

# Field-space Effects in Preheating

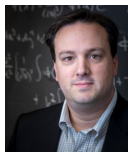
Evangelos Sfakianakis

Nikhef & Leiden University

Cosmology from Home 2020

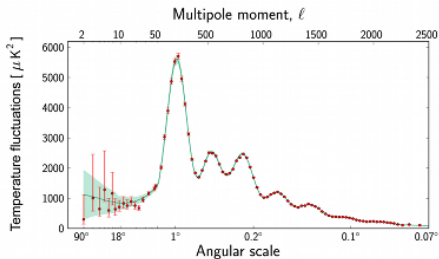
with [R. Nguyen](#), [J. van de Vis](#), [J. T. Giblin](#), [D. I. Kaiser](#)

- PRL **123**, 171301 (2019) [arXiv:1905.12562 [hep-ph]]
- arXiv:2005.00433 [astro-ph.CO], accepted PRD



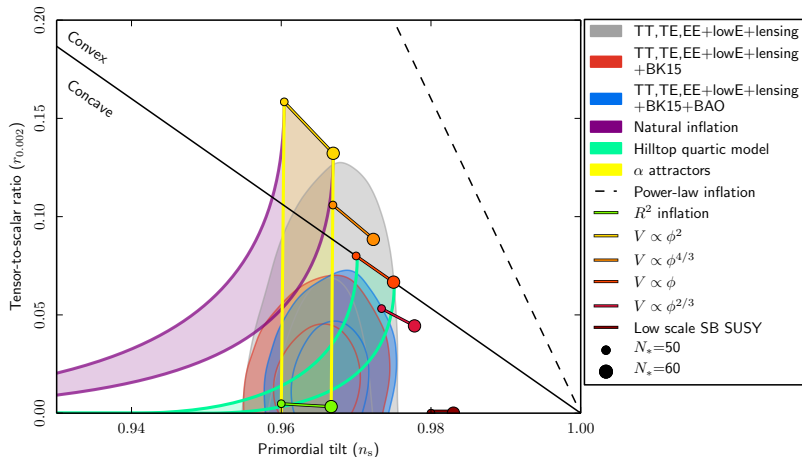
# Inflation: Successes and Predictions

- Solve horizon & flatness problems
- Explain **fluctuations** as stretched quantum mechanical perturbations
- Predict a **nearly scale invariant** spectrum (of tunable amplitude)
- Predict almost **Gaussian** perturbations



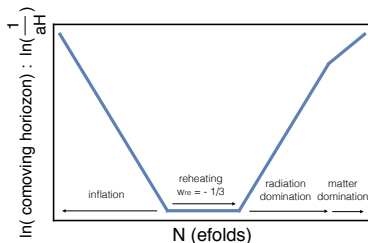
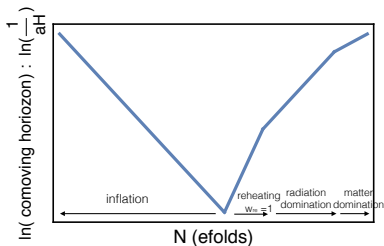
- Spectral index is  $5\sigma$  away from flat
- Spectral index running is small
- $|f_{NL}| \lesssim \mathcal{O}(1)$

# Hints from the sky

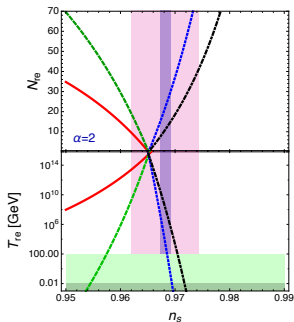


Plateau models of inflation are consistent with *Planck* data.

