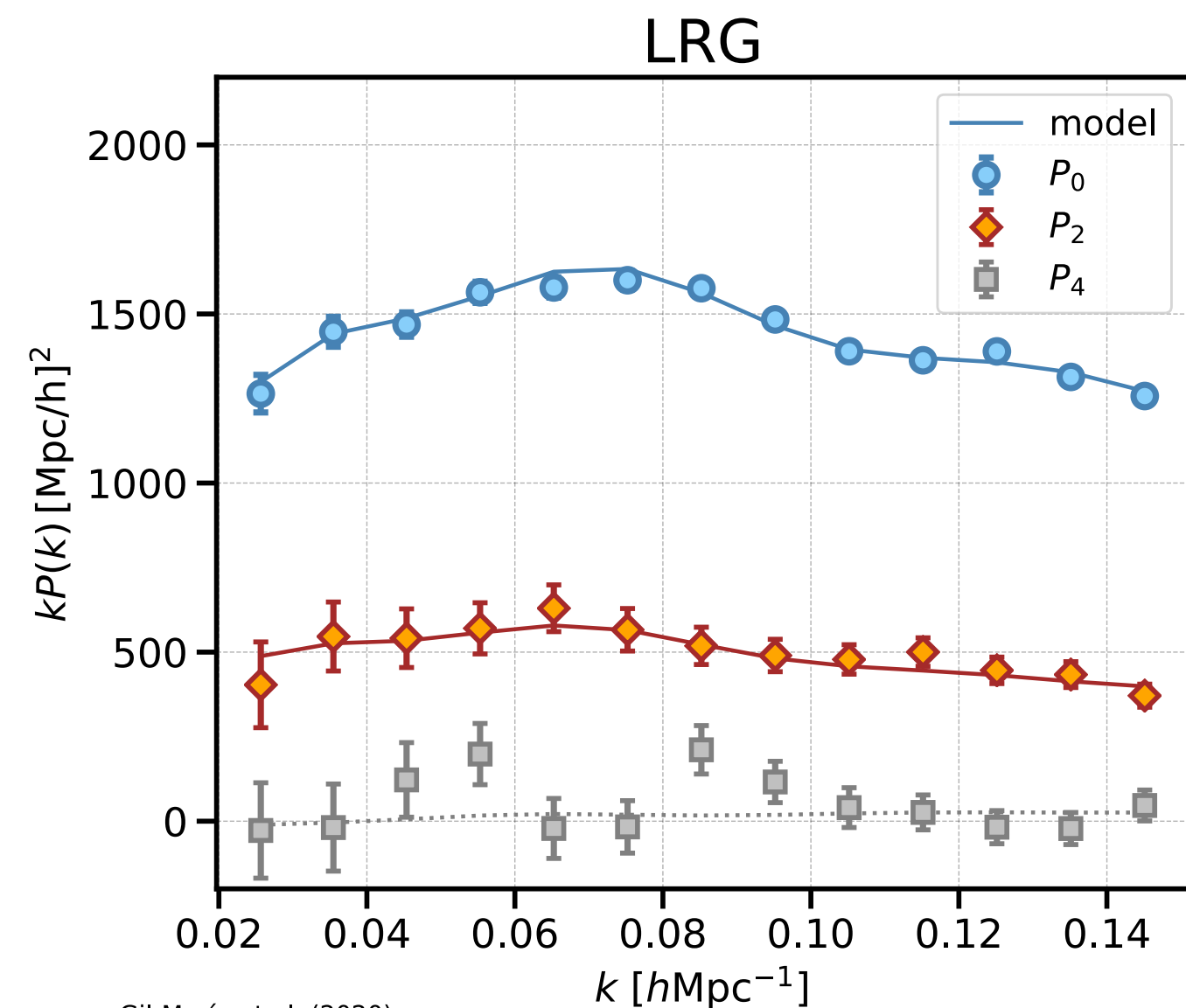
# Full Shape analysis

Simultaneous fit of,

$$f\sigma_8, \quad \alpha_{\parallel} (D_H/r_{\text{drag}}), \quad \alpha_{\perp} (D_M/r_{\text{drag}})$$

+ nuisance parameters (galaxy bias etc...)

For the LRG sample



Gil-Marín et al. (2020)  
(plot by Jiamin Hou, MPE)

# Logarithmic growth factor interpretation

## Interpretation of the best-fitting value

1. Find  $f_{\text{best-fit}}$  for a given (arbitrary) template,  $P_m(k)$
2.  $f_{\text{best-fit}}$  signal degenerated with  $P_m(k)$  amplitude of the template used,  $\sigma_8^{\text{temp}}$ :  $[f\sigma_8]^{\text{true}} = f_{\text{best-fit}}\sigma_8^{\text{temp}}$

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3.  $\sigma_8$  is the smoothed matter power spectrum in spheres of 8 Mpc/h. The size of these spheres is in [Mpc/h] units depends on the reference cosmology

Isotropic scale dilation  $q_0 = q_{\parallel}^{1/3} q_{\perp}^{2/3}$

**Affects the units of the smoothing spheres!**

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4. Invariant  $\sigma_8$  definition as a function of the best-fitting  $q_0$

$$\sigma_{8\text{resc}}^2(q_0) = \frac{1}{q_0^3} \int_0^{\infty} dk k^2 P_{\text{lin}}(k/q_0) W_{\text{TH}}^2([8\text{Mpc}/h]k)$$

5. We need a prior on  $r_s$  to infer  $q_0$  from  $a_0$ :  
We approximate  $r_{\text{drag}}$  as  $r_{\text{drag}}^{\text{temp}}$

$$\alpha_0 \simeq q_0$$

$$[f\sigma_8]^{\text{true}} = f_{\text{best-fit}}\sigma_{8\text{resc}}^{\text{temp}}(\alpha_0)$$

