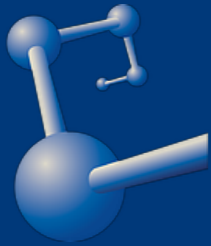


Instituto de  
Ciencias  
Nucleares  
UNAM



# Precision Cosmology for modified gravity

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**Celia Escamilla-Rivera**

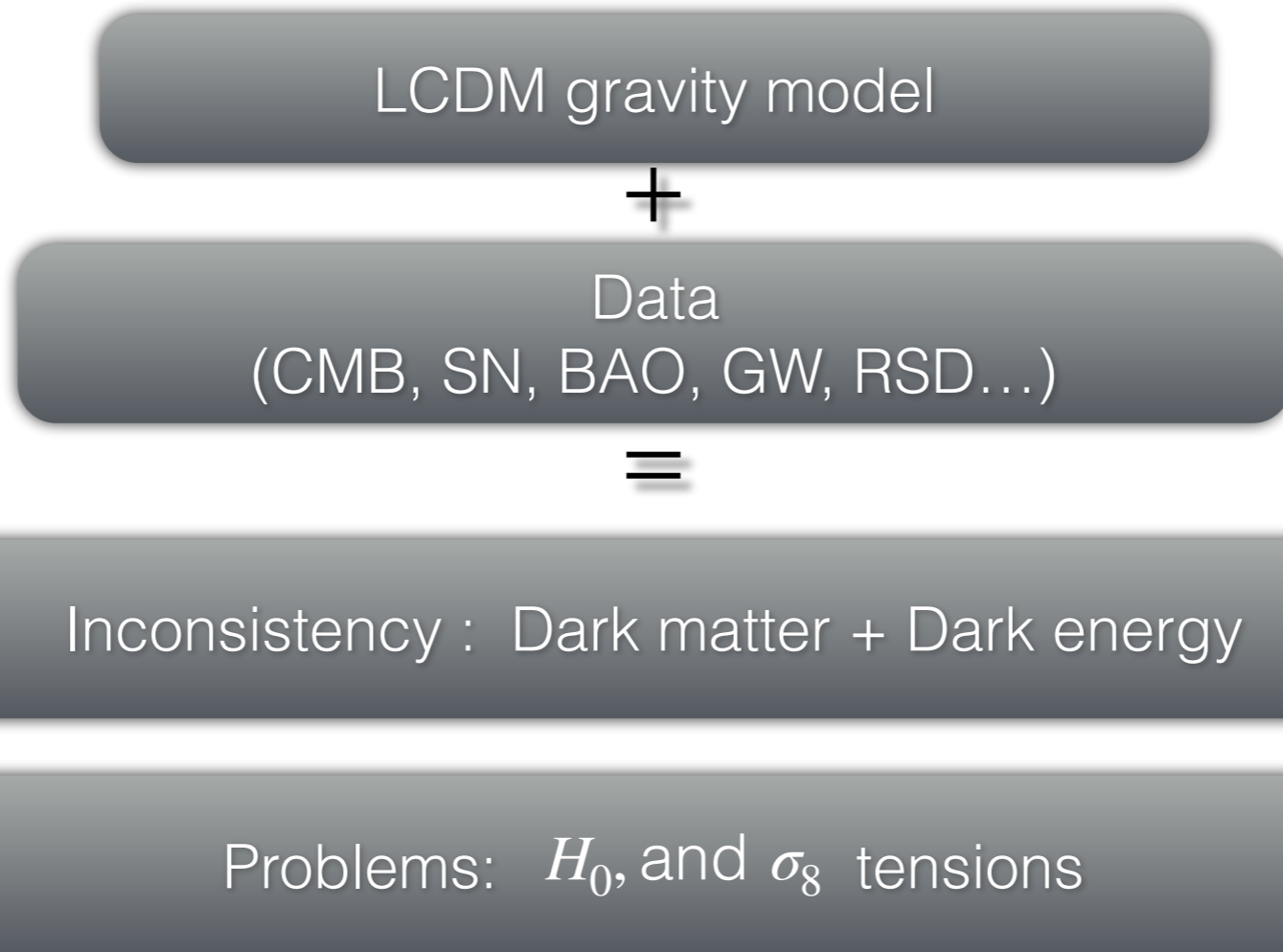
Nuclear Institute of Sciences (ICN-UNAM, Mexico)

Royal Astronomical Society (RAS, UK)

Cosmology from Home 2020

24 August 2020 – 04 September 2020

- Cosmology and Modified Gravity state-of-art
- Precision Cosmostatistics for Modified Gravity (MG)
- Frontiers in MG using Precision Cosmology



New Physics?

**Initial Conditions**

**Inflation**

Primordial GWs?

**Cosmic Structure**

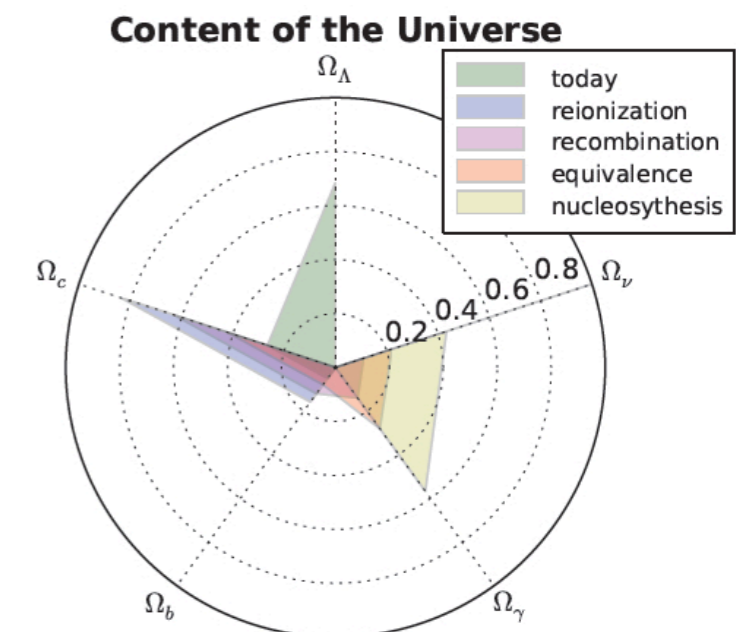
**Dark Matter**

Ultra-light/Axion?  
Primordial BHs?