# Reheating



Cook et al. 2015

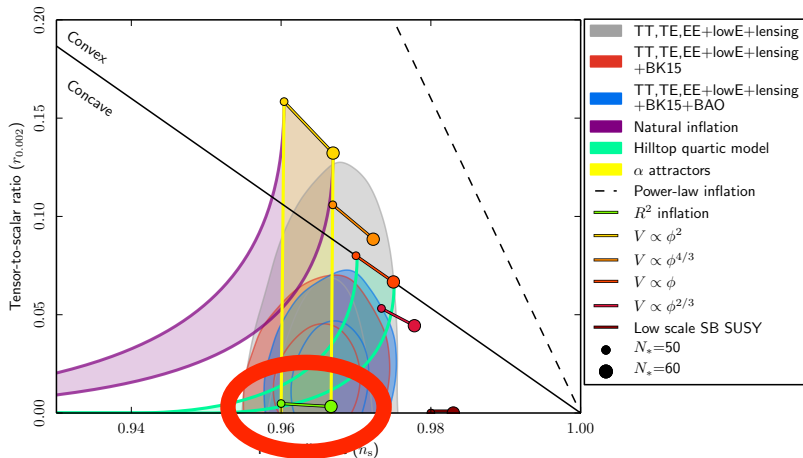


The reheating history connects the times of horizon exit & re-entry of perturbations  
 $\Rightarrow$  shifts CMB observables

*“The value of  $N_*$  is not well constrained and depends on unknown details of reheating”*

CMB-S4 Science Book, 2016

# Hints from the sky



Plateau models of inflation are consistent with *Planck* data,  
⇒ the time of horizon exit is being constrained.

# Mon-minimal coupling & Conformal Transformations

Non-minimal coupling to gravity:  $\mathcal{L} \subset \xi\phi^2 R$

$$S_{\text{Jordan}} = \int d^4x \sqrt{-\tilde{g}} \left[ f(\phi^I) \tilde{R} - \frac{1}{2} \tilde{G}_{IJ} \tilde{g}^{\mu\nu} \partial_\mu \phi^I \partial_\nu \phi^J - \tilde{V}(\phi^I) \right]$$

$$\tilde{g}_{\mu\nu}(x) = \frac{2}{M_{\text{Pl}}^2} f(\phi^I(x)) \tilde{g}_{\mu\nu}(x)$$

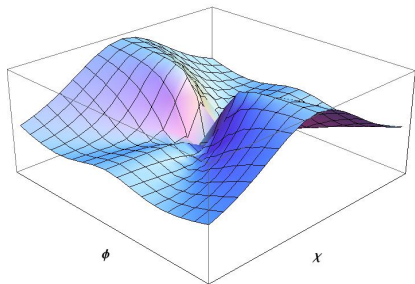
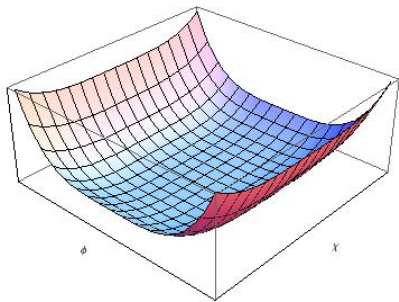


$$S_{\text{Einstein}} = \int d^4x \sqrt{-g} \left[ \frac{M_{\text{Pl}}^2}{2} R - \frac{1}{2} G_{IJ} g^{\mu\nu} \partial_\mu \phi^I \partial_\nu \phi^J - V(\phi^I) \right]$$

$$V(\phi^I) = \frac{M_{\text{Pl}}^4}{4f^2(\phi^I)} \tilde{V}(\phi^I)$$

# Jordan vs Einstein

$$f(\phi, \chi) = \frac{1}{2} [M_{Pl}^2 + \xi_\phi \phi^2 + \xi_\chi \chi^2] , \quad V(\phi, \chi) = \frac{\lambda_\phi}{4} \phi^4 + \frac{\lambda_\chi}{4} \chi^4 + \frac{g}{2} \phi^2 \chi^2$$



$$V(\phi^I) \rightarrow \frac{M_{Pl}^2}{4} \frac{\lambda_I}{\xi_I} \Rightarrow H = \frac{M_{Pl}}{\sqrt{12}} \sqrt{\frac{\lambda}{\xi^2}}$$

# Einstein-frame Field-space

In the Einstein frame, the field-space manifold is curved:

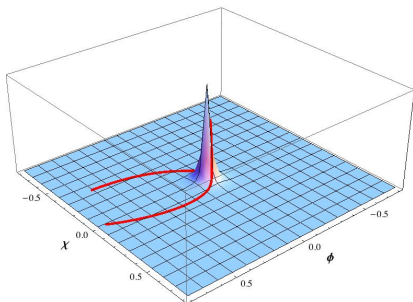
$$\mathcal{G}_{IJ}(\phi^K) = \left( \frac{M_{Pl}^2}{2f(\phi^K)} \right) \left[ \delta_{IJ} + \frac{3}{f(\phi^K)} f_{,I} f_{,J} \right] \neq F(\phi^K) \delta_{IJ}$$

$\phi^I$ : coordinates in field space  $\longleftrightarrow x^\mu$

$\mathcal{G}_{IJ}$  ( $\sim \frac{1}{\phi^2}$ ): metric on field space  $\longleftrightarrow g_{\mu\nu}$  (Note:  $\mathcal{G}_{IJ} \propto \phi^{-2}$ )

$$\mathcal{D}_J A^I = \partial_J A^I + \Gamma^I_{JK} A^K$$

We can “turn off” the potential and visualize the effects of the field-space metric alone.

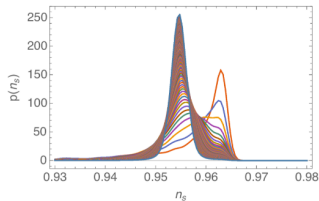




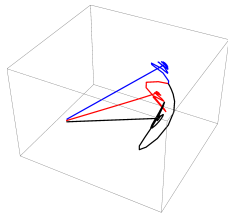
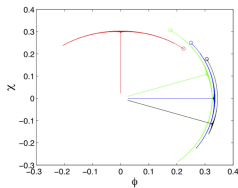
# Inflation and multiple fields

Only one scalar field at **high energies** is rather unlikely.

How do these models,  $\mathcal{L} \subset \xi\phi^2 R$ , cope with **many scalar fields**?



Easter, Frazer, Peiris, Price



Kaiser & EIS 2014

- Multi-field quadratic model  $V = \sum m_I^2 \phi_I^2$
- Simple models shift predictions for  $n_s$ .
- Non-minimal couplings lead to **strong single-field attractors**
- **Robust** Starobinsky-like predictions

$$n_s \simeq 1 - \frac{2}{N} \simeq 0.96\dots, \quad r \simeq \frac{12}{N^2} = \mathcal{O}(10^{-3})$$

# Equations of motion

Background fields:

$$\mathcal{D}_t \dot{\phi}^I + 3H \dot{\phi}^I + g^{IK} V_{,K} = 0$$

where  $\mathcal{D}_t A^I \equiv \dot{A}^I$  for our choice of variables

Fluctuations:

$$\ddot{Q}'_k + 3H \dot{Q}'_k + \left[ \frac{k^2}{a^2} \delta^I_J + \mathcal{M}'_J \right] Q'_k = 0$$

where

$$\mathcal{M}'_J = g^{IK} \mathcal{D}_J \mathcal{D}_K V - \mathcal{R}'_{LMJ} \dot{\phi}^L \dot{\phi}^M - \frac{1}{M_{Pl}^2 a^3} \mathcal{D}_t \left( \frac{a^3}{H} \dot{\phi}^I \dot{\phi}_J \right)$$

# Quantizing the fluctuations

For motion **along the single-field attractor**,  
quantization is simple

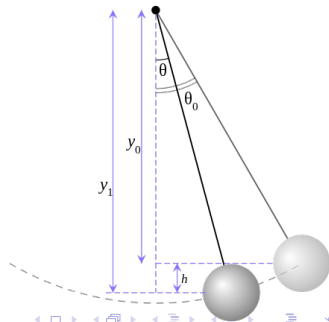
$$\hat{Q}^\phi(x^\mu) = \sqrt{g^{\phi\phi}} a(t) \int \frac{d^3k}{(2\pi)^{3/2}} \left[ (v_k \hat{b}_k) e^{i\mathbf{k}\cdot\mathbf{x}} + \text{c.c.} \right]$$

$$\hat{Q}^\chi(x^\mu) = \sqrt{g^{\chi\chi}} a(t) \int \frac{d^3k}{(2\pi)^{3/2}} \left[ (z_k \hat{c}_k) e^{i\mathbf{k}\cdot\mathbf{x}} + \text{c.c.} \right]$$