This correction only important for reference cosmology very different from true cosmo,

$$\alpha_0 \neq 1$$

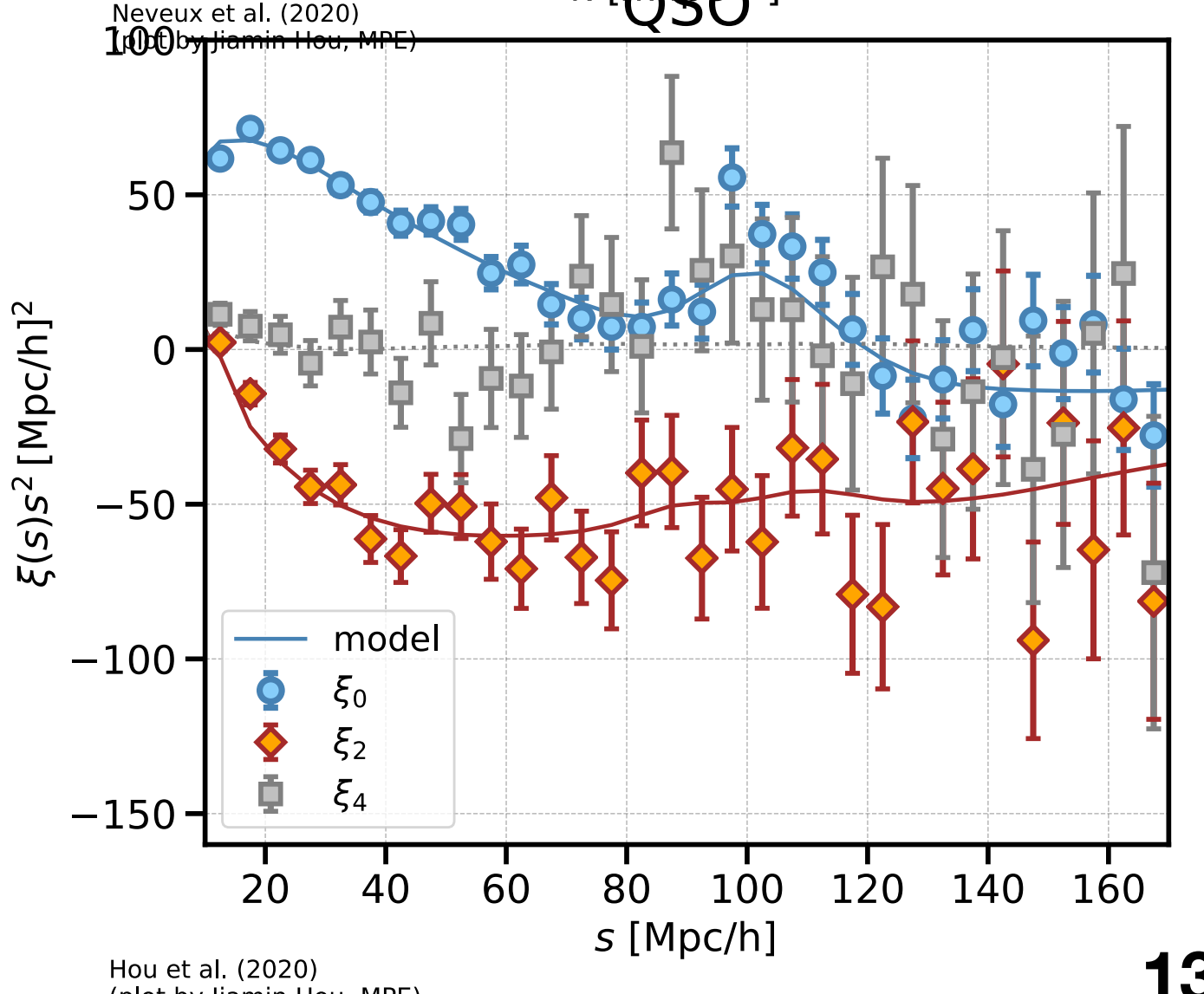