**Late acceleration**

$\Lambda$

**Modified Gravity?**



## Two main roots to determining $H_0$

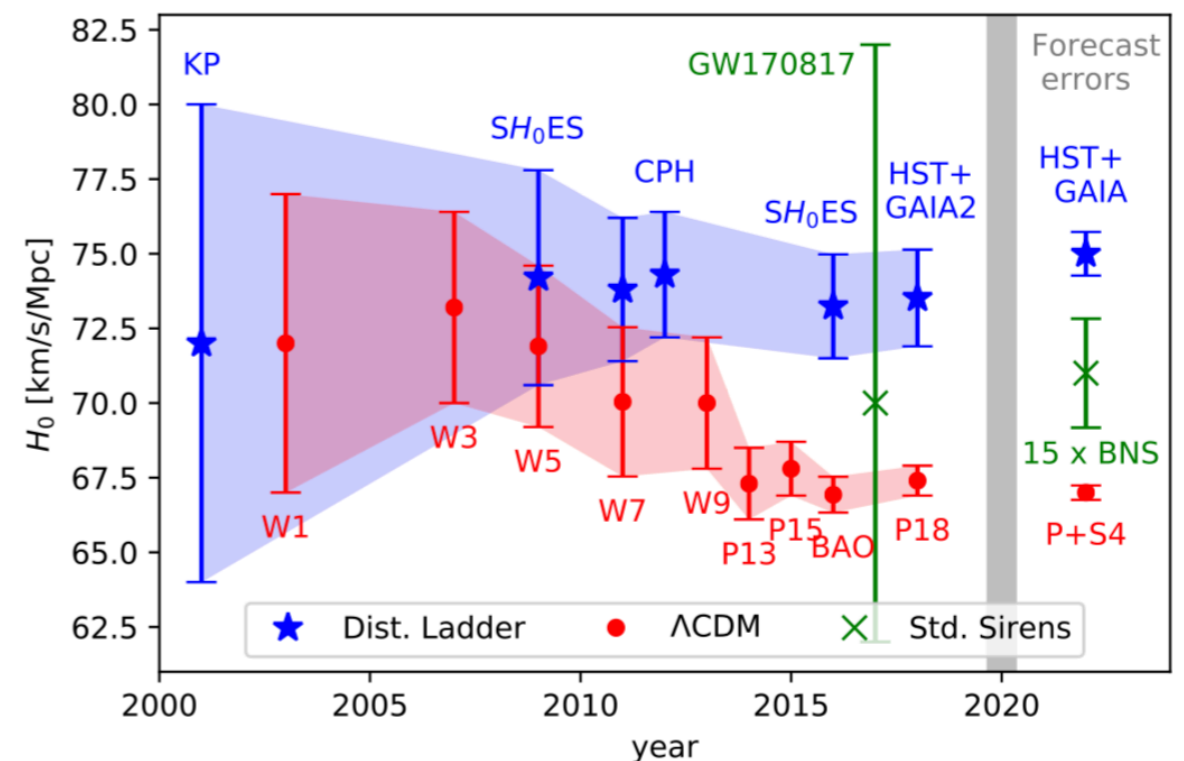
(1) **Distance ladder method**: Cepheids and TRGBs (calibrated to geometric anchor distances)

Improved: from 10% (2001) to  $< 2\%$  (2019)

Value:  $H_0 = 74.03 \pm 1.42$  km/s/Mpc

(2) **Via sound horizon observed from CMB**: not constrained directly. Using data at  $z \sim 1100$  and extrapolated to  $z \sim 0$ , based on the physics of the early universe.

Value:  $H_0 = 67.4 \pm 0.5$  km/s/Mpc



## Novel measurements of $H_0$

- Quasars strongly gravitationally lensed: H0LiCOW collaboration [Bonvin et al 2017]

$$\text{Value: } H_0 = 73.3_{-1.8}^{+1.7} \text{ km/s/Mpc}$$

- Geometric distantes measurements to megamaster-hosting galaxies:

Megamaster Cosmology Project [Pesce et al 2020]