Re-write as a harmonic oscillator

$$v_k'' + \Omega_{(\phi)}^2(k, \tau) v_k \simeq 0, \quad v_k \longleftrightarrow \delta\phi_k$$

$$z_k'' + \Omega_{(\chi)}^2(k, \tau) z_k \simeq 0, \quad z_k \longleftrightarrow \delta\chi_k$$



# Effective Mass-squared: Ingredients

$$\partial_\tau^2 v_k + (k^2 + a^2 m_{\text{eff},\phi}^2) v_k = 0 \quad , \quad \partial_\tau^2 z_k + (k^2 + a^2 m_{\text{eff},\chi}^2) z_k = 0$$

$$m_{\text{eff},I}^2 = m_{1,I}^2 + m_{2,I}^2 + m_{3,I}^2 + m_{4,I}^2$$

$$m_{1,\phi}^2 \equiv \mathcal{G}^{\phi K} (\mathcal{D}_\phi \mathcal{D}_K V) \longleftrightarrow \text{potential gradient}$$

$$m_{2,\phi}^2 \equiv -\mathcal{R}^\phi_{LM} \dot{\phi}^L \dot{\phi}^M \longleftrightarrow \text{non-trivial field-space manifold}$$

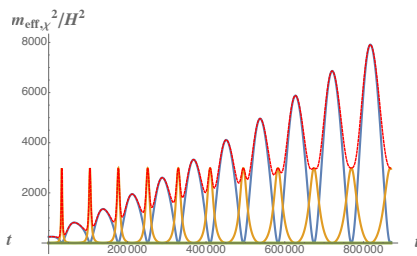
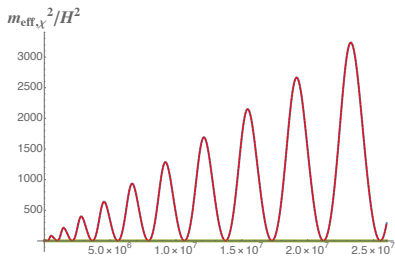
$$m_{3,\phi}^2 \equiv -\frac{\delta_I^\phi \delta_\phi^J}{M_{\text{Pl}}^2 a^3} \mathcal{D}_t \left( \frac{a^3}{H} \dot{\phi}^I \dot{\phi}_J \right) \longleftrightarrow \text{coupled metric perturbations}$$

$$m_{4,\phi}^2 \equiv -\frac{1}{6} R \longleftrightarrow \text{changes in the background spacetime}$$

# Effective Mass-squared for $\chi$ fluctuations

$$\xi = 0.1 \ll 1$$

$$\xi = 10$$

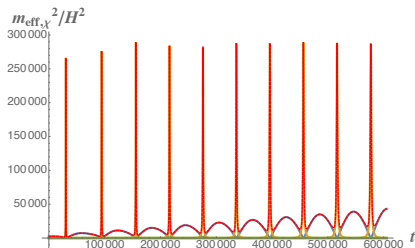


$$m_{\text{eff}}^2 \approx m_1^2 + m_2^2 + m_3^2$$

$$m_{\text{eff}}^2 \approx \text{potential} + \text{fieldspace} + \text{metric}$$

# Effective Mass-squared for $\xi = 100 \gg 1$

An “unusual” way for **adiabaticity violation** when  $\mathcal{R}$  spikes.



We define

$$\mathcal{A}(k, \tau) \equiv \frac{\Omega'(k, \tau)}{\Omega^2(k, \tau)}$$

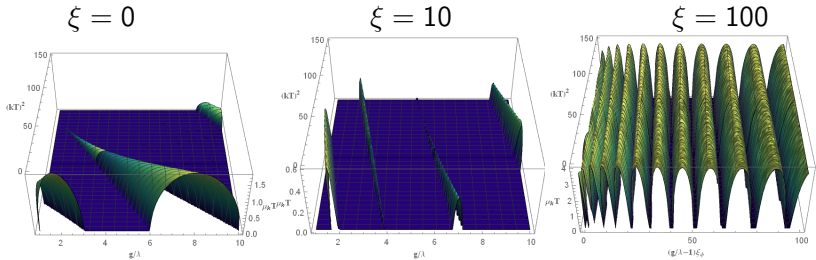
where

$$\Omega^2(k, \tau) = k^2 + a^2 m_{\text{eff},\phi}^2(\tau)$$

Adiabaticity is violated for  $\Omega' \gg \Omega^2$ , rather than  $\Omega \approx 0$ .