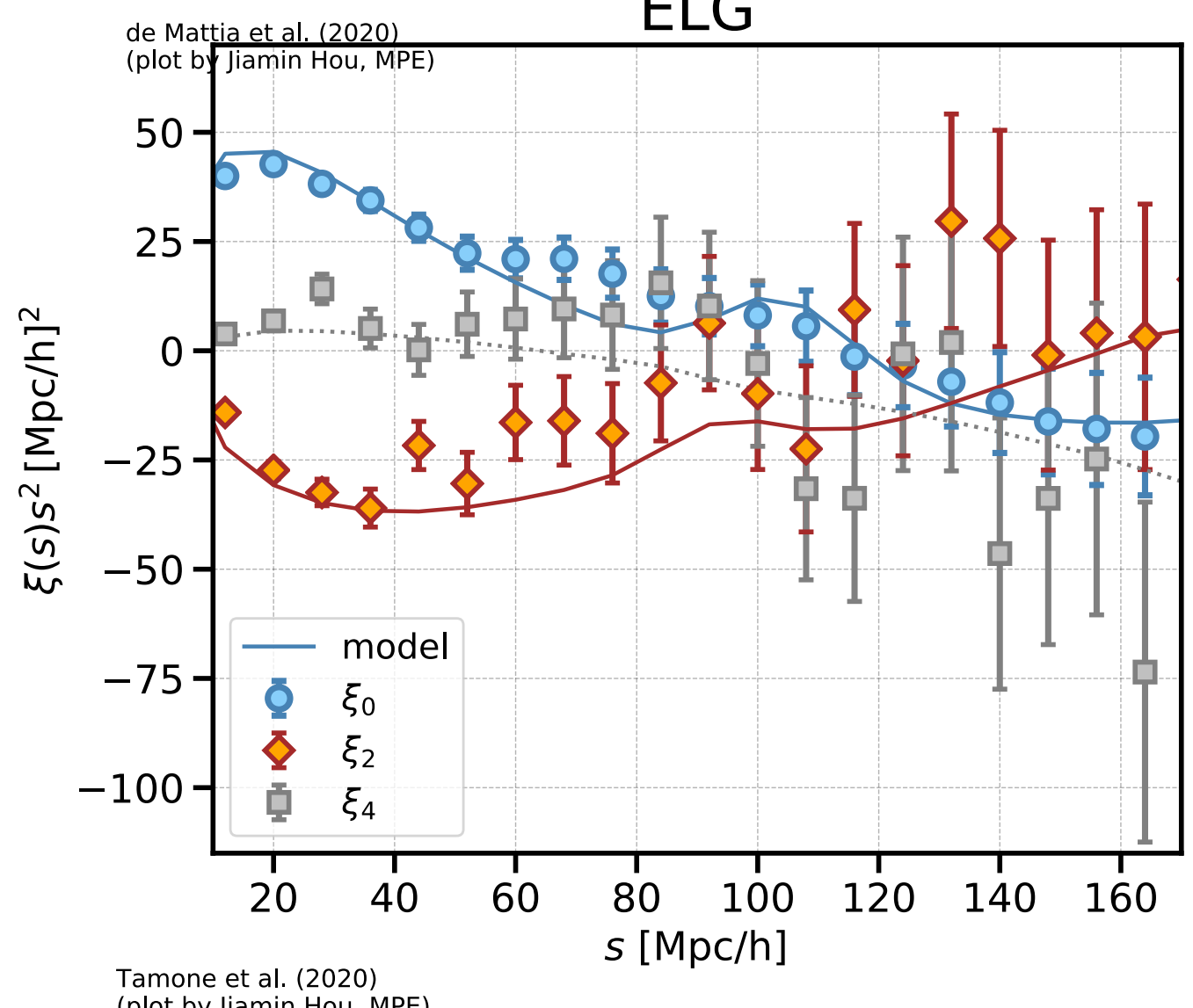
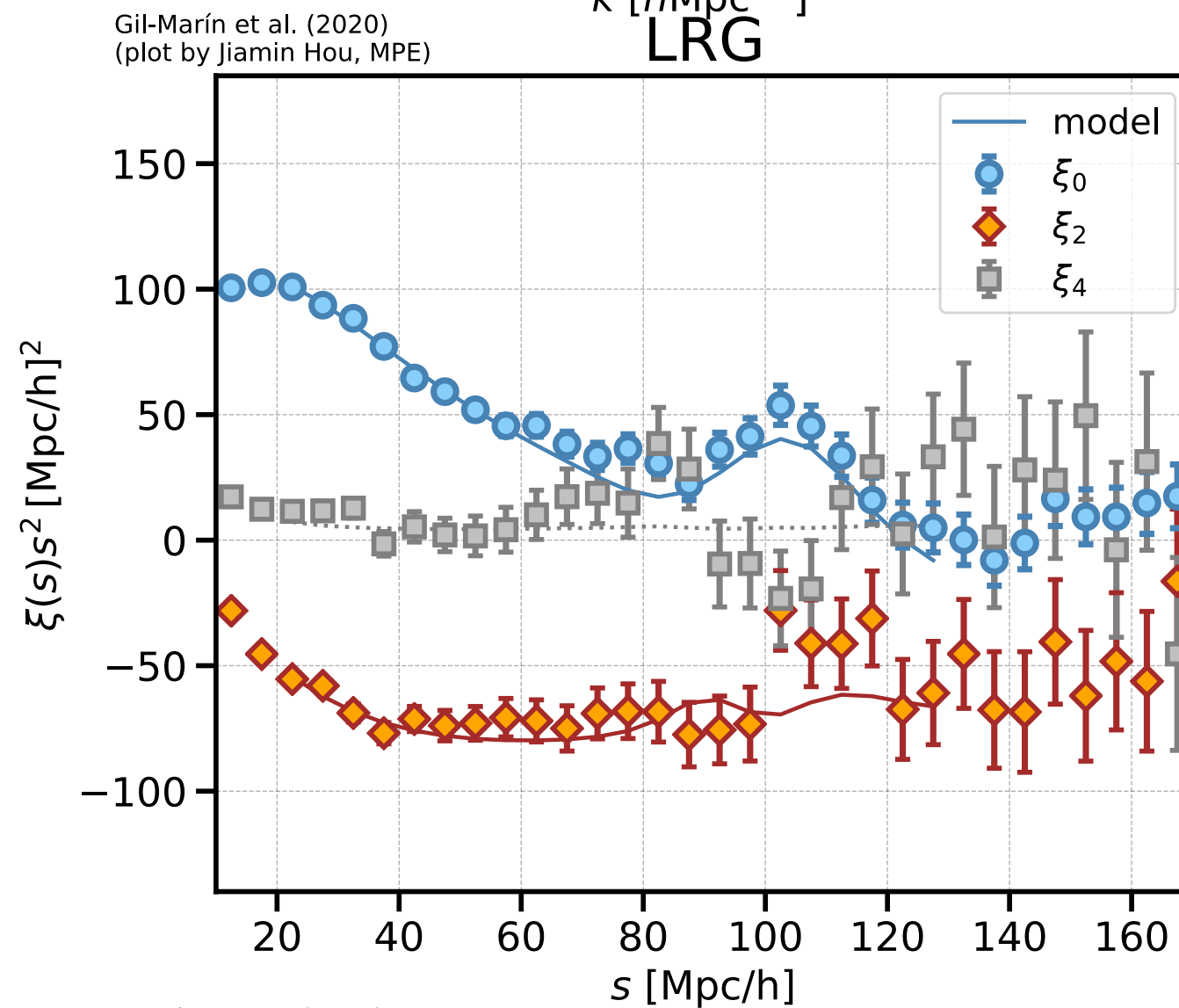
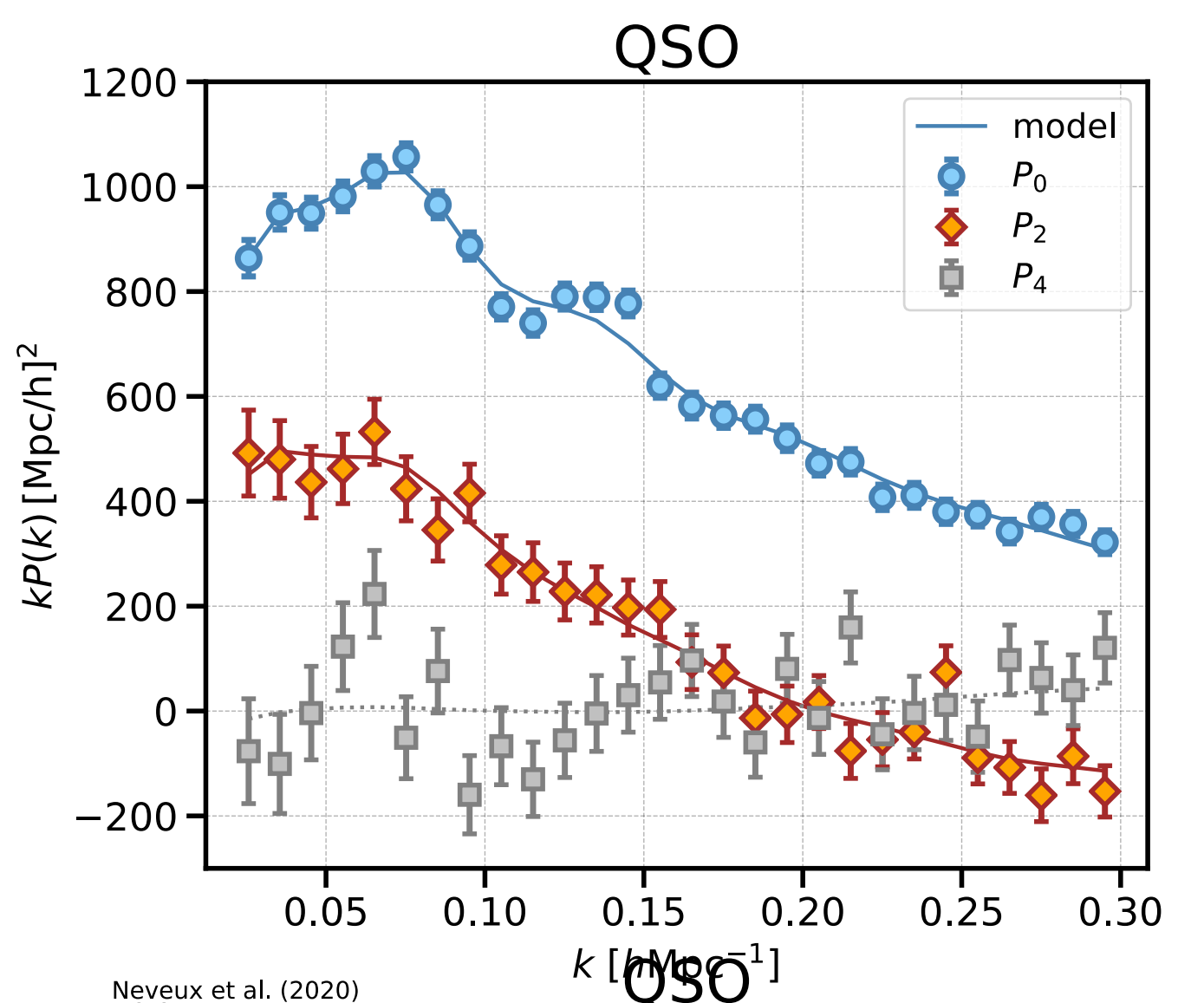