$$\text{Value: } H_0 = 73.9 \pm 3.0 \text{ km/s/Mpc}$$

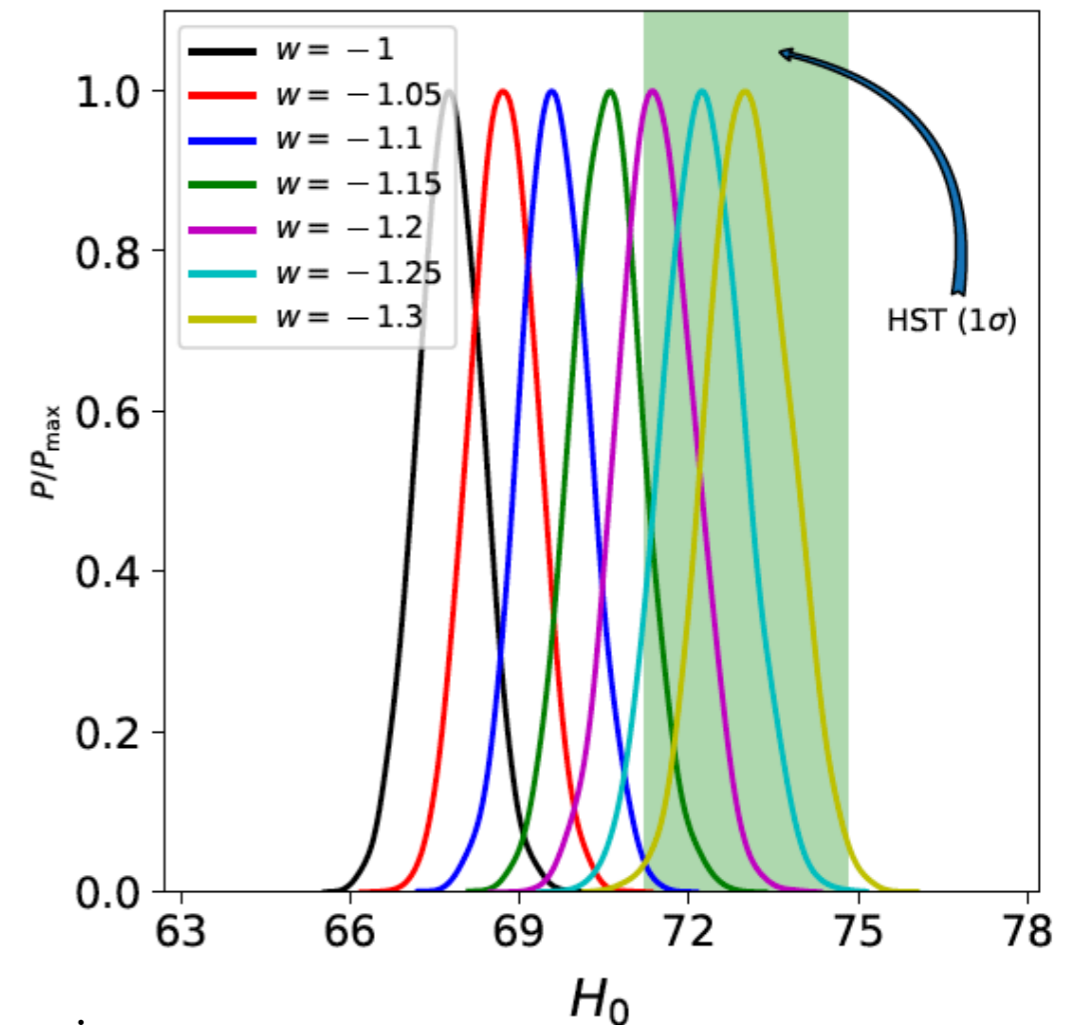
- **Standard sirens** from merger events detected through GW [Abbott et al 2017]

$$\text{Value: } H_0 = 70_{-8}^{+12} \text{ km/s/Mpc}$$

## Novel measurements of $H_0$ : Possible solutions

Physics beyond the canonical LCDM:

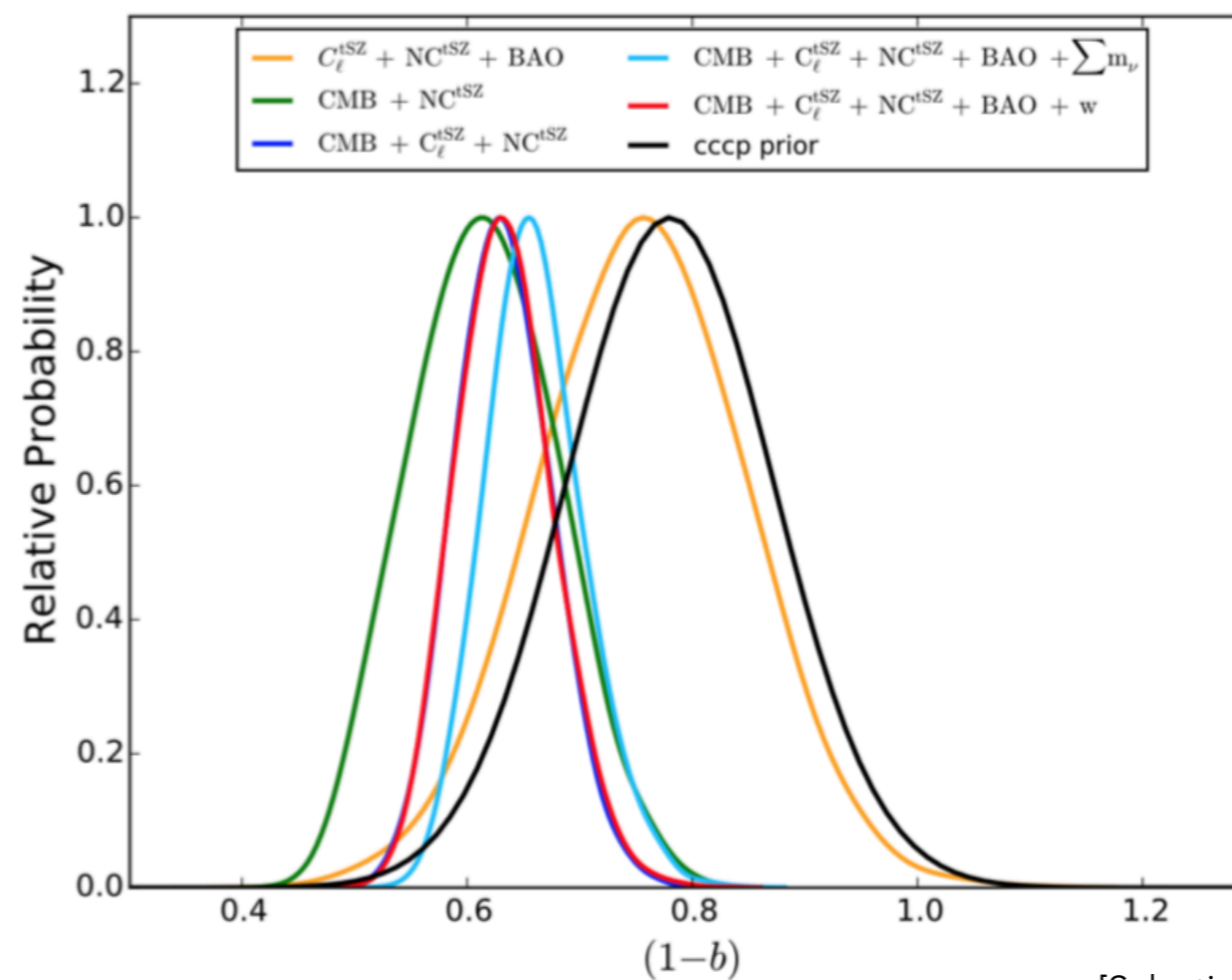
- phantom dark energy,
- dark radiation,
- dynamical dark energy,
- holographic dark energy,
- non-linear parametric dark energy,
- $f(T)$  gravity,
- $f(T,B)$  gravity,
- extended dark energy components with massive neutrinos, ...