A broad range of wavenumbers is excited  $k \lesssim \xi \phi H_{\text{end}}$

# Floquet charts

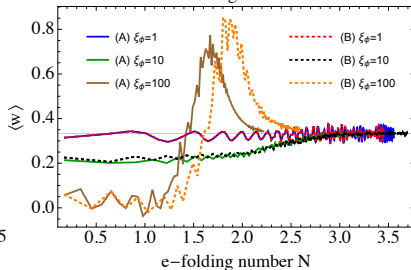
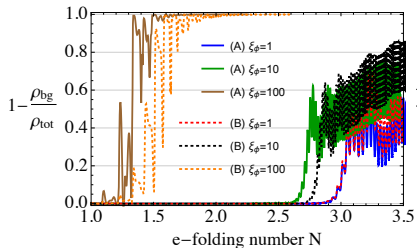
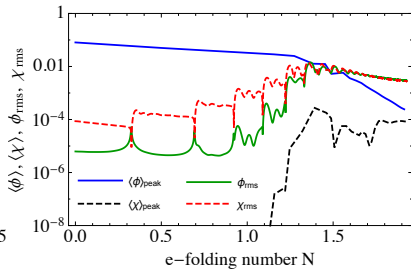
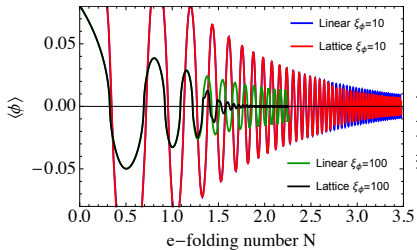


Efficient particle production  
can lead to **nonlinear effects**



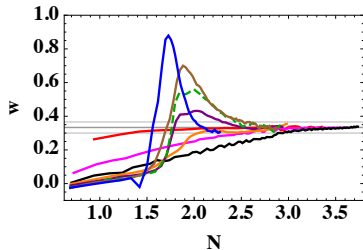
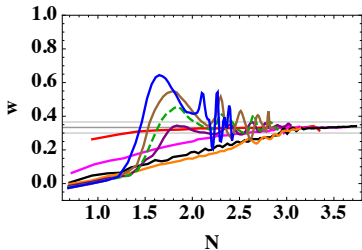
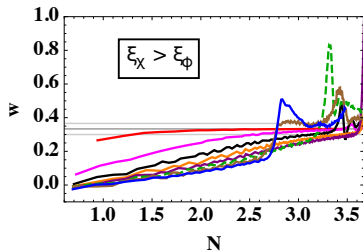
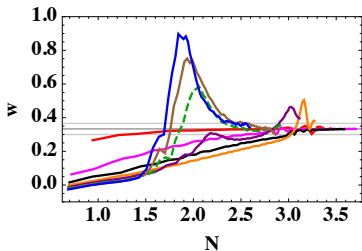
Need for  
lattice simulations

# Lattice results: Benchmark Case

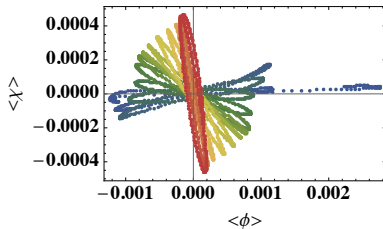
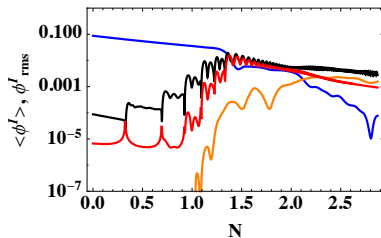