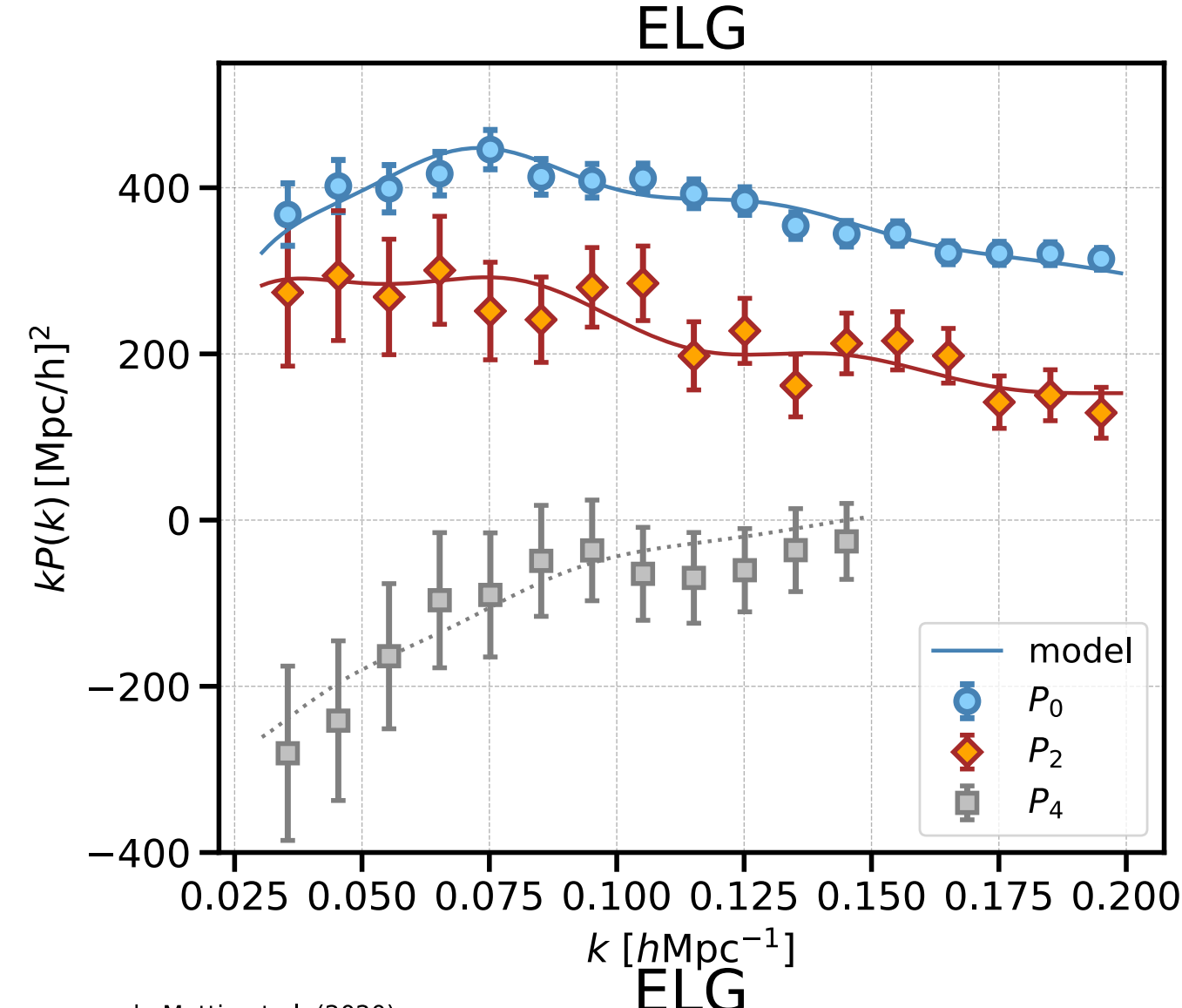
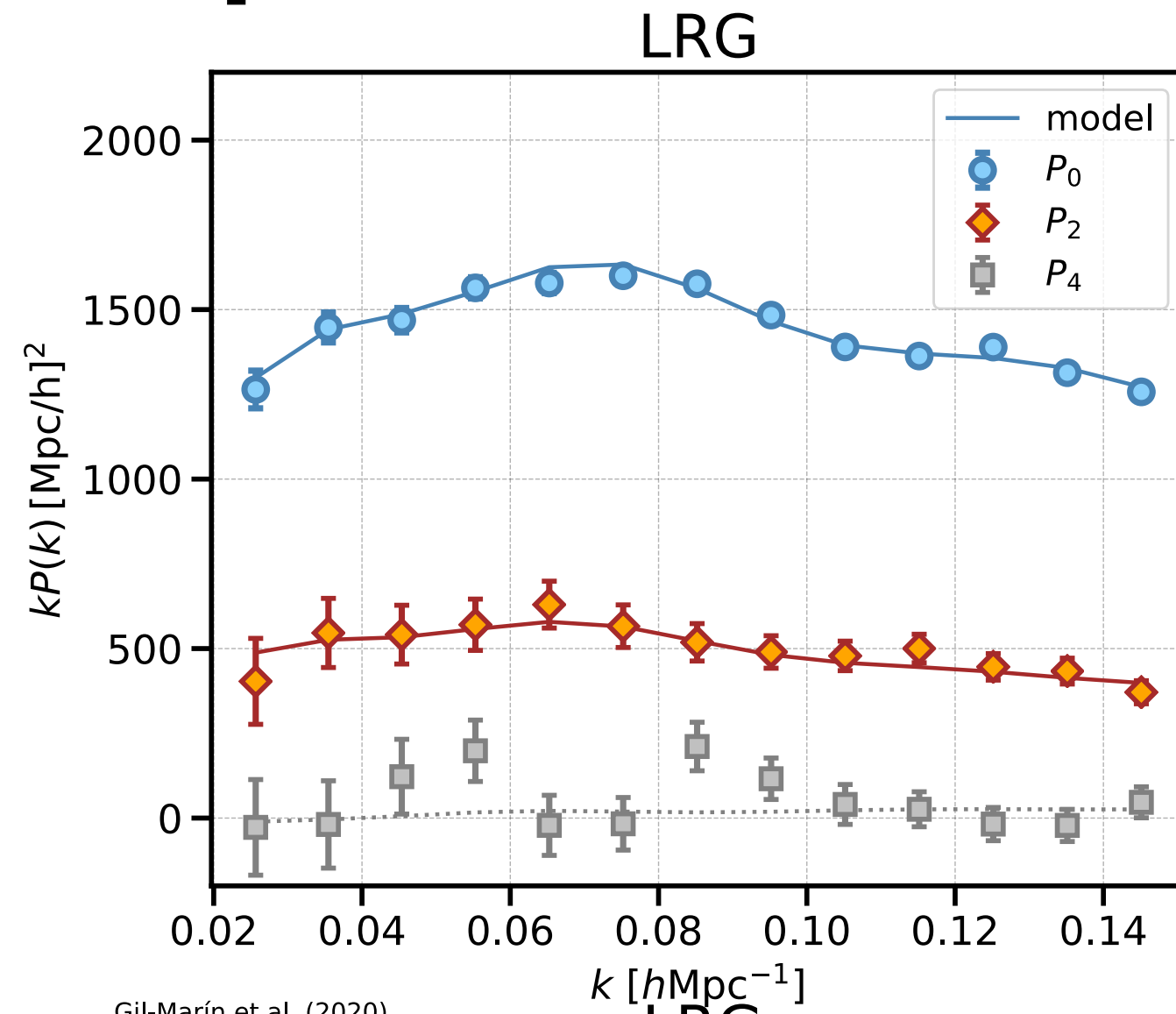
# Redshift Space Distortions: beyond Kaiser