## Tension in the matter fluctuation amplitude $\sigma_8$

Interesting since galaxy clusters and weak lensing observations are sensitive to the cosmic matter density.

Powerful complementary probe to CMB data and geometric observables.



[Salvati, L et al (2018) A&A 614, A13]

**Lovelock's theorem (1971)** [version from T. Clifton, et al Phys.Rept. 513 (2012)]

"The only second-order, local gravitational field equations derivable from an action containing solely the 4D metric tensor (plus related tensors) are the Einstein field equations with a cosmological constant"

$$S_{grav} = \frac{M_{Pl}^2}{2} \int \sqrt{-g} d^4x [R]$$



**Lovelock's theorem (1971)** [version from T. Clifton, et al Phys.Rept. 513 (2012)]

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$$S_{grav} = \frac{M_{Pl}^2}{2} \int \sqrt{-g} d^4x \left[ \phi R - \frac{\omega(\phi)}{\phi} (\nabla \phi)^2 - 2V(\phi) \right]$$

**Lovelock's theorem (1971)** [version from T. Clifton, et al Phys.Rept. 513 (2012)]

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$$S_{grav} = \frac{M_D^2}{2} \int \sqrt{-\gamma} d^D x [\mathcal{R} + \alpha \mathcal{G}]$$

**Lovelock's theorem (1971)** [version from T. Clifton, et al Phys.Rept. 513 (2012)]

"The only **second-order**, local gravitational field equations derivable from an action containing **solely the 4D metric tensor** (plus related tensors) are the Einstein field equations with a cosmological constant"

$$S_{grav} = \frac{M_{Pl}^2}{2} \int \sqrt{-g} d^4x [R + \beta_1 R \nabla_\mu \nabla^\mu R + \beta_2 \nabla_\mu R_{\beta\gamma} \nabla^\mu R^{\beta\gamma}]$$

**Lovelock's theorem (1971)** [version from T. Clifton, et al Phys.Rept. 513 (2012)]

"The only **second-order, local** gravitational field equations derivable from an action containing **solely the 4D metric tensor** (plus related tensors) are the Einstein field equations with a cosmological constant"

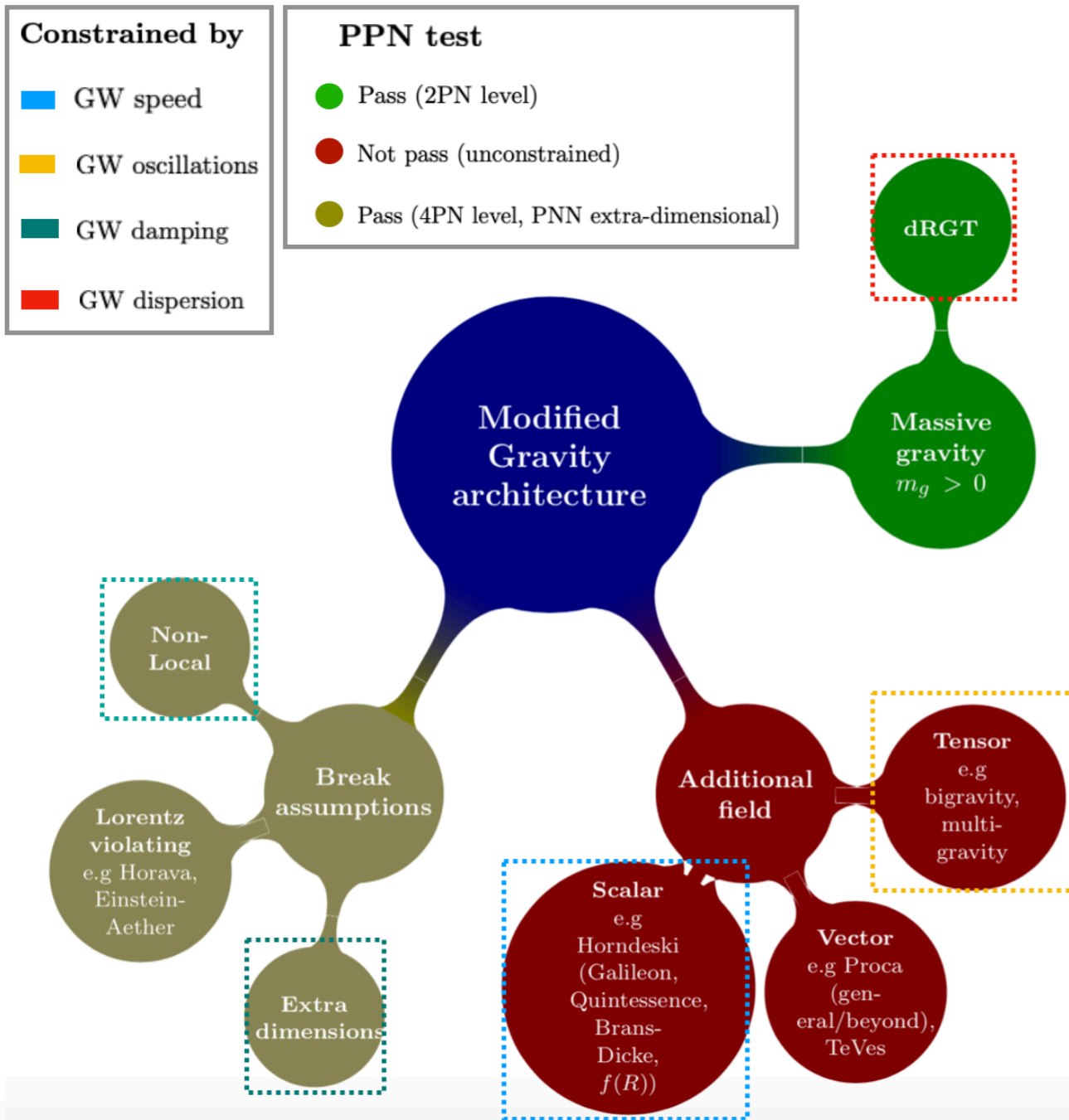
$$S_{grav} = \frac{M_{Pl}^2}{2} \int \sqrt{-g} d^4x \left[ R + f\left(\frac{1}{\square} R\right) \right]$$