# Lattice results: Parameter Scan

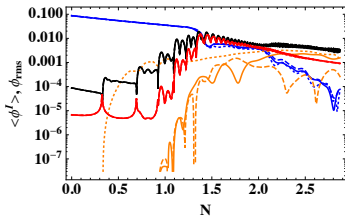
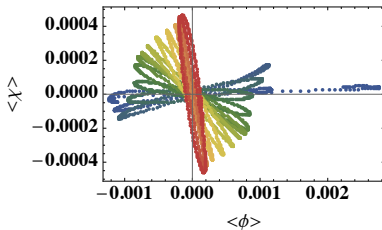
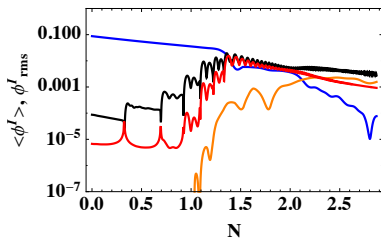


# Strong resonance and single-field motion



$\langle \chi \rangle > \langle \phi \rangle \Rightarrow$  Multi-field background motion (???)

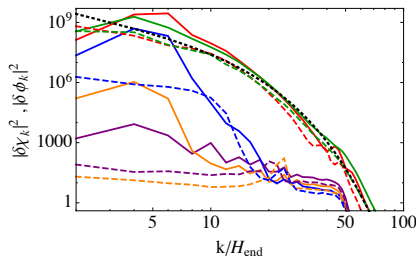
# Strong resonance and single-field motion



- $\langle \chi^2 \rangle \gg \langle \chi \rangle^2$
- initial-condition-dependent  $\langle \chi \rangle$
- No coherent background motion on super-horizon scales

$\Rightarrow$  **CMB modes are safe**

- **Fast preheating** for  $\xi \gtrsim 100$
- Efficient re-scattering  
 $\Rightarrow$  onset of **thermalization**
- **Robust single-field attractor**
- Fast approach to  $w \rightarrow 1/3$
- Detailed understanding of the **whole parameter space**



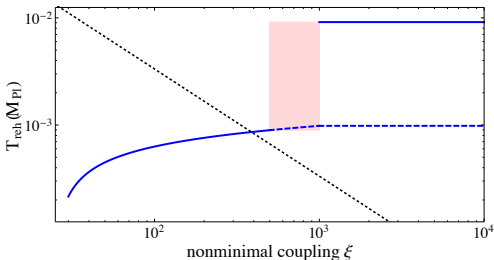
Non-minimal couplings  
quickly lead to a  
**thermal radiation bath**  
while **preserving**  
**CMB predictions**

# One last thing!

**Higgs inflation** is a multi-field non-minimally coupled model with known SM couplings  $\Rightarrow$  the inflaton decays into W, Z bosons.

$$m_{\text{spike}} \sim \xi H_{\text{end}}$$

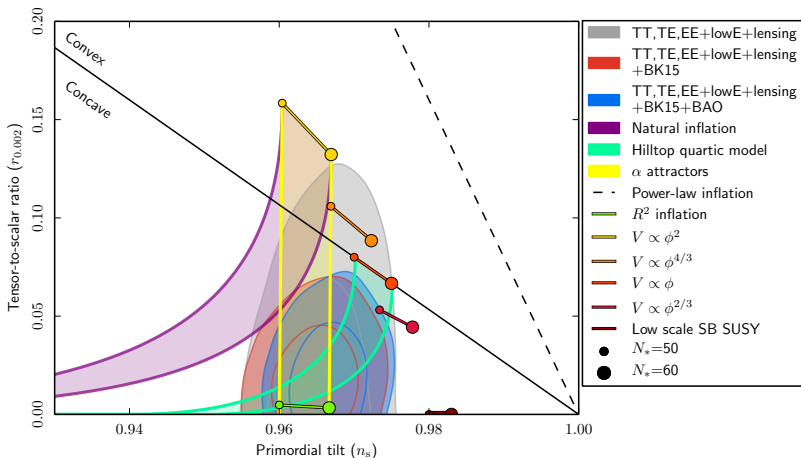
$$m_B \sim \frac{10^5}{\sqrt{\xi}} H_{\text{end}}$$



For  $\xi \gtrsim 10^3$  preheating completes within **ONE** oscillation

van de Vis & E.I.S, Phys. Rev. D **99**, no.8, 083519 (2019)

# Observations



Understanding **preheating** in major plateau models  
reduces theoretical **error-bars** of the  $n_s - r$  plot