- **LRG** {
  - **Fourier Space:** Resummed-PT + TNS
  - **Configuration Space:** RESPRESSO+TNS & CLPT-GS
  
- **ELG** {
  - **Fourier Space** RegPT +TNS
  - **Configuration Space** CLPT-GS
  
- **QSO** {
  - **Fourier Space** RegPT +TNS
  - **Configuration Space.** RESPRESSO+TNS

\*see J. Bautista & E. Müller talk for more eBOSS tracers

# eBOSS two-point statistics

Fourier Space  $\rightarrow$



Config. Space  $\rightarrow$

Bautista et al. (2020) (plot by Jiamin Hou, MPE)

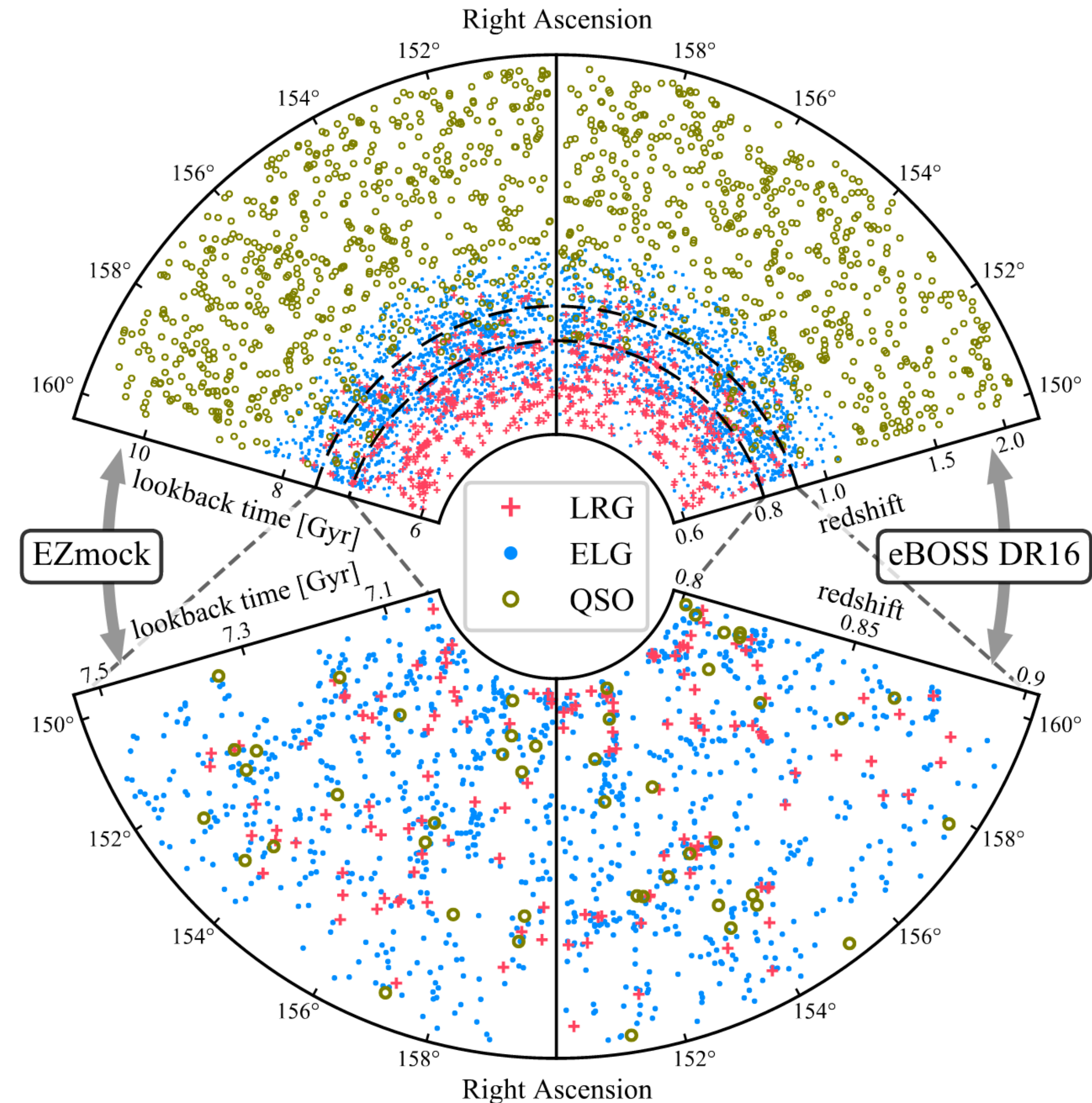
Tamone et al. (2020) (plot by Jiamin Hou, MPE)