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“The only **second-order, local** gravitational field equations **derivable from an action** containing **solely the 4D metric tensor** (plus related tensors) are the Einstein field equations with a cosmological constant”

? ? ? ? ? ?

[C. Escamilla-Rivera, Júlio Fabris. A non-lagrangian theory of gravity. Foundations on Physics (2020)]



Viable after GW170817

$c_g = c$	$c_g \neq c$
General Relativity Quintessence/k-essence Brans-Dicke/ $f(R)$ Kinetic Gravity Braiding	Quartic/quintic Galileons Fab Four de Sitter Horndeski $G_{\mu\nu}\phi^\mu\phi^\nu, f(\phi)$ . Gauss-Bonnet
Derivative Conformal Disformal Tuning Quadratic DHOST with $A_1 = 0$	Quartic/quintic GLPV Quadratic DHOST with $A_1 \neq 0$ Cubic DHOST

Non-viable after GW170817

[C. Escamilla-Rivera, Júlio Fabris. Foundations on Physics (2020)]

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## f(R)-like cosmology parameterisation

[Jaime L., Jaber, M., Escamilla-R, C. Phys.Rev D98 (2019)]

[Escamilla-R, C. V. Motta, M. Aspeitia and A. Almada. arXiv:2005.13957 (2020)]

$$S[g_{ab}, \psi] = \int \frac{f(R)}{2\kappa} \sqrt{-g} d^4x + S_{\text{matt}}[g_{ab}, \psi],$$

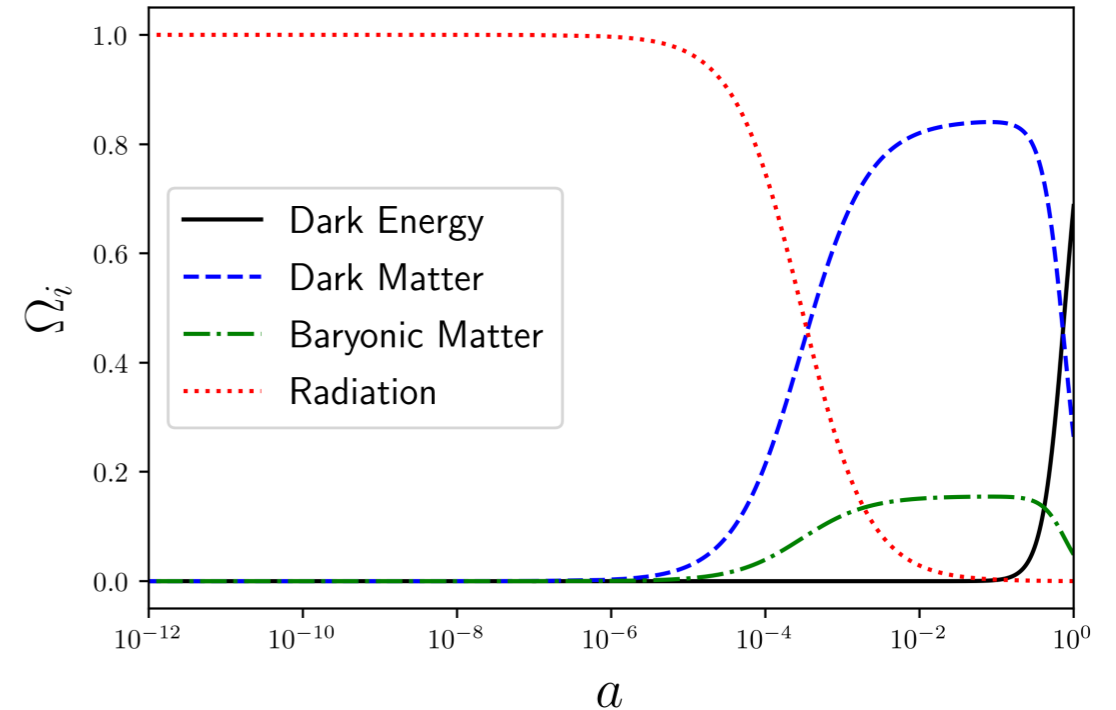
$$\ddot{R} = -3H\dot{R} - \frac{1}{3f_{RR}} \left[ 3f_{RRR}\dot{R}^2 + 2f - f_R R + \kappa T \right],$$

$$H^2 = -\frac{1}{f_{RR}} \left[ f_{RR} H \dot{R} - \frac{1}{6} (R f_R - f) \right] - \frac{\kappa T_t^t}{3f_R},$$

$$\dot{H} = -H^2 - \frac{1}{f_R} \left[ f_{RR} H \dot{R} + \frac{f}{6} + \frac{\kappa T_t^t}{3} \right],$$

$$\omega_X = \frac{3H^2 - 3\kappa P - R}{3(3H^2 - \kappa\rho)},$$

$$R = 6(\dot{H} + 2H),$$



Hu & Sawicki model  $f(R) = R - R_{\text{HS}} \frac{c_1 \left( \frac{R}{R_{\text{HS}}} \right)^n}{c_2 \left( \frac{R}{R_{\text{HS}}} \right)^n + 1},$