Hou et al. (2020) (plot by Jiamin Hou, MPE)



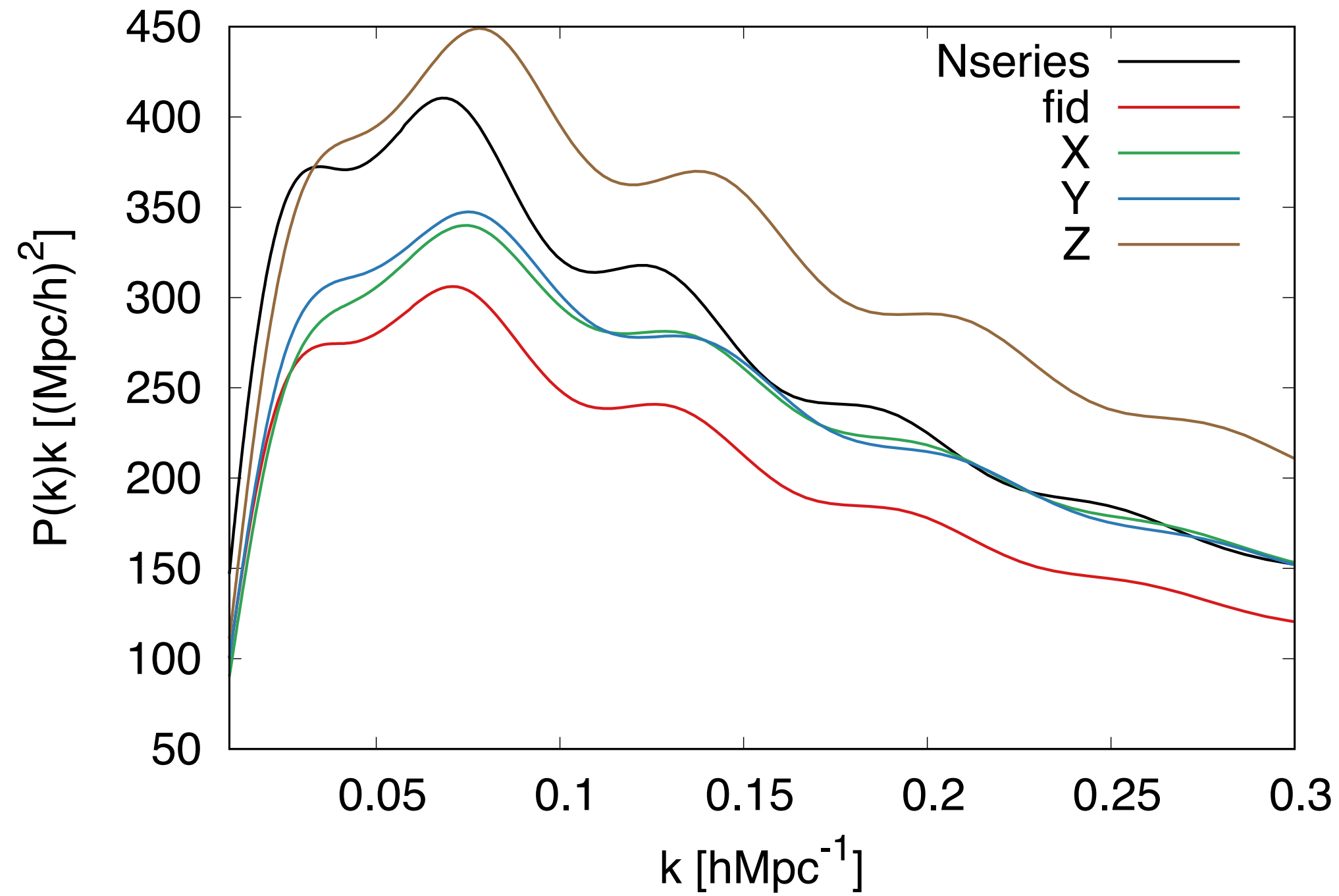
# Synthetic Catalogues

- Fast mocks: **Covariance**
  - 1000 realiz. EZmocks (ELG,LRG,QSO)
  - 2000 realiz. GLAM-QPM (ELG)
  
- N-body mocks: **Systematics**
  - OuterRim + HOD mocks (QSO,LRG, ELG)
  - N-series mocks (LRG)

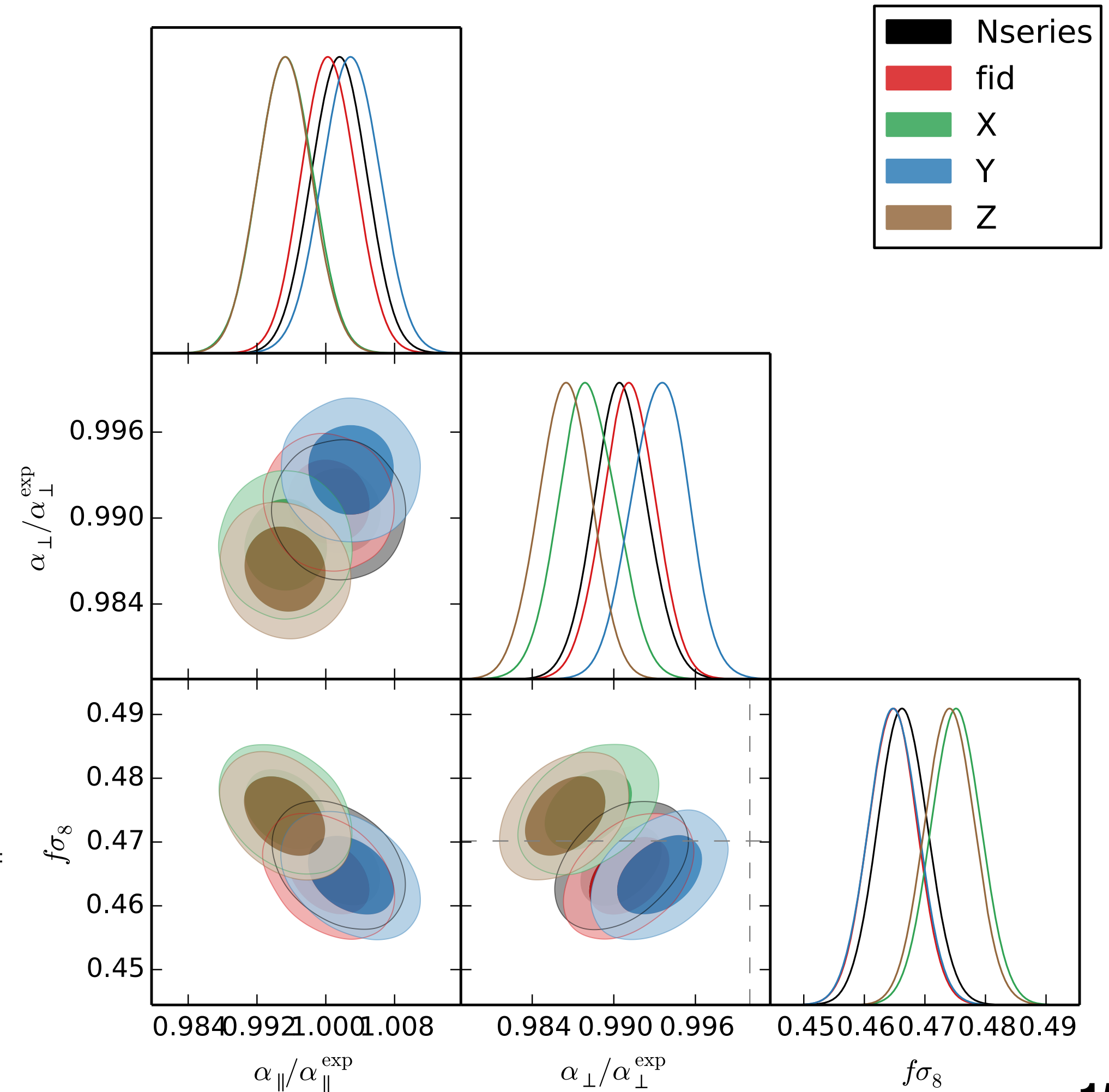


# Systematic checks: template-dependence

Template shapes tested

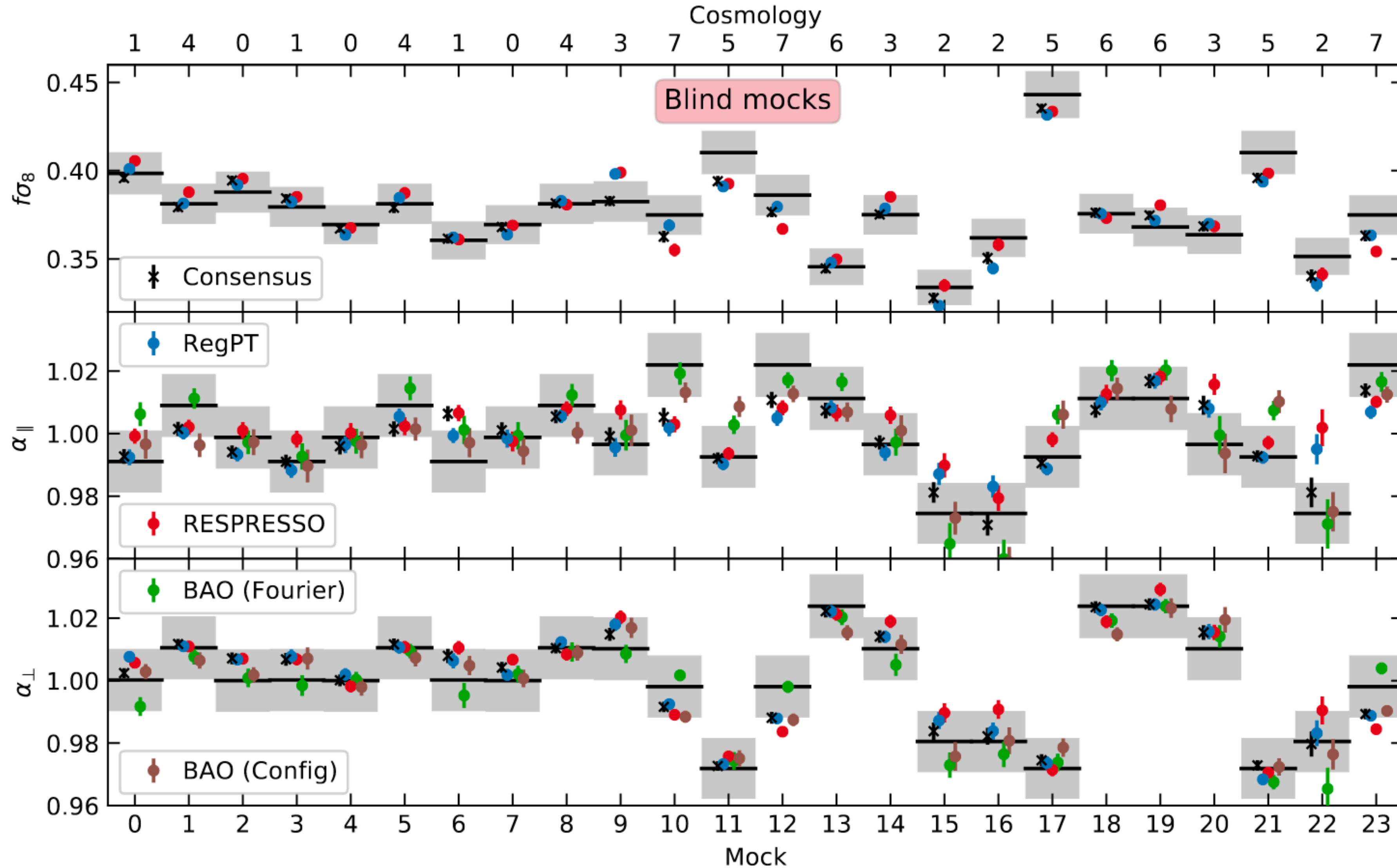


Performance on Nseries mocks

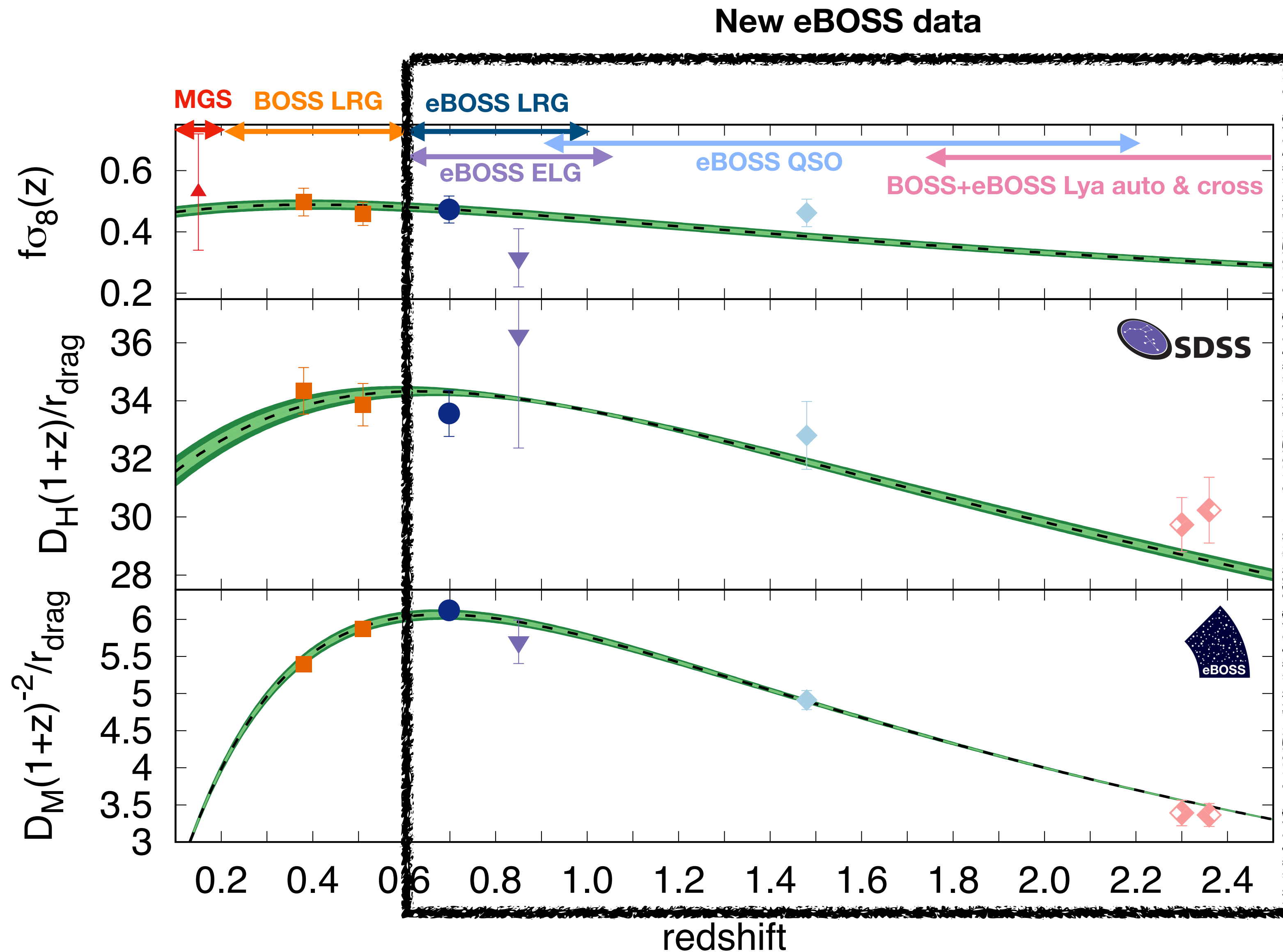


Model	$\Omega_m$	$\Omega_m h^2$	$\Omega_b$	$\Omega_b h^2$	$10^3 \times \Omega_\nu$	$h$	$n_s$	$A_s \times 10^9$	$\sigma_8^0$	$r_{\text{drag}} [\text{Mpc}]$	$N_{\text{eff}}$
$\Theta_{\text{fid}}$	0.310	0.1417	0.0481	0.0220	1.400	0.676	0.97	2.040	0.8	147.78	3.046
$\Theta_{\text{Nseries}}$	0.286	0.1401	0.0470	0.0230	0	0.700	0.96	2.146	0.82	147.15	3.046
$\Theta_X$	0.350	0.1599	0.0481	0.0220	1.313	0.676	0.97	1.767	0.814	143.17	3.046
$\Theta_Y$	0.350	0.1599	0.0481	0.0220	1.313	0.676	0.97	2.040	0.814	138.77	4.046
$\Theta_Z$	0.365	0.2053	0.0658	0.0370	0	0.750	0.96	2.146	0.9484	123.97	3.046

# Systematic checks: cosmology-dependence



# Conclusions



- SDSS-II, BOSS and eBOSS have provided direct measurements of  $D_M/r_{\text{drag}}$ ,  $D_H/r_{\text{drag}}$  and  $f\sigma_8$  in the redshift range from 0 up to 3 (up to 2 for  $f\sigma_8$ )