Starobinsky model  $f(R) = R + \lambda R_S \left[ \left( 1 + \frac{R^2}{R_S^2} \right)^{-q} - 1 \right],$

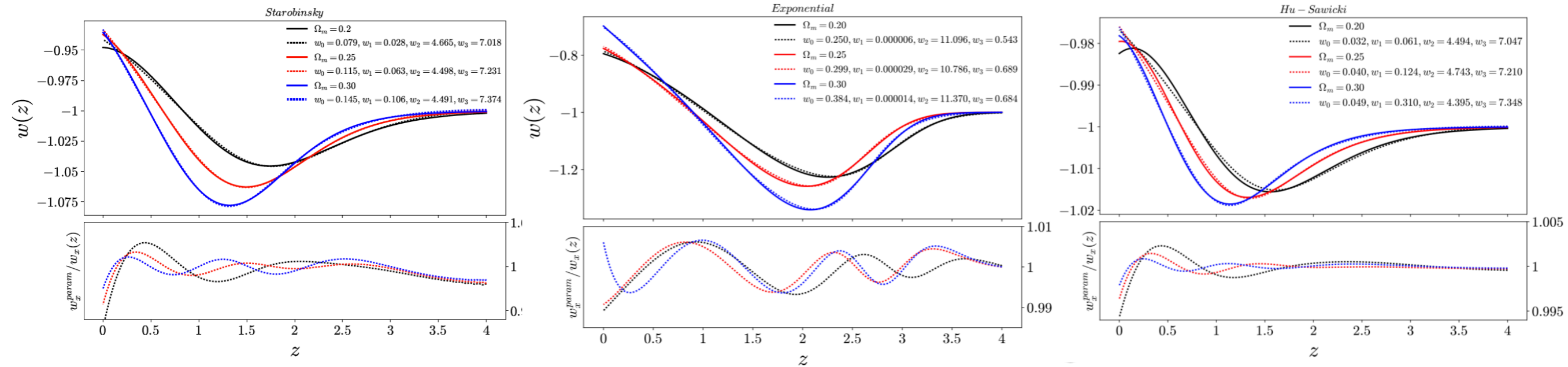
The exponential model  $f(R) = R + \beta R_* (1 - e^{-R/R_*}).$



f(R)-like cosmology parameterisation

$$w(z) = -1 + \frac{w_0}{1 + w_1 z^{w_2}} \cos(w_3 + z)$$

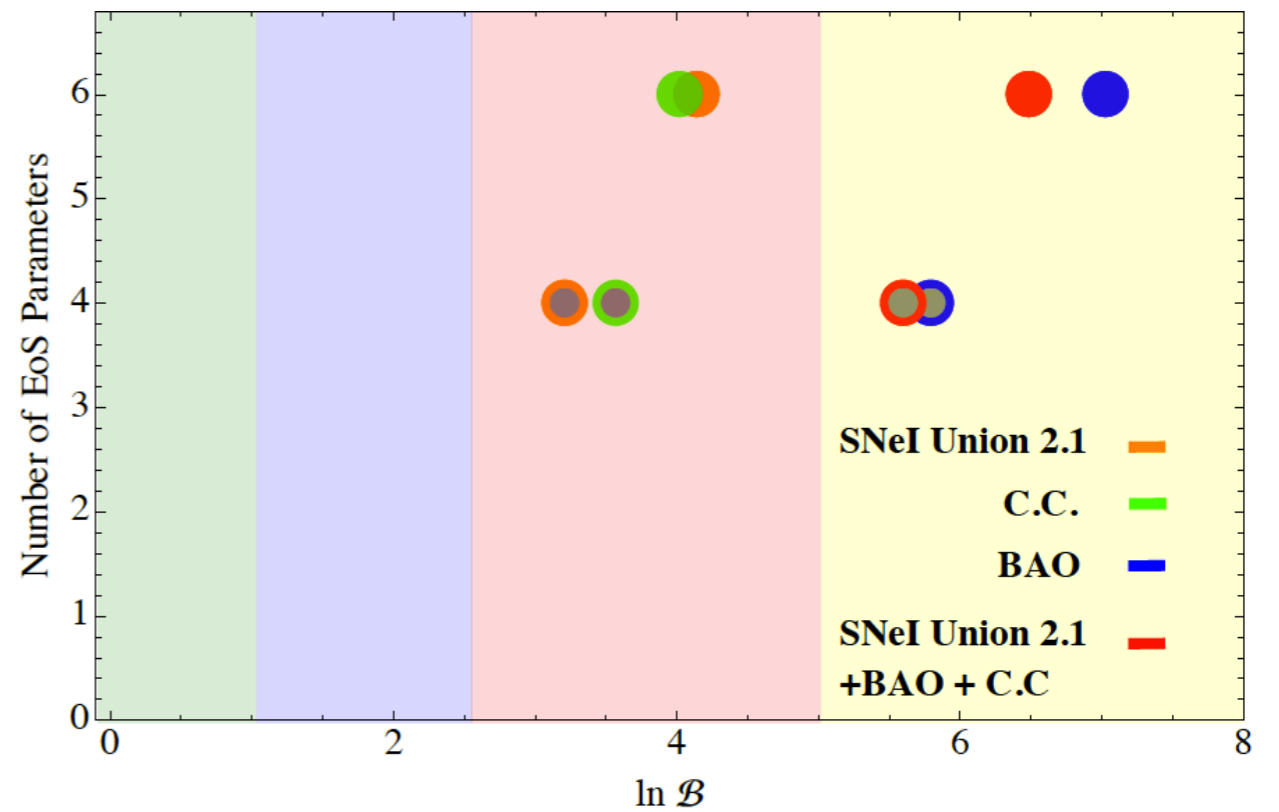
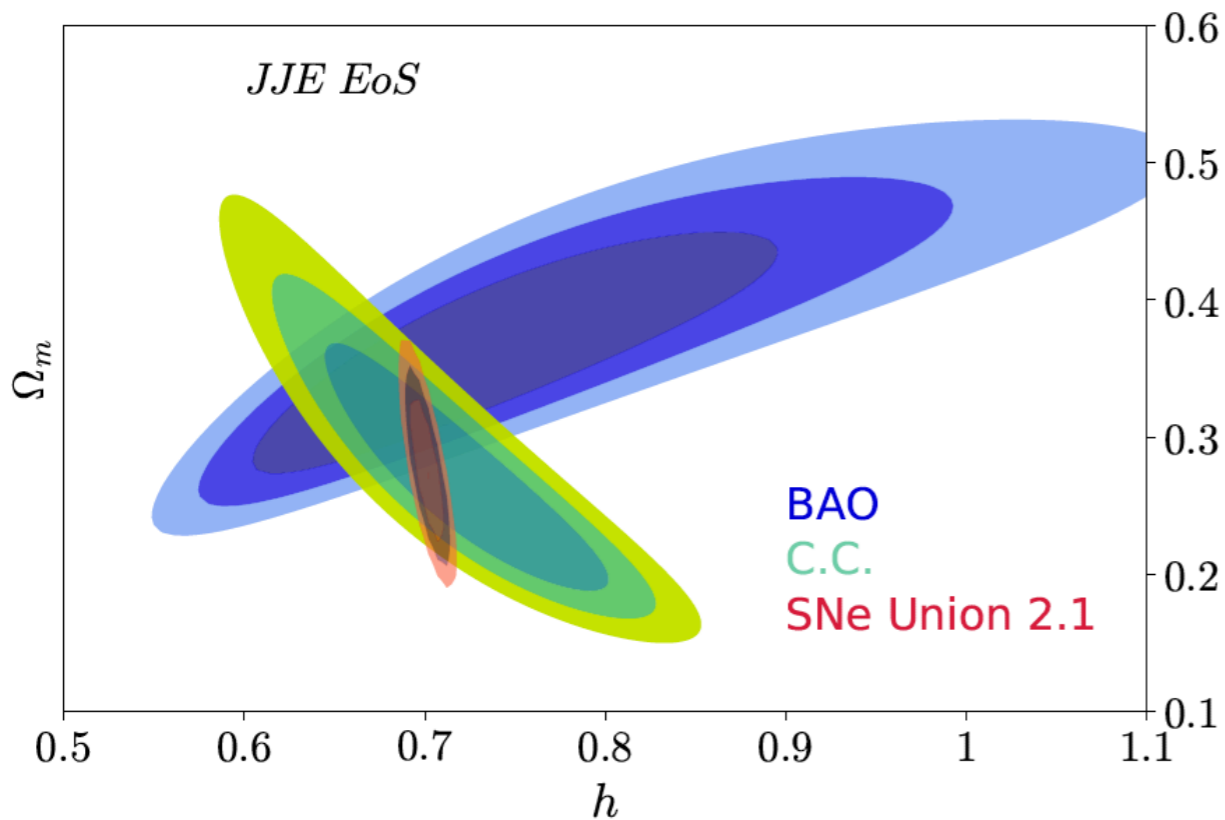
[Jaime L., Jaber, M., Escamilla-R, C. Phys.Rev D98 (2019)]



f(R)-like cosmology parameterisation

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## Current methods: Performing cosmostatistics and statistical diagnostics