- So far, the largest spectroscopic galaxy survey: state-of-the-art measurements.

## $f\sigma_8$ precision

• MGS SDSS-II	<b>35%</b>
• LRG BOSS (low-z)	<b>9.0%</b>
• LRG BOSS (mid-z)	<b>8.2%</b>
• LRG BOSS+eBOSS	<b>9.4%</b>
• ELG eBOSS	<b>30%</b>
• QSO eBOSS	<b>9.7%</b>

# References

- Cosmology interpretation: [eBOSS collaboration et al.](#)
- Catalogues: [Ross et al.](#) (LRG & QSO), [Raichoor et al.](#) (ELG)
- LRG BAO & RSD: [Bautista et al.](#) (Config.), [Gil-Marín et al.](#) (Fourier)
- ELG BAO & RSD: [Tamone et al.](#) (Config.), [de Mattia et al.](#) (Fourier)
- QSO BAO & RSD: [Hou et al.](#) (Config.), [Neveux et al.](#) (Fourier)
- Ly- $\alpha$  BAO: [du Mas des Bourboux et al.](#) (Config.)
- Fast-mocks: [Zhao et al.](#) (EZmocks), [Sicheng et al.](#) (GLAM-QPM)
- Mock challenges: [Rossi et al.](#) (LRG), [Smith et al.](#) (QSO), [Alam et al.](#) (ELG), [Ávila et al.](#) (ELG)
- Other: [Zhao et al.](#) (Multi-tracer), [Aubert et al.](#) (Voids), [Nadathur et al.](#) (Voids), [Mohammad et al.](#) (PIP weights)