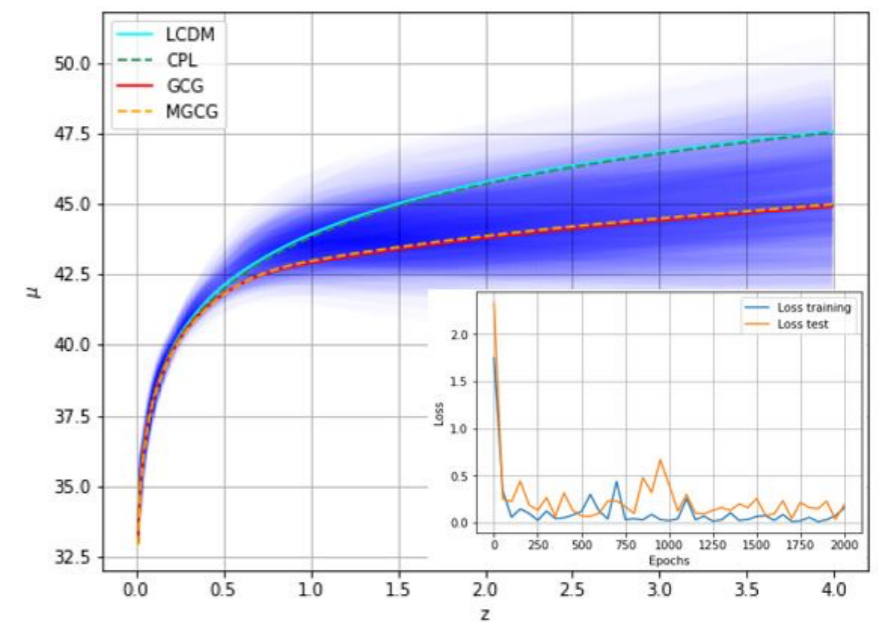
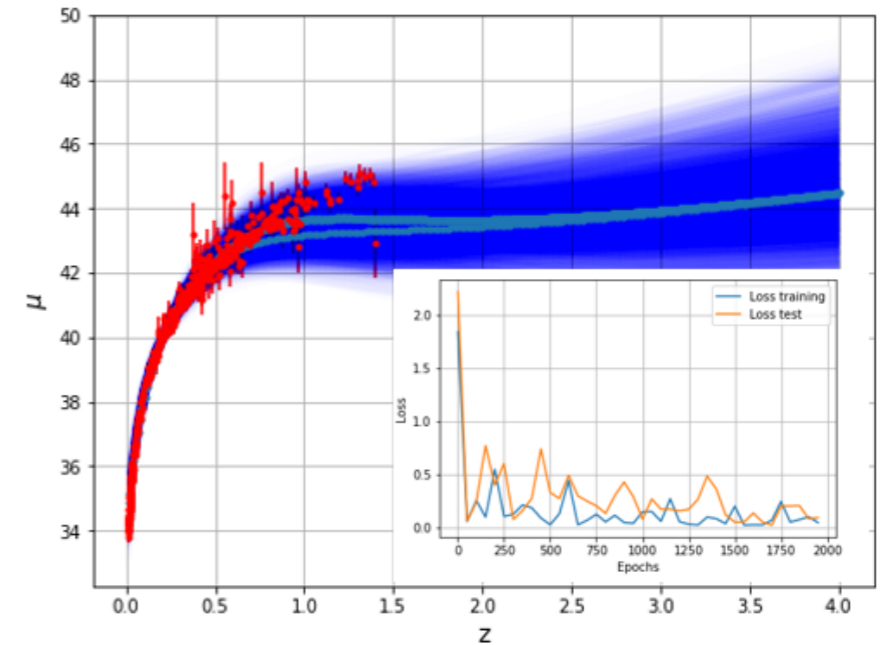
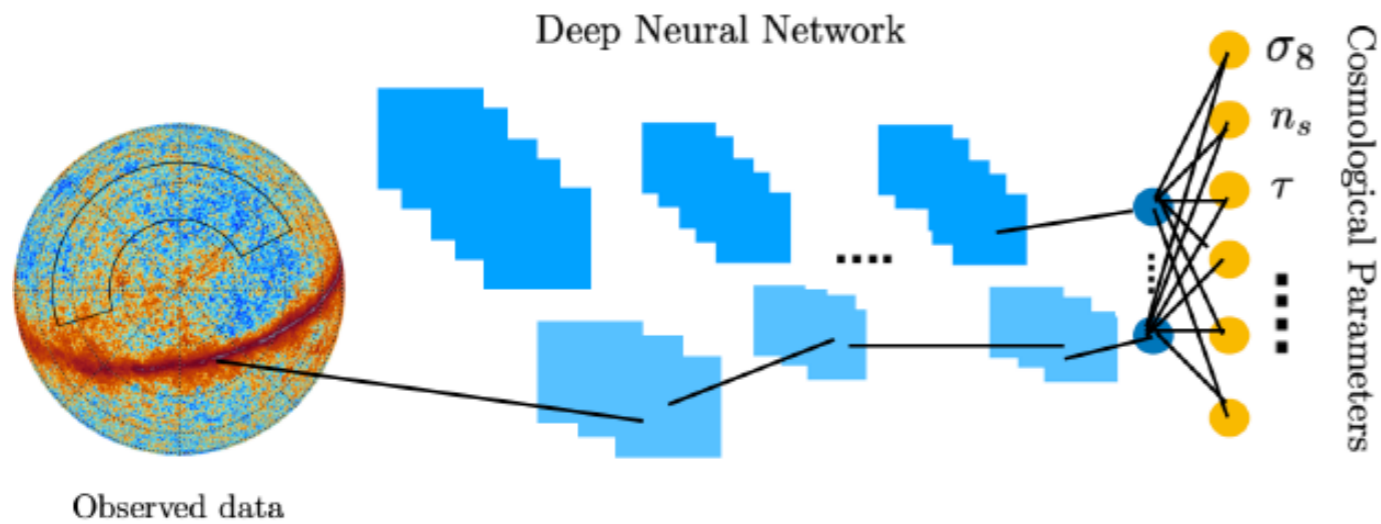
CAMB, CLASS, CosmoMC, MontePython, CosmoSIS, hiCLASS...

To obtain:

- C.L phase-constraints and likelihoods (evidence) of the cosmological parameters and free model parameters
- Model reconstructions: Gaussian Process, Principal Component Analysis, Smoothing Method [T. Holsclaw et al 2010, Huterer, et al 2010, A. Shafieloo et al 2006]
- Non-parametric approaches: Loess-Simex [Escamilla-Rivera, C et al 2014]
- Power spectra (matter, scalar, tensor)

**DLCosmo for gravity:** Code for Bayesian Neural Networks Analysis of gravity models

Working Team: ICN-UNAM, U. Glasgow-LIGO/VIRGO/LISA, U. Naples



[Escamilla-Rivera, C., Carvajal M., Capozziello, S. JCAP 03 (2020) 008]

[Escamilla-Rivera, C. Cosmology 2020 Book 10.5772/intechopen.91466]

[Zamora, C. Escamilla-Rivera, C. (2020) under review by JCAP]

[Escamilla-Rivera, C., Carvajal M., Hendry, M. et al (2020) under review by MNRAS]

[Escamilla-Rivera, C. and Hendry, M. Cosmostatistics. In editorial process by Cambridge Press]

Thanks for your kind attention!



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Horizon 2020

